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Mathematics Subject Classification 2010 Zentralblatt MATH

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- **03** Mathematical logic and foundations
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- **06** Order, lattices, ordered algebraic structures
- 08 General algebraic systems
- 11 Number theory
- 12 Field theory and polynomials
- 13 Commutative algebra
- **14** Algebraic geometry
- 15 Linear and multilinear algebra; matrix theory
- 16 Associative rings and algebras
- 17 Nonassociative rings and algebras
- 18 Category theory, homological algebra
- 19 K-theory
- 20 Group theory and generalizations
- 22 Topological groups, Lie groups
- **26** Real functions
- 28 Measure and integration
- **30** Functions of a complex variable
- 31 Potential theory
- **32** Several complex variables and analytic spaces
- 33 Special functions
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- 35 Partial differential equations
- 37 Dynamical systems and ergodic theory
- 39 Difference and functional equations
- 40 Sequences, series, summability
- 41 Approximations and expansions
- 42 Harmonic analysis on Euclidean spaces
- 43 Abstract harmonic analysis
- 44 Integral transforms, operational calculus
- 45 Integral equations
- 46 Functional analysis

- 47 Operator theory
- **49** Calculus of variations and optimal control; optimization
- **51** Geometry
- 52 Convex and discrete geometry
- 53 Differential geometry
- 54 General topology
- 55 Algebraic topology
- 57 Manifolds and cell complexes
- 58 Global analysis, analysis on manifolds
- **60** Probability theory and stochastic processes
- **62** Statistics
- 65 Numerical analysis
- 68 Computer science
- 70 Mechanics of particles and systems
- 74 Mechanics of deformable solids
- **76** Fluid mechanics
- 78 Optics, electromagnetic theory
- **80** Classical thermodynamics, heat transfer
- 81 Quantum theory
- **82** Statistical mechanics, structure of matter
- 83 Relativity and gravitational theory
- 85 Astronomy and astrophysics
- **86** Geophysics
- **90** Operations research, mathematical programming
- **91** Game theory, economics, social and behavioral sciences
- 92 Biology and other natural sciences
- 93 Systems theory, control
- 94 Information and communication, circuits
- 97 Mathematical education

General 1

00-XX General		00B30	Festschriften
		00B50	Volumes of selected translations
00-01	Instructional exposition (toythooks tutorial papers etc.)	00B55	Miscellaneous volumes of translations
00-02	(textbooks, tutorial papers, etc.) Research exposition (monographs,	00B60	Collections of reprinted articles
00 02	survey articles)		[See also 01A75]
	·	00B99	None of the above, but in this section
00Axx	General and miscellaneous specific topics	01-XX	(History and biography
00A05	General mathematics		[See also the classification num
	Mathematics for nonmathematicians		ber –03 in the other sections]
001100	(engineering, social sciences, etc.)	01-00	General reference works (handbooks,
00A07	Problem books		dictionaries, bibliographies, etc.)
00A08	Recreational mathematics	01-01	Instructional exposition
	[See also 97A20]		(textbooks, tutorial papers, etc.)
00A09	Popularization of mathematics	01-02	Research exposition (monographs,
00A15	Bibliographies	01.06	survey articles)
00A17	External book reviews	01-06	Proceedings, conferences, collections, etc.
00A20	Dictionaries and other general reference works	01-08	Computational methods
00A22	Formularies	01.4	TT: 4 4 4
00A30	Philosophy of mathematics	UIAXX	History of mathematics and mathematicians
	[See also 03A05]	01 A 05	General histories, source books
00A35	Methodology of mathematics, didactics		Ethnomathematics, general
00 4 6	[See also 97Cxx, 97Dxx]		Paleolithic, Neolithic
	Mathematics and music		Indigenous cultures of the Americas
00A66	Mathematics and visual arts, visualiza-		Other indigenous cultures
00A67	Mathematics and architecture	017110	(non-European)
	General applied mathematics	01A15	Indigenous European cultures
001107	(For physics, see 00A79 and Sections 70		(pre-Greek, etc.)
	through 86)	01A16	Egyptian
00A71	Theory of mathematical modeling		Babylonian
00A72	General methods of simulation		Greek, Roman
00A73	Dimensional analysis	01A25	China
00A79	Physics (use more specific entries from	01A27	Japan
	Sections 70 through 86 when possible)		Southeast Asia
00A99	Miscellaneous topics	01A30	Islam (Medieval)
		01A32	India
00Bxx	Conference proceedings and	01A35	Medieval
	collections of papers	01A40	15th and 16th centuries, Renaissance
	Collections of abstracts of lectures		17th century
	Collections of articles of general interest	01A50	18th century
00B15	Collections of articles of miscellaneous		19th century
00000	specific content		20th century
00B20	Proceedings of conferences of general interest		Twenty-first century
00B25	Proceedings of conferences of miscella-		Contemporary
30 22 0	neous specific interest		Future prospectives

01A70	Biographies, obituaries, personalia, bibliographies	03B35	Mechanization of proofs and logical operations [See also 68T15]
01A72	Schools of mathematics	03B40	Combinatory logic and lambda-calculus
	Universities	02042	[See also 68N18]
	Other institutions and academies	U3D42	Logics of knowledge and belief (including belief change)
01A75	Collected or selected works;	03B44	
	reprintings or translations of classics		Temporal logic Modal logic (including the logic of
	[See also 00B60] Sociology (and profession) of mathematics	03043	norms) (For knowledge and belief, see 03B42; for temporal logic, see 03B44; for provability logic, see also 03F45)
	Historiography	03B47	
	Bibliographic studies	03047	Substructural logics (including relevance, entailment, linear logic, Lambel
01A99	Miscellaneous topics		calculus, BCK and BCI logics) (For proof-
03-XX	Mathematical logic and		theoretic aspects see 03F52)
	foundations	03B48	Probability and inductive logic [See also
03-00	General reference works (handbooks,	03B50	60A05] Many-valued logic
02 01	dictionaries, bibliographies, etc.)		Fuzzy logic; logic of vagueness
03-01	Instructional exposition (textbooks, tutorial papers, etc.)	03032	[See also 68T27, 68T37, 94D05]
03-02	Research exposition (monographs,	03B53	Paraconsistent logics
	survey articles)		Intermediate logics
03-03	Historical (must also be assigned at least		Other nonclassical logic
	one classification number from Section		Combined logics
	01)	03B65	Logic of natural languages
03-04	Explicit machine computation and pro-		[See also 68T50, 91F20]
	grams (not the theory of computation or programming)	03B70	Logic in computer science
03-06	Proceedings, conferences, collections,	02000	[See also 68-XX]
00 00	etc.		Other applications of logic None of the above, but in this section
03Axx	Philosophical aspects of logic	03033	None of the above, but in this section
0012/01	and foundations	03Cxx	Model theory
03A05	Philosophical and critical (For philoso-		Equational classes, universal algebra
	phy of mathematics, see also 00A30)		[See also 08Axx, 08Bxx, 18C05]
03A10	Logic in the philosophy of science	03C07	Basic properties of first-order languages
03A99	None of the above, but in this section	00010	and structures
		03C10	Quantifier elimination, model complete
	General logic	02/212	ness andrelated topics
	Classical propositional logic		Finite structures [See also 68Q15, 68Q19]
	Classical first-order logic		Denumerable structures
	Higher-order logic and type theory		Ultraproducts and related constructions
03B20	Subsystems of classical logic		Model-theoretic forcing Other model constructions
02022	(including intuitionistic logic)		
03B22	Abstract deductive systems	03C33	Categoricity and completeness of theories
U3B25	Decidability of theories and sets of sentences [See also 11U05, 12L05, 20F10]	03C40	Interpolation, preservation, definability
03B30	Foundations of classical theories		Classification theory, stability and re-
00 0 00	(including reverse mathematics) [See also 03F35]		lated concepts [See also 03C48]

sentences

03C48	Abstract elementary classes and related topics [See also 03C45]	03D40	Word problems, etc. [See also 06B25, 08A50, 20F10, 68R15]
03C50	Models with special properties (saturated, rigid, etc.)	03D45	Theory of numerations, effectively presented structures [See also 03C57; for in
03C52	Properties of classes of models		tuitionistic and similar approaches see
	Set-theoretic model theory	00050	03F55]
	Effective and recursion-theoretic model theory [See also 03D45]		Recursive equivalence types of sets and structures, isols
03C60	Model-theoretic algebra [See also 08C10,		Hierarchies
	12Lxx, 13L05]	03D60	Computability and recursion theory or ordinals, admissible sets, etc.
03C62	Models of arithmetic and set theory [See also 03Hxx]	03D65	Higher-type and set recursion theory
03C64	Model theory of ordered structures;		Inductive definability
05001	o-minimality	03D75	Abstract and axiomatic computability
03C65	Models of other mathematical theories		and recursion theory
	Other classical first-order model theory	03D78	Computation over the reals
	Logic on admissible sets		(For constructive aspects, see 03F60)
	Other infinitary logic	03D80	Applications of computability and re
	Logic with extra quantifiers and operators [See also 03B42, 03B44, 03B45,	03D99	cursion theory None of the above, but in this section
	03B48]		
03C85	Second- and higher-order model theory		Set theory
	Nonclassical models (Boolean-valued,		Partition relations
	sheaf, etc.)	03E04	Ordered sets and their cofinalities;
03C95	Abstract model theory		pcf theory
03C98	Applications of model theory		Other combinatorial set theory
	[See also 03C60]		Ordinal and cardinal numbers
03C99	None of the above, but in this section	03E15	Descriptive set theory [See also 28A05 54H05]
03Dxx	Computability and recursion theory	03E17	Cardinal characteristics of the contin
	Thue and Post systems, etc.	02.500	uum
03D05	Automata and formal grammars in con-	03E20	Other classical set theory (including functions, relations, and se
	nection with logical questions		algebra)
	[See also 68Q45, 68Q70, 68R15]	03E25	Axiom of choice and related proposi
03D10	Turing machines and related notions		tions
02D15	[See also 68Q05]	03E30	Axiomatics of classical set theory and it
03D13	Complexity of computation (including implicit computational complexity)		fragments
	[See also 68Q15, 68Q17]	03E35	Consistency and independence results
03D20	Recursive functions and relations,	03E40	1
	subrecursive hierarchies	03E45	valued models
03D25	Recursively (computably) enumerable sets and degrees	U3E43	Inner models, including constructibility ordinal definability, and core models
03D28	Other Turing degree structures	03E47	Other notions of set-theoretic definabil
	Other degrees and reducibilities		ity
	Algorithmic randomness and dimension	03E50	Continuum hypothesis and Martin's ax iom [See also 03E57]
03D35	[See also 68Q30] Undecidability and degrees of sets of	03E55	Large cardinals

4 Combinatorics

03E57	Generic absoluteness and forcing axioms [See also 03E50]	03G25	Other algebras related to logic [See also 03F45, 06D20, 06E25, 06F35]
03E60	Determinacy principles	03G27	Abstract algebraic logic
03E65	Other hypotheses and axioms	03G30	Categorical logic, topoi [See also 18B25
03E70	Nonclassical and second-order set theories	03G99	18C05, 18C10] None of the above, but in this section
03E72	Fuzzy set theory		,
03E75	Applications of set theory	03Hxx	Nonstandard models [See also 03C62]
03E99	None of the above, but in this section		Nonstandard models in mathematics [See also 26E35, 28E05, 30G06, 46S20 47S20, 54J05]
03Fxx	Proof theory and constructive mathematics	03H10	Other applications of nonstandard mod-
03F03	Proof theory, general		els (economics, physics, etc.)
03F05	Cut-elimination and normal-form theorems	03H15	Nonstandard models of arithmetic [See also 11U10, 12L15, 13L05]
03F07	Structure of proofs	03H99	None of the above, but in this section
03F10	Functionals in proof theory	05-XX	Combinatorics
03F15	Recursive ordinals and ordinal notations	00 75	(For finite fields, see 11Txx)
03F20	Complexity of proofs	05-00	General reference works (handbooks,
03F25	Relative consistency and interpretations	03-00	dictionaries, bibliographies, etc.)
03F30	First-order arithmetic and fragments	05-01	Instructional exposition
03F35	Second- and higher-order arithmetic and		(textbooks, tutorial papers, etc.)
03F40	fragments [See also 03B30] Gödel numberings and issues of incom-	05-02	Research exposition (monographs, survey articles)
03F45	pleteness Provability logics and related algebras (e.g., diagonalizable algebras)	05-03	Historical (must also be assigned at leas one classification number from Section 01)
03F50	[See also 03B45, 03G25, 06E25] Metamathematics of constructive systems	05-04	Explicit machine computation and programs (not the theory of computation of
03F52	Linear logic and other substructural logics [See also 03B47]	05-06	programming) Proceedings, conferences, collections, etc.
03F55	Intuitionistic mathematics	05 A	
03F60	Constructive and recursive analysis [See also 03B30, 03D45, 03D78, 26E40,		Enumerative combinatorics (For enu- meration in graph theory, see 05C30) Permutations, words, matrices
00565	46S30, 47S30]		Factorials, binomial coefficients, com-
03F65	Other constructive mathematics [See also 03D45]	037110	binatorial functions [See also 11B65
03F99	None of the above, but in this section		33Cxx]
		05A15	Exact enumeration problems, generating functions [See also 33Cxx, 33Dxx]
	Algebraic logic	05A16	Asymptotic enumeration
	Boolean algebras [See also 06Exx] Lattices and related structures		Partitions of integers
03010	[See also 06Bxx]		[See also 11P81, 11P82, 11P83]
03G12	Quantum logic [See also 06C15, 81P10]		Partitions of sets
	Cylindric and polyadic algebras; relation algebras		Combinatorial identities, bijective combinatorics
03G20	Łukasiewicz and Post algebras [See also 06D25, 06D30]	U5A20	Combinatorial inequalities

Combinatorics 5

05A30	<i>q</i> -calculus and related topics	05C40	Connectivity
	[See also 33Dxx]	05C42	Density (toughness, etc.)
05A40	Umbral calculus	05C45	Eulerian and Hamiltonian graphs
05A99	None of the above, but in this section		Graphs and linear algebra
			(matrices, eigenvalues, etc.)
05Bxx	Designs and configurations (For applications of design theory, see 94C30)	05C51	Graph designs and isomomorphic decomposition [See also 05B30]
05B05	Block designs [See also 51E05, 62K10]	05C55	Generalized Ramsey theory
05B07	Triple systems		[See also 05D10]
05B10	Difference sets (number-theoretic,	05C57	Games on graphs
0=54=	group-theoretic, etc.) [See also 11B13]	05660	[See also 91A43, 91A46]
05B15	Orthogonal arrays, Latin squares,	U5C60	Isomorphism problems (reconstruction conjecture, etc.) and homomorphisms
0EP20	Room squares		(subgraph embedding, etc.)
	Matrices (incidence, Hadamard, etc.)	05C62	Graph representations (geometric and
03623	Finite geometries [See also 51D20, 51Exx]		intersection representations, etc.)
05B30			(For graph drawing, see also 68R10)
	[See also 51E30]	05C63	Infinite graphs
05B35	Matroids, geometric lattices	05C65	Hypergraphs
	[See also 52B40, 90C27]	05C69	Dominating sets, independent sets,
05B40	Packing and covering		cliques
OED 4E	[See also 11H31, 52C15, 52C17]	05C70	Factorization, matching, partitioning,
05B45	Tessellation and tiling problems [See also 52C20, 52C22]	05/77	covering and packing
05B50	Polyominoes	05C/2	Fractional graph theory, fuzzy graph theory
	None of the above, but in this section	05C75	Structural characterization of families of
		000,0	graphs
05Cxx	Graph theory (For applications of	05C76	Graph operations
	graphs, see 68R10, 81Q30, 81T15, 82B20,		(line graphs, products, etc.)
05C05	82C20, 90C35, 92E10, 94C15) Trees	05C78	Graph labelling (graceful graphs, bandwidth, etc.)
05C07	Vertex degrees [See also 05E30]	05C80	Random graphs [See also 60B20]
05C10	Planar graphs; geometric and topologi-	05C81	Random walks on graphs
	cal aspects of graph theory [See also 57M15, 57M25]	05C82	Small world graphs, complex networks [See also 90Bxx, 91D30]
05C12	Distance in graphs	05C83	Graph minors
	Coloring of graphs and hypergraphs		Graph algorithms
05C17	Perfect graphs		[See also 68R10, 68W05]
05C20	Directed graphs (digraphs), tournaments	05C90	Applications [See also 68R10, 81Q30, 81T15, 82B20, 82C20, 90C35, 92E10,
05C21	Flows in graphs		94C15]
	Signed and weighted graphs	05C99	None of the above, but in this section
	Graphs and abstract algebra (groups,		
	rings, fields, etc.) [See also 20F65]	05Dxx	Extremal combinatorics
05C30	Enumeration in graph theory	05D05	Extremal set theory
05C31	Graph polynomials		Ramsey theory [See also 05C55]
05C35	Extremal problems [See also 90C35]	05D15	Transversal (matching) theory
05C38	Paths and cycles [See also 90B10]	05D40	Probabilistic methods

05D99	None of the above, but in this section	06Bxx	Lattices [See also 03G10]
OFFra	Alcohyaia sambinatavisa		Structure theory
05E05	Algebraic combinatorics Symmetric functions and generaliza-		Ideals, congruence relations
00100	tions		Representation theory
05E10	Combinatorial aspects of representation	06B20	Varieties of lattices
	theory [See also 20C30]	06B23	1 . 1
05E15	Combinatorial aspects of groups and algebras [See also 14Nxx, 22E45, 33C80]	06B25	Free lattices, projective lattices, word problems [See also 03D40, 08A50, 20F10]
05E18	Group actions on combinatorial structures	06B30	Topological lattices, order topologies [See also 06F30, 22A26, 54F05, 54H12]
05E30	Association schemes, strongly regular graphs	06B35	cations [See also 06B30, 06D10, 06F30]
05E40	Combinatorial aspects of commutative	06 D 75	18B35, 22A26, 68Q55]
	algebra		Generalizations of lattices
05E45	Combinatorial aspects of simplicial complexes	<u></u>	None of the above, but in this section
05E99	None of the above, but in this section	06Cxx	Modular lattices,
06-XX	Order, lattices, ordered algebraic	06605	complemented lattices
	structures [See also 18B35]		Modular lattices, Desarguesian lattices
06-00	General reference works (handbooks,		Semimodular lattices, geometric lattices Complemented lattices, orthocomple-
00 00	dictionaries, bibliographies, etc.)	00C13	mented lattices and posets
06-01	Instructional exposition		[See also 03G12, 81P10]
	(textbooks, tutorial papers, etc.)	06C20	Complemented modular lattices, contin-
06-02	Research exposition (monographs,		uous geometries
	survey articles)	06C99	None of the above, but in this section
06-03	Historical (must also be assigned at least		
	one classification number from Section 01)		Distributive lattices
06-04	Explicit machine computation and pro-		Structure and representation theory
00-01	grams (not the theory of computation or		Complete distributivity
	programming)		Pseudocomplemented lattices
06-06	Proceedings, conferences, collections,		Heyting algebras [See also 03G25]
	etc.	06D22	Frames, locales
06Axx	Ordered sets	06D2E	(For topological questions see 54-XX)
06A05	Total order		Post algebras [See also 03G20]
06A06	Partial order, general	06D30	De Morgan algebras, Łukasiewicz algebras [See also 03G20]
06A07	Combinatorics of partially ordered sets	06D35	MV-algebras
06A11	Algebraic aspects of posets		Lattices and duality
06A12	Semilattices [See also 20M10; for topological semilattices see 22A26]		Fuzzy lattices (soft algebras) and related topics
06A15	Galois correspondences, closure operators	06D75	Other generalizations of distributive lat- tices
06A75	Generalizations of ordered sets	06D99	None of the above, but in this section
06A99	None of the above, but in this section		,

General algebraic systems 7

06Exx	Boolean algebras (Boolean rings) [See also 03G05]		Algebraic structures [See also 03C05] Relational systems, laws of composition
06E05	Structure theory		Structure theory
	Chain conditions, complete algebras		Subalgebras, congruence relations
	Stone spaces (Boolean spaces) and		Automorphisms, endomorphisms
	related structures Ring-theoretic properties		Operations, polynomials, primal algebras
06E25	[See also 16E50, 16G30]	08A45	Equational compactness
00E23	Boolean algebras with additional operations (diagonalizable algebras, etc.) [See also 03G25, 03F45]	08A50	Word problems [See also 03D40, 06B25, 20F10, 68R15]
06E30	Boolean functions [See also 94C10]	08A55	Partial algebras
	Generalizations of Boolean algebras	08A60	Unary algebras
	None of the above, but in this section	08A62	Finitary algebras
		08A65	Infinitary algebras
06Fxx	Ordered structures	08A68	Heterogeneous algebras
06F05	Ordered semigroups and monoids	08A70	Applications of universal algebra
	[See also 20Mxx]		in computer science
06F07	Quantales		Fuzzy algebraic structures
06F10	Noether lattices	08A99	None of the above, but in this section
06F15	Ordered groups [See also 20F60]		
06F20	Ordered abelian groups, Riesz groups,		Varieties [See also 03C05]
	ordered linear spaces [See also 46A40]	08B05	Equational logic, Mal'cev (Mal'tsev) con-
06F25	Ordered rings, algebras, modules	08B10	ditions Congruence modularity
	(For ordered fields, see 12J15; see also	00D10	Congruence modularity, congruence distributivity
0650	13J25, 16W80)	08B15	Lattices of varieties
06F30	Topological lattices, order topologies [See also 06B30, 22A26, 54F05, 54H12]		Free algebras
06F35	BCK-algebras, BCI-algebras		Products, amalgamated products, and
001 55	[See also 03G25]	00220	other kinds of limits and colimits
06F99	None of the above, but in this section		[See also 18A30]
	General algebraic systems	08B26	Subdirect products and subdirect irreducibility
08-00	General reference works (handbooks,	08B30	Injectives, projectives
09 01	dictionaries, bibliographies, etc.)	08B99	None of the above, but in this section
08-01	Instructional exposition (textbooks, tutorial papers, etc.)		
08-02	Research exposition (monographs,	08Cxx	Other classes of algebras
00 02	survey articles)	08C05	Categories of algebras [See also 18C05]
08-03	Historical (must also be assigned at least	08C10	Axiomatic model classes
	one classification number from Section	00 01	[See also 03Cxx, in particular 03C60]
	01)		Quasivarieties
08-04	Explicit machine computation and pro-	08C20	Natural dualities for classes of algebras
	grams (not the theory of computation or programming)	08C99	[See also 06E15, 18A40, 22A30] None of the above, but in this section
08-06	Proceedings, conferences, collections, etc.		

11-XX	(Number theory		Farey sequences; the sequences $1^k, 2^k, \cdots$
11-00	General reference works (handbooks,	11B65	Binomial coefficients; factorials; <i>q</i> -identities [See also 05A10, 05A30]
11-01	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.)	11B68	Bernoulli and Euler numbers and polynomials
11-02	Research exposition (monographs,		Bell and Stirling numbers
11 02	survey articles)		Other combinatorial number theory
11-03	Historical (must also be assigned at least		Special sequences and polynomials
	one classification number from Section 01)	11B85 11B99	Automata sequences None of the above, but in this section
11-04	Explicit machine computation and programs (not the theory of computation or programming)		Polynomials and matrices Polynomials [See also 13F20]
11-06	Proceedings, conferences, collections,		Matrices, determinants [See also 15B36]
11-00	etc.		None of the above, but in this section
11 A xx		110))	Notic of the above, but in this section
ПАХХ	Elementary number theory (For analogues in number fields, see 11R04)	11Dxx	Diophantine equations
11A05	Multiplicative structure; Euclidean algo-	112701	[See also 11Gxx, 14Gxx]
	rithm; greatest common divisors	11D04	Linear equations
11A07	Congruences; primitive roots; residue	11D07	The Frobenius problem
	systems	11D09	Quadratic and bilinear equations
	Power residues, reciprocity	11D25	Cubic and quartic equations
	Arithmetic functions; related numbers; inversion formulas	11D41	Higher degree equations; Fermat's equation
11A41	Primes	11D45	Counting solutions of Diophantine
	Factorization; primality		equations
11A55	Continued fractions (For approximation	11D57	Multiplicative and norm form equations
	results, see 11J70) [See also 11K50, 30B70, 40A15]		Thue-Mahler equations
11A63	Radix representation; digital problems		Exponential equations
	(For metric results, see 11K16)		Rational numbers as sums of fractions
11A67	Other representations	11D72	Equations in many variables [See also 11P55]
11A99	None of the above, but in this section	11D75	Diophantine inequalities [See also 11]25]
			Congruences in many variables
	Sequences and sets		Representation problems
	Density, gaps, topology		[See also 11P55]
11B13	Additive bases, including sumsets	11D88	<i>p</i> -adic and power series fields
11B25	[See also 05B10] Arithmetic progressions	11D99	None of the above, but in this section
11B30	[See also 11N13] Arithmetic combinatorics; higher degree uniformity	11Exx	Forms and linear algebraic groups [See also 19Gxx] (For quadratic forms in linear algebra, see 15A63)
11B34	Representation functions	11E04	Quadratic forms over general fields
11B37	Recurrences (For applications to special functions, see 33-XX)		Quadratic forms over local rings and
11B39	Fibonacci and Lucas numbers and poly-	11F10	fields Forms over real fields
	nomials and generalizations		Quadratic forms over global rings and
11B50	Sequences (mod <i>m</i>)	111116	fields

11E16 General binary quadratic forms 11E20 General ternary and quaternary quadratic forms; forms of more than two variables 11E25 Sums of squares and representations by other particular quadratic forms 11E39 Bilinear and Hermitian forms 11E41 Class numbers of quadratic and Hermitian forms 11E45 Analytic theory (Epstein zeta functions; relations with automorphic forms and functions) 11E57 Classical groups [See also 14Lxx, 20Gxx] 11E70 K-theory of quadratic and Hermitian forms 11E72 Galois cohomology of linear algebraic groups [See also 20G10] 11E76 Forms of degree higher than two 11E81 Algebraic theory of quadratic forms; Witt groups and rings [See also 19G12, 19G24] 11E88 Quadratic spaces; Clifford algebras [See also 15A63, 15A66] 11E95 *p*-adic theory 11E99 None of the above, but in this section 11Fxx Discontinuous groups and automorphic forms [See also 11R39, 11S37, 14Gxx, 14Kxx, 22E50, 22E55, 30F35, 32Nxx] (For relations with quadratic forms, see 11E45) 11F03 Modular and automorphic functions 11F06 Structure of modular groups and generalizations; arithmetic groups [See also 20H05, 20H10, 22E40] 11F11 Holomorphic modular forms of integral weight 11F12 Automorphic forms, one variable 11F20 Dedekind eta function, Dedekind sums 11F22 Relationship to Lie algebras and finite simple groups 11F23 Relations with algebraic geometry and topology 11F25 Hecke-Petersson operators, differential operators (one variable) 11F27 Theta series; Weil representation; theta correspondences 11F30 Fourier coefficients of automorphic

forms

11F32 Modular correspondences, etc. 11F33 Congruences for modular and *p*-adic modular forms [See also 14G20, 22E50] 11F37 Forms of half-integer weight; nonholomorphic modular forms 11F41 Automorphic forms on GL(2); Hilbert and Hilbert-Siegel modular groups and their modular and automorphic forms; Hilbert modular surfaces [See also 14J20] 11F46 Siegel modular groups; Siegel and Hilbert-Siegel modular and automorphic forms 11F50 Jacobi forms 11F52 Modular forms associated to Drinfel'd modules 11F55 Other groups and their modular and automorphic forms (several variables) 11F60 Hecke-Petersson operators, differential operators (several variables) 11F66 Langlands L-functions; one variable Dirichlet series and functional equations 11F67 Special values of automorphic L-series, periods of modular forms, cohomology, modular symbols 11F68 Dirichlet series in several complex variables associated to automorphic forms; Weyl group multiple Dirichlet series 11F70 Representation-theoretic methods; automorphic representations over local and global fields 11F72 Spectral theory; Selberg trace formula 11F75 Cohomology of arithmetic groups 11F80 Galois representations 11F85 *p*-adic theory, local fields [See also 14G20, 22E50] 11F99 None of the above, but in this section 11Gxx Arithmetic algebraic geometry (Diophantine geometry) [See also 11Dxx, 14Gxx, 14Kxx] 11G05 Elliptic curves over global fields [See also 14H52] 11G07 Elliptic curves over local fields [See also 14G20, 14H52]

11G09 Drinfel'd modules; higher-dimensional

motives, etc. [See also 14L05]

11G10 Abelian varieties of dimension > 1

[See also 14Kxx]

11G15	Complex multiplication and moduli of abelian varieties [See also 14K22]	11J13	Simultaneous homogeneous approximation, linear forms
11G16	Elliptic and modular units [See also 11R27]	11J17	Approximation by numbers from a fixed field
11G18	Arithmetic aspects of modular and	11J20	Inhomogeneous linear forms
	Shimura varieties [See also 14G35]	11J25	Diophantine inequalities
11G20	Curves over finite and local fields [See also 14H25]	11J54	[See also 11D75] Small fractional parts of polynomials
11G25	Varieties over finite and local fields [See also 14G15, 14G20]	11171	and generalizations
11G30	Curves of arbitrary genus or genus $\neq 1$	11J61	Approximation in non-Archimedean valuations
	over global fields [See also 14H25]	11J68	Approximation to algebraic numbers
11G32	Dessins d'enfants, Belyĭ theory	11J70	Continued fractions and generalizations
11G35	Varieties over global fields	44184	[See also 11A55, 11K50]
11010	[See also 14G25]	11J71	Distribution modulo one [See also 11K06]
11G40	<i>L</i> -functions of varieties over global fields; Birch-Swinnerton-Dyer conjecture [See also 14G10]	11J72	Irrationality; linear independence over a field
11G42	Arithmetic mirror symmetry	11J81	Transcendence (general theory)
	[See also 14J33]	11J82	Measures of irrationality and of tran-
11G45	Geometric class field theory	11100	scendence
	[See also 11R37, 14C35, 19F05]	11J83	Metric theory
	Heights [See also 14G40, 37P30]	11J85	Algebraic independence; Gel'fond's method
11G55	Polylogarithms and relations with <i>K</i> -theory	11J86	Linear forms in logarithms;
11G99	None of the above, but in this section	11J87	Baker's method Schmidt Subspace Theorem and appli-
11Hxx	Geometry of numbers (For applications in coding theory, see 94B75)	11J89	cations Transcendence theory of elliptic and abelian functions
11H06	Lattices and convex bodies [See also 11P21, 52C05, 52C07]	11J91	Transcendence theory of other special functions
11H16	Nonconvex bodies	11J93	Transcendence theory of Drinfel'd and
11H31	Lattice packing and covering [See also 05B40, 52C15, 52C17]	11J95	<i>t</i> -modules Results involving abelian varieties
11H46	Products of linear forms	11J97	Analogues of methods in Nevanlinna
	Minima of forms	44700	theory (work of Vojta et al.)
11H55	Quadratic forms (reduction theory, extreme forms, etc.)	11J99 	None of the above, but in this section
11H56	Automorphism groups of lattices	11Kxx	Probabilistic theory: distribution mod-
	Mean value and transfer theorems	447606	ulo 1; metric theory of algorithms
11H71	Relations with coding theory	11K06	General theory of distribution modulo 1
11H99	None of the above, but in this section	11K16	[See also 11J71] Normal numbers, radix expansions,
		111110	Pisot numbers, Salem numbers, good
11Jxx	Diophantine approximation, transcendental number theory [See also 11K60]	111/21	lattice points, etc. [See also 11A63]
11J04	Homogeneous approximation to one		Special sequences Well-distributed sequences and other
	number	11100	variations
11J06	Markov and Lagrange spectra and generalizations	11K38	Irregularities of distribution, discrepancy [See also 11Nxx]

- 11K41 Continuous, *p*-adic and abstract analogues
- 11K45 Pseudo-random numbers; Monte Carlo methods
- 11K50 Metric theory of continued fractions [See also 11A55, 11J70]
- 11K55 Metric theory of other algorithms and expansions; measure and Hausdorff dimension [See also 11N99, 28Dxx]
- 11K60 Diophantine approximation [See also 11Jxx]
- 11K65 Arithmetic functions [See also 11Nxx]
- 11K70 Harmonic analysis and almost periodicity
- 11K99 None of the above, but in this section

11Lxx Exponential sums and character sums (For finite fields, see 11Txx)

- 11L03 Trigonometric and exponential sums, general
- 11L05 Gauss and Kloosterman sums; generalizations
- 11L07 Estimates on exponential sums
- 11L10 Jacobsthal and Brewer sums; other complete character sums
- 11L15 Weyl sums
- 11L20 Sums over primes
- 11L26 Sums over arbitrary intervals
- 11L40 Estimates on character sums
- 11L99 None of the above, but in this section

11Mxx Zeta and L-functions: analytic theory

- 11M06 $\zeta(s)$ and $L(s, \chi)$
- 11M20 Real zeros of $L(s, \chi)$; results on $L(1, \chi)$
- 11M26 Nonreal zeros of $\zeta(s)$ and $L(s, \chi)$; Riemann and other hypotheses
- 11M32 Multiple Dirichlet series and zeta functions and multizeta values
- 11M35 Hurwitz and Lerch zeta functions
- 11M36 Selberg zeta functions and regularized determinants; applications to spectral theory, Dirichlet series, Eisenstein series, etc. Explicit formulas
- 11M38 Zeta and *L*-functions in characteristic *p*
- 11M41 Other Dirichlet series and zeta functions (For local and global ground fields, see 11R42, 11R52, 11S40, 11S45; for algebrogeometric methods, see 14G10; see also 11E45, 11F66, 11F70, 11F72)

- 11M45 Tauberian theorems [See also 40E05]
- 11M50 Relations with random matrices
- 11M55 Relations with noncommutative geometry
- 11M99 None of the above, but in this section

11Nxx Multiplicative number theory

- 11N05 Distribution of primes
- 11N13 Primes in progressions [See also 11B25]
- 11N25 Distribution of integers with specified multiplicative constraints
- 11N30 Turán theory [See also 30Bxx]
- 11N32 Primes represented by polynomials; other multiplicative structure of polynomial values
- 11N35 Sieves
- 11N36 Applications of sieve methods
- 11N37 Asymptotic results on arithmetic functions
- 11N45 Asymptotic results on counting functions for algebraic and topological structures
- 11N56 Rate of growth of arithmetic functions
- 11N60 Distribution functions associated with additive and positive multiplicative functions
- 11N64 Other results on the distribution of values or the characterization of arithmetic functions
- 11N69 Distribution of integers in special residue classes
- 11N75 Applications of automorphic functions and forms to multiplicative problems [See also 11Fxx]
- 11N80 Generalized primes and integers
- 11N99 None of the above, but in this section

11Pxx Additive number theory; partitions

- 11P05 Waring's problem and variants
- 11P21 Lattice points in specified regions
- 11P32 Goldbach-type theorems; other additive questions involving primes
- 11P55 Applications of the Hardy-Littlewood method [See also 11D85]
- 11P70 Inverse problems of additive number theory, including sumsets
- 11P81 Elementary theory of partitions [See also 05A17]
- 11P82 Analytic theory of partitions

11P83	Partitions; congruences and congruential restrictions	11R65	Class groups and Picard groups of orders
11P84	Partition identities; identities of Rogers-	11R70	K-theory of global fields [See also 19Fxx]
	Ramanujan type	11R80	Totally real fields [See also 12J15]
11P99	None of the above, but in this section	11R99	None of the above, but in this section
11Rxx	Algebraic number theory: global	11Sxx	Algebraic number theory:
	fields (For complex multiplication, see		local and p -adic fields
11D04	11G15)	11S05	Polynomials
11K04	Algebraic numbers; rings of algebraic integers	11S15	Ramification and extension theory
11R06	PV-numbers and generalizations; other		Galois theory
111100	special algebraic numbers; Mahler mea-	11S23	Integral representations
	sure	11S25	0)
11R09	Polynomials (irreducibility, etc.)	11521	[See also 12Gxx, 16H05]
	Quadratic extensions	11331	Class field theory; <i>p</i> -adic formal groups [See also 14L05]
	Cubic and quartic extensions	11S37	Langlands-Weil conjectures, nonabelian
	Cyclotomic extensions		class field theory [See also 11Fxx, 22E50]
	Other abelian and metabelian extensions	11S40	Zeta functions and L-functions [See also
	Other number fields		11M41, 19F27]
	Iwasawa theory	11S45	Algebras and orders, and their zeta func-
	Units and factorization		tions [See also 11R52, 11R54, 16Hxx, 16Kxx]
11K29	Class numbers, class groups, discriminants	11S70	K-theory of local fields [See also 19Fxx]
11R32	Galois theory	11S80	Other analytic theory (analogues of beta
	Integral representations related to alge-	11000	and gamma functions, <i>p</i> -adic integra-
	braic numbers; Galois module structure		tion, etc.)
	of rings of integers [See also 20C10]	11S82	Non-Archimedean dynamical systems
11R34	Galois cohomology		[See mainly 37Pxx]
11D27	[See also 12Gxx, 19A31]	11S85	Other nonanalytic theory
	Class field theory	11S90	Prehomogeneous vector spaces
11K39	Langlands-Weil conjectures, nonabelian class field theory [See also 11Fxx, 22E55]	11S99	None of the above, but in this section
11R42	Zeta functions and <i>L</i> -functions of number fields [See also 11M41, 19F27]	11Txx	Finite fields and commutative rings
11R44	Distribution of prime ideals	11T06	(number-theoretic aspects)
	[See also 11N05]		Polynomials
11R45	Density theorems		Cyclotomy Exponential sums
11R47	Other analytic theory [See also 11Nxx]		Other character sums and Gauss sums
11R52	Quaternion and other division algebras:		Structure theory
44054	arithmetic, zeta functions		Arithmetic theory of polynomial rings
11R54	Other algebras and orders, and their zeta and <i>L</i> -functions [See also 11S45, 16Hxx,		over finite fields
	16Kxx]	11T60	Finite upper half-planes
11R56	Adèle rings and groups	11T71	
	Arithmetic theory of algebraic function	11T99	None of the above, but in this section
11R60	fields [See also 14-XX] Cyclotomic function fields (class groups,		
111/00	Bernoulli objects, etc.)		

11I Jvv	Connections with logic	12D10	Polynomials: location of zeros (algebraic
	Decidability [See also 03B25]		theorems) (For the analytic theory, see
	Ultraproducts [See also 03C20]		26C10, 30C15)
	Model theory [See also 03Cxx]	12D15	Fields related with sums of squares (for-
	Nonstandard arithmetic		mally real fields, Pythagorean fields, etc.) [See also 11Exx]
11010	[See also 03H15]	12D00	None of the above, but in this section
11U99	None of the above, but in this section	12077	None of the above, but in this section
		12Exx	General field theory
11Yxx	Computational number theory [See		Polynomials (irreducibility, etc.)
	also 11-04]	12E10	•
	Factorization	12E12	Equations
	Primality		Skew fields, division rings
	Algorithms; complexity [See also 68Q25]		[See also 11R52, 11R54, 11S45, 16Kxx]
	Analytic computations	12E20	Finite fields (field-theoretic aspects)
11Y40	Algebraic number theory computations	12E25	Hilbertian fields; Hilbert's irreducibility
11Y50	Computer solution of Diophantine		theorem
	equations	12E30	Field arithmetic
11Y55	Calculation of integer sequences	12E99	None of the above, but in this section
11Y60	Evaluation of constants		
11Y65	Continued fraction calculations	12Fxx	Field extensions
11Y70	Values of arithmetic functions; tables	12F05	Algebraic extensions
11Y99	None of the above, but in this section	12F10	Separable extensions, Galois theory
		12F12	Inverse Galois theory
11Zxx	Miscellaneous applications of number	12F15	Inseparable extensions
	theory	12F20	Transcendental extensions
11Z05	Miscellaneous applications of number theory	12F99	None of the above, but in this section
11 Z 99	None of the above, but in this section	12Gxx	Homological methods (field theory)
12-XX	Field theory and polynomials		Galois cohomology
12-00	General reference works (handbooks,		[See also 14F22, 16Hxx, 16K50]
12-00	dictionaries, bibliographies, etc.)	12G10	Cohomological dimension
12-01	Instructional exposition (textbooks, tutorial papers, etc.)	12G99	None of the above, but in this section
12-02	Research exposition (monographs,	12Hxx	Differential and difference algebra
12 02	survey articles)		Differential algebra [See also 13Nxx]
12-03	Historical (must also be assigned at least		Difference algebra [See also 39Axx]
12 00	one classification number from Section		Abstract differential equations
	01)		[See also 34Mxx]
12-04	Explicit machine computation and pro-	12H25	<i>p</i> -adic differential equations
	grams (not the theory of computation or		[See also 11S80, 14G20]
	programming)	12H99	None of the above, but in this section
12-06	Proceedings, conferences, collections,		
	etc.	12Jxx	Topological fields
12Dxx	Real and complex fields	12J05	Normed fields
	Polynomials: factorization	12J10	Valued fields
	•	12J12	Formally <i>p</i> -adic fields

14 Commutative algebra

12J15	Ordered fields	13A15	Ideals; multiplicative ideal theory
12J17	Topological semifields		Valuations and their generalizations
12J20	General valuation theory		[See also 12J20]
,	[See also 13A18]	13A30	Associated graded rings of ideals (Rees
12J25	Non-Archimedean valued fields		ring, form ring), analytic spread and re-
-	[See also 30G06, 32P05, 46S10, 47S10]		lated topics
12J27	Krasner-Tate algebras [See mainly	13A35	Characteristic p methods (Frobenius en-
	32P05; see also 46S10, 47S10]		domorphism) and reduction to charac-
12J99	None of the above, but in this section		teristic <i>p</i> ; tight closure [See also 13B22]
		13A50	Actions of groups on commutative rings;
12Kxx	Generalizations of fields	12.100	invariant theory [See also 14L24]
12K05	Near-fields [See also 16Y30]	13A99	None of the above, but in this section
12K10	Semifields [See also 16Y60]		
12K99	None of the above, but in this section		Ring extensions and related topics
			Extension theory
12Lxx	Connections with logic		Galois theory
12L05	Decidability [See also 03B25]		Morphisms
12L10	Ultraproducts [See also 03C20]	13B21	
12L12	Model theory [See also 03C60]	12B22	down Integral closure of rings and ideals
12L15	Nonstandard arithmetic	13022	[See also 13A35]; integrally closed rings,
	[See also 03H15]		related rings (Japanese, etc.)
12L99	None of the above, but in this section	13B25	
		10020	[See also 11C08, 11T06, 13F20, 13M10]
12Yxx	Computational aspects of field theory	13B30	
	and polynomials	13B30	
	and polynomials Computational aspects of field theory	13B30 13B35	Rings of fractions and localization [See also 16S85]
12Y05	and polynomials Computational aspects of field theory and polynomials		Rings of fractions and localization [See also 16S85] Completion [See also 13J10]
12Y05	and polynomials Computational aspects of field theory	13B35	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation
12Y05 12Y99	and polynomials Computational aspects of field theory and polynomials	13B35 13B40	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25]
12Y05 12Y99	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section	13B35 13B40	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation
12Y05 12Y99 13-XX 13-00	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra	13B35 13B40 13B99	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section
12Y05 12Y99 13-XX	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition	13B35 13B40 13B99 13Cxx	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals
12Y05 12Y99 13-XX 13-00	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.)	13B35 13B40 13B99 13Cxx 13C05	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems
12Y05 12Y99 13-XX 13-00	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs,	13B35 13B40 13B99 13Cxx 13C05	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems
12Y05 12Y99 13-XX 13-00 13-01 13-02	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles)	13B35 13B40 13B99 13Cxx 13C05 13C10	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals
12Y05 12Y99 13-XX 13-00 13-01	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs,	13B35 13B40 13B99 13Cxx 13C05 13C10	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13]
12Y05 12Y99 13-XX 13-00 13-01 13-02	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals
12Y05 12Y99 13-XX 13-00 13-01 13-02	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming)	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13 13C14	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types Cohen-Macaulay modules
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections,	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13 13C14	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types Cohen-Macaulay modules [See also 13H10]
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03 13-04	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming)	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13 13C14 13C15	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types Cohen-Macaulay modules [See also 13H10] Dimension theory, depth, related rings
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03 13-04 13-06	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections,	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13 13C14 13C15 13C20	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types Cohen-Macaulay modules [See also 13H10] Dimension theory, depth, related rings (catenary, etc.) Class groups [See also 11R29] Linkage, complete intersections and de-
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03 13-04 13-06 13Axx	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc.	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13 13C14 13C15 13C20	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types Cohen-Macaulay modules [See also 13H10] Dimension theory, depth, related rings (catenary, etc.) Class groups [See also 11R29] Linkage, complete intersections and determinantal ideals [See also 14M06,
12Y05 12Y99 13-XX 13-00 13-01 13-02 13-03 13-04 13-06 13Axx 13A02	and polynomials Computational aspects of field theory and polynomials None of the above, but in this section Commutative algebra General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General commutative ring theory	13B35 13B40 13B99 13Cxx 13C05 13C10 13C11 13C12 13C13 13C14 13C15 13C20 13C40	Rings of fractions and localization [See also 16S85] Completion [See also 13J10] Étale and flat extensions; Henselization; Artin approximation [See also 13J15, 14B12, 14B25] None of the above, but in this section Theory of modules and ideals Structure, classification theorems Projective and free modules and ideals [See also 19A13] Injective and flat modules and ideals Torsion modules and ideals Other special types Cohen-Macaulay modules [See also 13H10] Dimension theory, depth, related rings (catenary, etc.)

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13C99	None of the above, but in this section		Excellent rings Seminormal rings
13Dxx	Homological methods (For noncommutative rings, see 16Exx; for general categories, see 18Cxx)	13F50	Rings with straightening laws, Hodge algebras
13D02	gories, see 18Gxx) Syzygies, resolutions, complexes	13F55	Stanley-Reisner face rings; simplicial complexes [See also 55U10]
	(Co)homology of commutative rings	13F60	Cluster algebras
	and algebras (e.g., Hochschild, André- Quillen, cyclic, dihedral, etc.)	13F99	None of the above, but in this section
	Homological dimension	13Gxx	Integral domains
13D07	Homological functors on modules		Integral domains
12000	(Tor, Ext, etc.)	13G99	None of the above, but in this section
	Derived categories Deformations and infinitesimal methods		
13D10	[See also 14B10, 14B12, 14D15, 32Gxx]	13Hxx	Local rings and semilocal rings
13D15	Grothendieck groups, <i>K</i> -theory		Regular local rings
	[See also 14C35, 18F30, 19Axx, 19D50]	13H10	Special types (Cohen-Macaulay, Goren-
13D22	Homological conjectures	40774	stein, Buchsbaum, etc.) [See also 14M05]
	(intersection theorems)	13H15	Multiplicity theory and related topics
	Torsion theory [See also 13C12, 18E40]	121100	[See also 14C17] None of the above, but in this section
13D40	Hilbert-Samuel and Hilbert-Kunz functions; Poincaré series		None of the above, but in this section
13D45	Local cohomology [See also 14B15]	13Jxx	Topological rings and modules
13D99	None of the above, but in this section	4.010.5	[See also 16W60, 16W80]
-		13J05	Power series rings [See also 13F25]
13Exx	Chain conditions, finiteness conditions	13J07	Analytical algebras and rings [See also 32B05]
13E05	Noetherian rings and modules	13J10	Complete rings, completion
13E10	Artinian rings and modules,	10,10	[See also 13B35]
	finite-dimensional algebras	13J15	Henselian rings [See also 13B40]
13E15	Rings and modules of finite generation	13J20	Global topological rings
12E00	or presentation; number of generators	13J25	Ordered rings [See also 06F25]
13E99	None of the above, but in this section	13J30	Real algebra [See also 12D15, 14Pxx]
400		13J99	None of the above, but in this section
	Arithmetic rings and other special rings		
13F03	Dedekind, Prüfer, Krull and Mori rings and their generalizations	13Lxx	Applications of logic to commutative algebra [See also 03Cxx, 03Hxx]
13F07	Euclidean rings and generalizations	13L05	Applications of logic to commutative al-
13F10	Principal ideal rings	10200	gebra [See also 03Cxx, 03Hxx]
13F15	Rings defined by factorization properties (e.g., atomic, factorial, half-factorial) [See also 13A05, 14M05]	13L99	
13F20	Polynomial rings and ideals; rings of	13Mxx	Finite commutative rings (For number-
	integer-valued polynomials	4.5.	theoretic aspects, see 11Txx)
	[See also 11C08, 13B25]		Structure
13F25	Formal power series rings		Polynomials
	[See also 13J05]		None of the above, but in this section
13F30	Valuation rings [See also 13A18]	sy	nopa13NxxDifferential algebra [See also 12H05, 14F10]
	Witt vectors and related rings		1500 3160 17HU3 1/1HUU

16 Algebraic geometry

	Modules of differentials	14Bxx	Local theory
	Rings of differential operators and their modules [See also 16S32, 32C38]	14B05	Singularities [See also 14E15, 14H20, 14J17, 32Sxx, 58Kxx]
	Derivations	14B07	Deformations of singularities
13N99	None of the above, but in this section		[See also 14D15, 32S30]
13Pvv	Computational aspects and		Infinitesimal methods [See also 13D10]
	applications [See also 14Qxx, 68W30]		Local deformation theory, Artin approximation, etc. [See also 13B40, 13D10]
	Polynomials, factorization [See also 12Y05]	14B15	Local cohomology [See also 13D45, 32C36]
13P10	Gröbner bases; other bases for ideals and	14B20	Formal neighborhoods
	modules (e.g., Janet and border bases)	14B25	Local structure of morphisms: étale, flat,
13P15	Solving polynomial systems; resultants		etc. [See also 13B40]
13P20	Computational homological algebra [See also 13Dxx]	14B99	None of the above, but in this section
13P25	Applications of commutative algebra	14Cxx	Cycles and subschemes
	(e.g., to statistics, control theory, opti-		Parametrization
12D00	mization, etc.)		(Chow and Hilbert schemes)
	None of the above, but in this section Algebraic geometry	14C15	(Equivariant) Chow groups and rings; motives
		14C17	Intersection theory, characteristic
14-00	General reference works (handbooks,		classes, intersection multiplicities
14-01	dictionaries, bibliographies, etc.) Instructional exposition		[See also 13H15]
14-01	(textbooks, tutorial papers, etc.)	14C20	Divisors, linear systems, invertible sheaves
14-02	Research exposition (monographs,	14C21	Pencils, nets, webs [See also 53A60]
4400	survey articles)	14C22	Picard groups
14-03	Historical (must also be assigned at least		Algebraic cycles
	one classification number from Section		Transcendental methods, Hodge theory
14.04	01)		[See also 14D07, 32G20, 32J25, 32S35],
14-04	Explicit machine computation and programs (not the theory of computation or		Hodge conjecture
	programming)	14C34	Torelli problem [See also 32G20]
14-06	Proceedings, conferences, collections,	14C35	Applications of methods of algebraic
11 00	etc.		K-theory [See also 19Exx]
14Axx	Foundations	14C40	Riemann-Roch theorems
	Relevant commutative algebra	14000	[See also 19E20, 19L10]
	[See also 13-XX]	14C99	None of the above, but in this section
	Varieties and morphisms	14Dxx	Families, fibrations
	Schemes and morphisms		Structure of families (Picard-Lefschetz,
14A20	Generalizations	11200	monodromy, etc.)
	(algebraic spaces, stacks)	14D06	Fibrations, degenerations
14A22	Noncommutative algebraic geometry		Variation of Hodge structures
14405	[See also 16S38]	11207	[See also 32G20]
	Elementary questions	14D10	Arithmetic ground fields
14A99	None of the above, but in this section		(finite, local, global)
		14D15	Formal methods; deformations
			[See also 13D10, 14B07, 32Gxx]

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14D20	Algebraic moduli problems, moduli of vector bundles (For analytic moduli	14F40	de Rham cohomology [See also 14C30, 32C35, 32L10]
14D01	problems, see 32G13)	14F42	Motivic cohomology; motivic homotopy
14021	Applications of vector bundles and moduli spaces in mathematical physics	14F43	theory Other algebro-geometric (co)homolo-
	(twistor theory, instantons, quantum field theory)	14143	gies (e.g., intersection, equivariant, Lawson, Deligne (co)homologies)
14D22	Fine and coarse moduli spaces	14F45	Topological properties
	Stacks and moduli problems	14F99	None of the above, but in this section
	Geometric Langlands program: algebro-	111//	Trone of the above, but in this section
	geometric aspects [See also 22E57]	14Gvv	Arithmetic problems. Diophantine ge-
14D99	None of the above, but in this section	110	ometry [See also 11Dxx, 11Gxx]
		14G05	Rational points
	Birational geometry	14G10	Zeta-functions and related questions
14E05	Rational and birational maps		[See also 11G40] (Birch-Swinnerton-
14E07	Birational automorphisms, Cremona	44045	Dyer conjecture)
	group and generalizations		Finite ground fields
	Rationality questions [See also 14M20]		Positive characteristic ground fields
14E15	Global theory and resolution of singularities [Second 20045]		Local ground fields
1/E16	larities [See also 14B05, 32S20, 32S45]		Rigid analytic geometry
	McKay correspondence		Global ground fields
	Arcs and motivic integration Coverings [See also 14H30]	14G2/	Other nonalgebraically closed ground fields
	Ramification problems [See also 11S15]	14G32	Universal profinite groups (relationship
14E25	Embeddings		to moduli spaces, projective and moduli towers, Galois theory)
	Minimal model program (Mori theory, extremal rays)	14G35	Modular and Shimura varieties [See also 11F41, 11F46, 11G18]
14E99	None of the above, but in this section	14G40	Arithmetic varieties and schemes;
-			Arakelov theory; heights
	(Co)homology theory [See also 13Dxx]		[See also 11G50, 37P30]
14F05	Sheaves, derived categories of sheaves and related constructions [See also	14G50	Applications to coding theory and cryp-
	14H60, 14J60, 18F20, 32Lxx, 46M20]	1.1000	tography [See also 94A60, 94B27, 94B40]
14F10	Differentials and other special sheaves;	14G99	None of the above, but in this section
	D-modules; Bernstein-Sato ideals and	1411	
	polynomials [See also 13Nxx, 32C38]		Curves
14F17	Vanishing theorems [See also 32L20]	141103	Algebraic functions; function fields [See also 11R58]
14F18	Multiplier ideals	14H10	Families, moduli (algebraic)
14F20	Étale and other Grothendieck topologies		Families, moduli (analytic)
	and cohomologies		[See also 30F10, 32Gxx]
14F22	Brauer groups of schemes [See also 12G05, 16K50]	14H20	Singularities, local rings
14F25	Classical real and complex cohomology	14H25	[See also 13Hxx, 14B05] Arithmetic ground fields
14F30	<i>p</i> -adic cohomology, crystalline cohomol-	1-11-12-0	[See also 11Dxx, 11G05, 14Gxx]
	ogy	14H30	Coverings, fundamental group
14F35	Homotopy theory; fundamental groups		[See also 14E20, 14F35]
	[See also 14H30]	14H37	Automorphisms

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14H40	Jacobians, Prym varieties [See also 32G20]	14J70	Hypersurfaces
14H42	Theta functions; Schottky problem	14J80	Topology of surfaces (Donaldson polynomials, Seiberg-Witten invariants)
	[See also 14K25, 32G20]	14J81	Relationships with physics
	Special curves and curves of low genus	14J99	None of the above, but in this section
14H50	Plane and space curves		
14H51	Special divisors (gonality, Brill-Noether theory)		Abelian varieties and schemes
1/1152	•		Isogeny
141132	Elliptic curves [See also 11G05, 11G07, 14Kxx]		Algebraic theory
14H55	Riemann surfaces; Weierstrass points; gap sequences [See also 30Fxx]	14K10	Algebraic moduli, classification [See also 11G15]
141157		14K12	Subvarieties
14П3/	Dessins d'enfants theory (For arithmetic aspects, see 11G32)	14K15	Arithmetic ground fields [See also 11Dxx, 11Fxx, 11Gxx, 14Gxx]
14H60	Vector bundles on curves and their moduli [See also 14D20, 14F05]	14K20	Analytic theory; abelian integrals and
14H70	Relationships with integrable systems	14K22	differentials Complex multiplication [See also 11G15]
	Relationships with physics		Theta functions [See also 14H42]
	None of the above, but in this section		Picard schemes, higher Jacobians
	<u> </u>	14100	[See also 14H40, 32G20]
14Jxx	Surfaces and higher-dimensional varieties (For analytic theory, see 32Jxx)	14K99	None of the above, but in this section
14J10	Families, moduli, classification: algebraic theory	14Lxx	Algebraic groups (For linear algebraic
	-		groups, see 20Gxx; for Lie algebras, see
14J15	Moduli, classification: analytic theory;		17B45)
14J15	Moduli, classification: analytic theory; relations with modular forms	14L05	17B45) Formal groups, <i>p</i> -divisible groups
14J15		14L05	17B45) Formal groups, <i>p</i> -divisible groups [See also 55N22]
14J15 14J17	relations with modular forms		Formal groups, <i>p</i> -divisible groups
	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields	14L10	Formal groups, <i>p</i> -divisible groups [See also 55N22]
14J17	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular	14L10	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra
14J17 14J20	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx]	14L10 14L15 14L17	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35]
14J17 14J20	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular	14L10 14L15 14L17	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra
14J17 14J20 14J25 14J26 14J27	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35)	14L10 14L15 14L17 14L24	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory
14J17 14J20 14J25 14J26 14J27 14J28	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces	14L10 14L15 14L17 14L24	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50]
14J17 14J20 14J25 14J26 14J27	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces	14L10 14L15 14L17 14L24 14L30	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects)
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25]	14L10 14L15 14L17 14L24 14L30 14L35	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30]
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type	14L10 14L15 14L17 14L24 14L30	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds Mirror symmetry	14L10 14L15 14L17 14L24 14L30 14L35 14L40	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30]
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds	14L10 14L15 14L17 14L24 14L30 14L35 14L40	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects)
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32 14J33	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds Mirror symmetry [See also 11G42, 53D37]	14L10 14L15 14L17 14L24 14L30 14L35 14L40 14L99	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects)
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32 14J33	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds Mirror symmetry [See also 11G42, 53D37] 4-folds	14L10 14L15 14L17 14L24 14L30 14L35 14L40 14L99 14Mxx	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects) None of the above, but in this section
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32 14J33 14J35 14J40	relations with modular forms [See also $32G13$] Singularities [See also $14B05$, $14E15$] Arithmetic ground fields [See also $11Dxx$, $11G25$, $11G35$, $14Gxx$] Special surfaces (For Hilbert modular surfaces, see $14G35$) Rational and ruled surfaces Elliptic surfaces $K3$ surfaces and Enriques surfaces Surfaces of general type 3 -folds [See also $32Q25$] Calabi-Yau manifolds Mirror symmetry [See also $11G42$, $53D37$] 4 -folds n -folds $(n > 4)$	14L10 14L15 14L17 14L24 14L30 14L35 14L40 14L99 14Mxx	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects) None of the above, but in this section Special varieties Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal)
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32 14J33 14J35 14J40 14J45 14J50	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces $K3$ surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds Mirror symmetry [See also 11G42, 53D37] 4-folds n -folds (n > 4) Fano varieties Automorphisms of surfaces and higher-dimensional varieties	14L10 14L15 14L17 14L24 14L30 14L35 14L40 14L99 14Mxx 14M05	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects) None of the above, but in this section Special varieties Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal) [See also 13F45, 13H10]
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32 14J33 14J35 14J40 14J45	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces K3 surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds Mirror symmetry [See also 11G42, 53D37] 4-folds n -folds ($n > 4$) Fano varieties Automorphisms of surfaces and higher-dimensional varieties Vector bundles on surfaces and higher-	14L10 14L15 14L17 14L24 14L30 14L35 14L40 14L99 14Mxx 14M05	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects) None of the above, but in this section Special varieties Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal) [See also 13F45, 13H10] Linkage [See also 13C40]
14J17 14J20 14J25 14J26 14J27 14J28 14J29 14J30 14J32 14J33 14J35 14J40 14J45 14J50	relations with modular forms [See also 32G13] Singularities [See also 14B05, 14E15] Arithmetic ground fields [See also 11Dxx, 11G25, 11G35, 14Gxx] Special surfaces (For Hilbert modular surfaces, see 14G35) Rational and ruled surfaces Elliptic surfaces $K3$ surfaces and Enriques surfaces Surfaces of general type 3-folds [See also 32Q25] Calabi-Yau manifolds Mirror symmetry [See also 11G42, 53D37] 4-folds n -folds (n > 4) Fano varieties Automorphisms of surfaces and higher-dimensional varieties	14L10 14L15 14L17 14L24 14L30 14L35 14L40 14L99 14Mxx 14M05	Formal groups, <i>p</i> -divisible groups [See also 55N22] Group varieties Group schemes Affine algebraic groups, hyperalgebra constructions [See also 17B45, 18D35] Geometric invariant theory [See also 13A50] Group actions on varieties or schemes (quotients) [See also 13A50, 14L24] Classical groups (geometric aspects) [See also 20Gxx, 51N30] Other algebraic groups (geometric aspects) None of the above, but in this section Special varieties Varieties defined by ring conditions (factorial, Cohen-Macaulay, seminormal) [See also 13F45, 13H10]

14M12	Determinantal varieties [See also 13C40]	14Q20	Effectivity, complexity
14M15	Grassmannians, Schubert varieties, flag manifolds [See also 32M10, 51M35]	14Q99	None of the above, but in this section
14M17	Homogeneous spaces and generaliza-	14Rxx	Affine geometry
	tions [See also 32M10, 53C30, 57T15]	14R05	Classification of affine varieties
14M20	Rational and unirational varieties	14R10	Affine spaces (automorphisms, embed-
141422	[See also 14E08]		dings, exotic structures, cancellation
	Rationally connected varieties Toric varieties, Newton polyhedra	4.474.5	problem)
1711123	[See also 52B20]		Jacobian problem
14M27	Compactifications;	14R20	Group actions on affine varieties [See also 13A50, 14L30]
	symmetric and spherical varieties	14R25	Affine fibrations [See also 14D06]
14M30	Supervarieties [See also 32C11, 58A50]		None of the above, but in this section
14M99	None of the above, but in this section	1110)	Trone of the above, but in this section
14Nxx	Projective and enumerative geometry	14Txx	Tropical geometry [See also 12K10, 14M25, 14N10, 52B20]
	[See also 51-XX]	14T05	Tropical geometry [See also 12K10,
14N05	Projective techniques [See also 51N35]	11100	14M25, 14N10, 52B20]
14N10	Enumerative problems (combinatorial problems)	14T99	None of the above, but in this section
14N15	Classical problems, Schubert calculus	15-XX	Linear and multilinear algebra
	Configurations and arrangements of lin-		matrix theory
	ear subspaces	15-00	General reference works (handbooks,
14N25	Varieties of low degree	4 - 04	dictionaries, bibliographies, etc.)
	Adjunction problems	15-01	Instructional exposition
14N35	Gromov-Witten invariants, quantum co-	15-02	(textbooks, tutorial papers, etc.)
	homology, Gopakumar-Vafa invariants, Donaldson-Thomas invariants	13-02	Research exposition (monographs, survey articles)
	[See also 53D45]	15-03	Historical (must also be assigned at least
14N99	None of the above, but in this section		one classification number from Section 01)
14Pxx	Real algebraic and real analytic	15-04	Explicit machine computation and pro-
	geometry		grams (not the theory of computation or
14P05	Real algebraic sets	15.06	programming)
	[See also 12D15, 13J30]	15-06	Proceedings, conferences, collections, etc.
14P10	Semialgebraic sets and related spaces		
14P15	Real analytic and semianalytic sets		Basic linear algebra
14P20	[See also 32B20, 32C05] Nash functions and manifolds		Vector spaces, linear dependence, rank Linear transformations, semilinear
141 20	[See also 32C07, 58A07]	13/104	transformations
14P25	Topology of real algebraic varieties	15A06	Linear equations
	None of the above, but in this section	15A09	Matrix inversion, generalized inverses
		15A12	Conditioning of matrices
14Qxx	Computational aspects in algebraic ge-		[See also 65F35]
	ometry [See also 12Y05, 13Pxx, 68W30]	15A15	Determinants, permanents, other special
	Curves	15 A 1 C	matrix functions [See also 19B10, 19B14]
	Surfaces, hypersurfaces	13A10	Matrix exponential and similar func- tions of matrices
14Q15	Higher-dimensional varieties		

15 A 1Q	Figonyalues singular values and eigen	15B52	Random matrices
13A16	Eigenvalues, singular values, and eigenvectors		Hermitian, skew-Hermitian, and related
15A21	Canonical forms, reductions,	13037	matrices
	classification	15B99	None of the above, but in this section
	Matrix pencils [See also 47A56]		Associative rings and algebras
	Factorization of matrices	10-77	(For the commutative case, see
	Matrix equations and identities		13-XX)
15A27	Commutativity	16.00	<u> </u>
	Inverse problems	16-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
15A30	Algebraic systems of matrices [See also 16S50, 20Gxx, 20Hxx]	16-01	Instructional exposition (textbooks, tutorial papers, etc.)
15A33	Matrices over special rings (quaternions, finite fields, etc.)	16-02	Research exposition (monographs, survey articles)
15A39	Linear inequalities	16 02	
15A42	Inequalities involving eigenvalues and eigenvectors	16-03	Historical (must also be assigned at least one classification number from Section 01)
	Miscellaneous inequalities involving matrices	16-04	Explicit machine computation and programs (not the theory of computation or
15A54	Matrices over function rings in one or more variables		programming)
15A60	Norms of matrices, numerical range, ap-	16-06	Proceedings, conferences, collections,
	plications of functional analysis to ma-		etc.
	trix theory [See also 65F35, 65J05]	16Bxx	General and miscellaneous
15A63	Quadratic and bilinear forms, inner products [See mainly 11Exx]	16B50	Category-theoretic methods and results (except as in 16D90) [See also 18-XX]
15A66	Clifford algebras, spinors	16B70	Applications of logic [See also 03Cxx]
15A69	Multilinear algebra, tensor products	16B99	None of the above, but in this section
15A72	Vector and tensor algebra, theory of in-		
	variants [See also 13A50, 14L24]		Modules, bimodules and ideals
	Exterior algebra, Grassmann algebras		General module theory
	Other algebras built from modules	16D20	Bimodules
	Max-plus and related algebras	16D25	Ideals
	Matrix completion problems	16D30	Infinite-dimensional simple rings
	Linear preserver problems		(except as in 16Kxx)
15A99	Miscellaneous topics		Free, projective, and flat modules and ideals [See also 19A13]
15Bxx	Special matrices	16D50	Injective modules, self-injective rings
15B05	Toeplitz, Cauchy, and related matrices	1(D(0	[See also 16L60]
15B10	Orthogonal matrices	16D60	Simple and semisimple modules, primitive rings and ideals
15B15	Fuzzy matrices	16D70	tive rings and ideals
15B33	Matrices over special rings (quaternions, finite fields, etc.)	16D70	Structure and classification (except as in 16Gxx), direct sum decomposition, cancellation
15B34	Boolean and Hadamard matrices	16D80	Other classes of modules and ideals
15B35	Sign pattern matrices		[See also 16G50]
15B36	Matrices of integers [See also 11C20]	16D90	Module categories [See also 16Gxx,
15B48	Positive matrices and their generalizations; cones of matrices		16S90]; module theory in a category- theoretic context; Morita equivalence
15B51	Stochastic matrices		and duality

algebras

16H20 Lattices over orders

16D99	None of the above, but in this section	16H99	None of the above, but in this section
16Exx	Homological methods (For commutative rings, see 13Dxx; for general cat-		Division rings and semisimple Artin rings [See also 12E15, 15A30]
14505	egories, see 18Gxx)	16K20	Finite-dimensional
	Syzygies, resolutions, complexes	161/40	(For crossed products, see 16S35)
	Homological dimension		Infinite-dimensional and general
16E20	[See also 18F30, 19Axx, 19D50]		Brauer groups [See also 12G05, 14F22] None of the above, but in this section
16E30	Homological functors on modules (Tor, Ext, etc.)	16J vv	Local rings and generalizations
16E35	Derived categories		Noncommutative local and semilocal
16E40	(Co)homology of rings and algebras (e.g. Hochschild, cyclic, dihedral, etc.)		rings, perfect rings
16F45	Differential graded algebras and appli-		Quasi-Frobenius rings [See also 16D50]
	cations	16L99	None of the above, but in this section
16E50	von Neumann regular rings and generalizations	16Nxx	Radicals and radical properties of rings
16E60	Semihereditary and hereditary rings,		Jacobson radical, quasimultiplication
	free ideal rings, Sylvester rings, etc.		Nil and nilpotent radicals, sets, ideals,
16E65	Homological conditions on rings (gener-		rings
	alizations of regular, Gorenstein, Cohen-	16N60	Prime and semiprime rings
17500	Macaulay rings, etc.)	1 () 100	[See also 16D60, 16U10]
16E99	None of the above, but in this section	16180	General radicals and rings (For radicals in module categories, see 16S90)
16Gxx	Representation theory of rings and algebras	16N99	None of the above, but in this section
16G10	Representations of Artinian rings	16Pxx	Chain conditions, growth conditions,
16G20	Representations of quivers and partially ordered sets	16P10	and other forms of finiteness Finite rings and finite-dimensional al-
16G30	Representations of orders, lattices, alge-	101 10	gebras (For semisimple, see 16K20; for
10000	bras over commutative rings		commutative, see 11Txx, 13Mxx)
	[See also 16Hxx]	16P20	Artinian rings and modules
16G50	Cohen-Macaulay modules	16P40	•
16G60	Representation type (finite, tame, wild, etc.)		Localization and Noetherian rings [See also 16U20]
16G70	Auslander-Reiten sequences (almost split sequences) and Auslander-Reiten quivers	16P60	Chain conditions on annihilators and summands: Goldie-type conditions [See also 16U20], Krull dimension
16G99	None of the above, but in this section	16P70	Chain conditions on other classes of submodules, ideals, subrings, etc.; coher-
16Hyy	Algebras and orders (For arithmetic as-		ence
1011//	pects, see 11R52, 11R54, 11S45; for rep-	16P90	Growth rate, Gelfand-Kirillov dimension
16H05	resentation theory, see 16G30) Separable algebras (e.g., quaternion al-	16P99	None of the above, but in this section
101100	gebras, Azumaya algebras, etc.)		
16H10	Orders in separable algebras	16Rxx	Rings with polynomial identity
	Commutative orders	16R10	T-ideals, identities, varieties of rings and

16R20	Semiprime p.i. rings, rings embeddable in matrices over commutative rings	16Txx	Hopf algebras, quantum groups and re- lated topics
16R30	Trace rings and invariant theory	16T05	Hopf algebras and their applications
	Identities other than those of matrices		[See also 16S40, 57T05]
4 (7) = 0	over commutative rings	16T10	Bialgebras
16R50	Other kinds of identities (generalized	16T15	Coalgebras and comodules; corings
16R60	polynomial, rational, involution) Functional identities	16T20	Ring-theoretic aspects of quantum groups [See also 17B37, 20G42, 81R50]
16R99	None of the above, but in this section	16T25	Yang-Baxter equations
			Connections with combinatorics
16Sxx	Rings and algebras arising under various constructions		None of the above, but in this section
16810			
16S10	Rings determined by universal properties (free algebras, coproducts, adjunc-	16Uxx	Conditions on elements
	tion of inverses, etc.)	16U10	Integral domains
16S15	Finite generation, finite presentability,	16U20	Ore rings, multiplicative sets, Ore localization
	normal forms (diamond lemma, term-	16U30	Divisibility, noncommutative UFDs
16620	rewriting)		Units, groups of units
16S20	Centralizing and normalizing extensions		Center, normalizer (invariant elements)
16S30	Universal enveloping algebras of Lie al-		Generalizations of commutativity
	gebras [See mainly 17B35]		None of the above, but in this section
16S32	Rings of differential operators		,
	[See also 13N10, 32C38]	16Wxx	Rings and algebras with additional
16S34	Group rings [See also 20C05, 20C07],		structure
	Laurent polynomial rings	16W10	Rings with involution; Lie, Jordan and
16S35	Twisted and skew group rings, crossed products		other nonassociative structures [See also 17B60, 17C50, 46Kxx]
16S36	Ordinary and skew polynomial rings	16W20	Automorphisms and endomorphisms
	and semigroup rings [See also 20M25]		Actions of groups and semigroups;
16S37	Quadratic and Koszul algebras	4 (1110=	invariant theory
16S38	Rings arising from non-commutative al-		Derivations, actions of Lie algebras
	gebraic geometry [See also 14A22]		Graded rings and modules
16S40	Smash products of general Hopf actions [See also 16T05]	16W55	"Super" (or "skew") structure [See also 17A70, 17Bxx, 17C70] (For exterior alge-
16S50	Endomorphism rings; matrix rings [See also 15-XX]		bras, see 15A75; for Clifford algebras, see 11E88, 15A66)
16S60	Rings of functions, subdirect products, sheaves of rings	16W60	Valuations, completions, formal power series and related constructions
16S70	Extensions of rings by ideals		[See also 13Jxx]
16S80	Deformations of rings [See also 13D10, 14D15]	16W70	Filtered rings; filtrational and graded techniques
16S85	Rings of fractions and localizations	16W80	Topological and ordered rings and mod-
	[See also 13B30]		ules [See also 06F25, 13Jxx]
16S90	Torsion theories; radicals on module categories [See also 13D30, 18E40] (For rad-		None of the above, but in this section
	icals of rings, see 16Nxx)	16Yxx	Generalizations
16500	None of the above but in this section		(For nonassociative rings, see 17-XX)

16Y30 Near-rings [See also 12K05]

16Y60	Semirings [See also 12K10]		
16Y99	None of the above, but in this section	17Bxx	Lie algebras and Lie superalgebras (For Lie groups, see 22Exx)
16Zxx	Computational aspects of	17B01	Identities, free Lie (super)algebras
	associative rings	17B05	Structure theory
16Z05	Computational aspects of	17B08	Coadjoint orbits; nilpotent varieties
16 Z 99	associative rings [See also 68W30] None of the above, but in this section	17B10	Representations, algebraic theory (weights)
17-XX	Nonassociative rings and	17B15	Representations, analytic theory
	algebras	17B20	Simple, semisimple, reductive (super)algebras
17-00	General reference works (handbooks,	17B22	Root systems
17 01	dictionaries, bibliographies, etc.)	17B25	Exceptional (super)algebras
17-01	Instructional exposition (textbooks, tutorial papers, etc.)		Solvable, nilpotent (super)algebras
17-02	Research exposition (monographs, survey articles)	17B35	Universal enveloping (super)algebras [See also 16S30]
17-03	Historical (must also be assigned at least one classification number from Section	17B37	Quantum groups (quantized enveloping algebras) and related deformations [See also 16T20, 20G42, 81R50, 82B23]
17-04	01) Explicit machine computation and pro-	17B40	Automorphisms, derivations, other op-
17-04	grams (not the theory of computation or	1=5.1=	erators
	programming)	17B45	Lie algebras of linear algebraic groups
17-06	Proceedings, conferences, collections,	17B50	[See also 14Lxx and 20Gxx] Modular Lie (super)algebras
	etc.	17B55	Homological methods in
17-08	Computational methods		Lie (super)algebras
17Axx	General nonassociative rings	17B56	Cohomology of Lie (super)algebras
	General theory	17B60	Lie (super)algebras associated with
	Power-associative rings		other structures (associative, Jordan, etc.) [See also 16W10, 17C40, 17C50]
17A15	Noncommutative Jordan algebras	17B62	Lie bialgebras; Lie coalgebras
17A20	Flexible algebras		Poisson algebras
17A30	Algebras satisfying other identities	17B65	Infinite-dimensional Lie (super)algebras
17A32	Leibniz algebras		[See also 22E65]
17A35	Division algebras	17B66	Lie algebras of vector fields and related
17A36	Automorphisms, derivations, other op-		(super) algebras
15 4 40	erators	17B67	Kac-Moody (super)algebras; extended
	Ternary compositions		affine Lie algebras; toroidal Lie algebras
	Other <i>n</i> -ary compositions $(n \ge 3)$	17B68	Virasoro and related algebras
	Quadratic algebras (but not quadratic Jordan algebras)		Vertex operators; vertex operator algebras and related structures
	Free algebras		Graded Lie (super)algebras
	Structure theory		Color Lie (super)algebras
	Radical theory		Applications to integrable systems
17A70	Superalgebras		Applications to physics
17A75	Composition algebras	17B99	None of the above, but in this section
17A80	Valued algebras		
17A99	None of the above, but in this section		

17Cxx	Jordan algebras (algebras, triples and pairs)	18-04	grams (not the theory of computation or
17C05	Identities and free Jordan structures	10.06	programming)
17C10	Structure theory	18-06	Proceedings, conferences, collections, etc.
17C17	Radicals		
17C20	Simple, semisimple algebras	18Axx	General theory of categories and functors
17C27	Idempotents, Peirce decompositions	18405	Definitions, generalizations
17C30	Associated groups, automorphisms		Graphs, diagram schemes, precategories
17C36	Associated manifolds	107110	[See especially 20L05]
17C37	Associated geometries	18A15	Foundations, relations to logic and de-
17C40	Exceptional Jordan structures		ductive systems [See also 03-XX]
17C50	Jordan structures associated with other structures [See also 16W10]	18A20	Epimorphisms, monomorphisms, spe cial classes of morphisms, null mor
17C55	Finite-dimensional structures		phisms
17C60	Division algebras	18A22	Special properties of functors (faithful
17C65	Jordan structures on Banach spaces and		full, etc.)
	algebras [See also 46H70, 46L70]	18A23	Natural morphisms, dinatural mor
	Super structures		phisms
	Applications to physics		Functor categories, comma categories
17C99	None of the above, but in this section	18A30	Limits and colimits (products, sums, di- rected limits, pushouts, fiber products
17Dxx	Other nonassociative rings and algebras		equalizers, kernels, ends and coends etc.)
17D05	Alternative rings	18A32	Factorization of morphisms, substruc-
17D10	Mal'cev (Mal'tsev) rings and		tures, quotient structures, congruences amalgams
	algebras	18Δ35	Categories admitting limits (complete
	Right alternative rings	10/13/3	categories), functors preserving limits
	(γ, δ) -rings, including $(1, -1)$ -rings		completions
	Lie-admissible algebras	18A40	Adjoint functors (universal construc-
	Genetic algebras		tions, reflective subcategories, Kan ex-
17D99	None of the above, but in this section		tensions, etc.)
18-XX	Category theory; homological al-	18A99	None of the above, but in this section
	gebra (For commutative rings		
	see 13Dxx, for associative rings		Special categories
	16Exx, for groups 20Jxx, for topo-	18B05	Category of sets, characterizations
	logical groups and related structures 57Txx; see also 55Nxx and	10D10	[See also 03-XX]
	55Uxx for algebraic topology)		Category of relations, additive relations
18-00	General reference works (handbooks,	18B15	Embedding theorems, universal categories [See also 18E20]
10 00	dictionaries, bibliographies, etc.)	18B20	Categories of machines, automata, oper-
18-01	Instructional exposition	10220	ative categories [See also 03D05, 68Qxx]
	(textbooks, tutorial papers, etc.)	18B25	Topoi [See also 03G30]
18-02	Research exposition (monographs, survey articles)	18B30	Categories of topological spaces and continuous mappings [See also 54-XX]
18-03	Historical (must also be assigned at least one classification number from Section 01)	18B35	Preorders, orders and lattices (viewed as categories) [See also 06-XX]

18E25 Derived functors and satellites

18B40	Groupoids, semigroupoids, semigroups, groups (viewed as categories)		Derived categories, triangulated categories
10000	[See also 20Axx, 20L05, 20Mxx]	18E35	Localization of categories
10099	None of the above, but in this section	18E40	Torsion theories, radicals [See also 13D30, 16S90]
18Cxx	Categories and theories	18E99	None of the above, but in this section
	Equational categories	102,	Trone of the above, but in this section
	[See also 03C05, 08C05]	18Fxx	Categories and geometry
18C10	Theories (e.g. algebraic theories), struc-	18F05	Local categories and functors
	ture, and semantics [See also 03G30]	18F10	Grothendieck topologies
18C15	Triples (= standard construction, monad		[See also 14F20]
	or triad), algebras for a triple, homology and derived functors for triples	18F15	Abstract manifolds and fiber bundles [See also 55Rxx, 57Pxx]
10 C2 0	[See also 18Gxx]	18F20	Presheaves and sheaves [See also 14F05,
18C20	Algebras and Kleisli categories associated with monads		32C35, 32L10, 54B40, 55N30]
18C30	Sketches and generalizations	18F25	Algebraic K-theory and L-theory [See
	Accessible and locally presentable categories		also 11Exx, 11R70, 11S70, 12-XX, 13D15, 14Cxx, 16E20, 19-XX, 46L80, 57R65,
18/250	Categorical semantics of formal lan-	40500	57R67]
	guages [See also 68Q55, 68Q65]	18F30	Grothendieck groups [See also 13D15, 16E20, 19Axx]
18C99	None of the above, but in this section	18F99	None of the above, but in this section
18Dxx	Categories with structure	18Gxx	Homological algebra [See also 13Dxx
	Double categories, 2-categories, bicate-	18Gxx	Homological algebra [See also 13Dxx, 16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx]
18D05	Double categories, 2-categories, bicategories and generalizations		16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also
18D05	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative	18G05	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50]
18D05	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories	18G05	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors
18D05	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories	18G05 18G10	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25]
18D05 18D10	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23]	18G05 18G10	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth
18D05 18D10	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and	18G05 18G10 18G15	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25]
18D05 18D10 18D15	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.)	18G05 18G10 18G15	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension
18D05 18D10 18D15	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and	18G05 18G10 18G15 18G20	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10]
18D05 18D10 18D15 18D20	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or	18G05 18G10 18G15 18G20 18G25	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes
18D05 18D10 18D15 18D20 18D25	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories)	18G05 18G10 18G15 18G20 18G25	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a
18D05 18D10 18D15 18D20 18D25 18D30	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions	18G05 18G10 18G15 18G20 18G25 18G30	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10]
18D05 18D10 18D15 18D20 18D25 18D30	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories	18G05 18G10 18G15 18G20 18G25 18G30	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15]
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.) Operads [See also 55P48]	18G05 18G10 18G15 18G20 18G25 18G30	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.)	18G05 18G10 18G15 18G20 18G25 18G30 18G35 18G40	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology [See also 55Txx]
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50 18D99	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.) Operads [See also 55P48] None of the above, but in this section	18G05 18G10 18G15 18G20 18G25 18G30 18G35 18G40 18G50	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50 18D99 18Exx	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.) Operads [See also 55P48] None of the above, but in this section	18G05 18G10 18G15 18G20 18G25 18G30 18G35 18G40 18G50 18G55	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology [See also 55Txx] Nonabelian homological algebra
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50 18D99 18Exx 18E05	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.) Operads [See also 55P48] None of the above, but in this section Abelian categories Preadditive, additive categories	18G05 18G10 18G15 18G20 18G25 18G30 18G35 18G40 18G50 18G55	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology [See also 55Txx] Nonabelian homological algebra Homotopical algebra
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50 18D99 18Exx 18E05 18E10	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.) Operads [See also 55P48] None of the above, but in this section Abelian categories Preadditive, additive categories Exact categories, abelian categories	18G05 18G10 18G15 18G20 18G25 18G30 18G35 18G40 18G50 18G55 18G60	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology [See also 55Txx] Nonabelian homological algebra Homotopical algebra Other (co)homology theories
18D05 18D10 18D15 18D20 18D25 18D30 18D35 18D50 18D99 18Exx 18E05 18E10	Double categories, 2-categories, bicategories and generalizations Monoidal categories (= multiplicative categories), symmetric monoidal categories, braided categories [See also 19D23] Closed categories (closed monoidal and Cartesian closed categories, etc.) Enriched categories (over closed or monoidal categories) Strong functors, strong adjunctions Fibered categories Structured objects in a category (group objects, etc.) Operads [See also 55P48] None of the above, but in this section Abelian categories Preadditive, additive categories	18G05 18G10 18G15 18G20 18G25 18G30 18G35 18G40 18G50 18G55 18G60	16Exx, 20Jxx, 55Nxx, 55Uxx, 57Txx] Projectives and injectives [See also 13C10, 13C11, 16D40, 16D50] Resolutions; derived functors [See also 13D02, 16E05, 18E25] Ext and Tor, generalizations, Künneth formula [See also 55U25] Homological dimension [See also 13D05, 16E10] Relative homological algebra, projective classes Simplicial sets, simplicial objects (in a category) [See also 55U10] Chain complexes [See also 18E30, 55U15] Spectral sequences, hypercohomology [See also 55Txx] Nonabelian homological algebra Homotopical algebra Other (co)homology theories [See also 19D55, 46L80, 58J20, 58J22]

26 K-theory

19-XX	(K-theory [See also 16E20, 18F25]	19D23	Symmetric monoidal categories [See also 18D10]
19-00	General reference works (handbooks,	19D25	Karoubi-Villamayor-Gersten K-theory
	dictionaries, bibliographies, etc.)		Negative <i>K</i> -theory, NK and Nil
19-01	Instructional exposition		Higher symbols, Milnor K-theory
	(textbooks, tutorial papers, etc.)		Computations of higher <i>K</i> -theory of
19-02	Research exposition (monographs, survey articles)		rings [See also 13D15, 16E20]
19-03	Historical (must also be assigned at least	19D55	K-theory and homology; cyclic homol-
17 03	one classification number from Section		ogy and cohomology [See also 18G60]
	01)	19D99	None of the above, but in this section
19-04	Explicit machine computation and pro-		
	grams (not the theory of computation or		K-theory in geometry
	programming)		<i>K</i> -theory of schemes [See also 14C35]
19-06	Proceedings, conferences, collections, etc.	19E15	Algebraic cycles and motivic cohomology [See also 14C25, 14C35]
10.4		19F20	Relations with cohomology theories
19AXX	Grothendieck groups and K ₀ [See also 13D15, 18F30]	17220	[See also 14Fxx]
19A13	Stability for projective modules	19E99	None of the above, but in this section
	[See also 13C10]		
19A15	Efficient generation	19Fxx	K-theory in number theory
19A22	Frobenius induction, Burnside and rep-		[See also 11R70, 11S70]
	resentation rings	19F05	Generalized class field theory
19A31	K_0 of group rings and orders	10515	[See also 11G45]
	K_0 of other rings		Symbols and arithmetic [See also 11R37]
19A99	None of the above, but in this section	19F27	Étale cohomology, higher regulators, zeta and <i>L</i> -functions [See also 11G40,
			11R42, 11S40, 14F20, 14G10]
	Whitehead groups and K_1	19F99	None of the above, but in this section
19B10	Stable range conditions		*
	Stability for linear groups	19Gxx	K-theory of forms [See also 11Exx]
19828	K_1 of group rings and orders [See also 57Q10]		Stability for quadratic modules
19B37	Congruence subgroup problems		Witt groups of rings [See also 11E81]
17007	[See also 20H05]		L-theory of group rings [See also 11E81]
19B99	None of the above, but in this section	19G38	Hermitian <i>K</i> -theory, relations with
			K-theory of rings
19Cxx	Steinberg groups and K ₂	19G99	None of the above, but in this section
19C09	Central extensions and Schur multipli-		
10000	ers	19Jxx	Obstructions from topology
19C20	Symbols, presentations and	19J05	Finiteness and other obstructions in K_0
10020	stability of K_2	19J10	Whitehead (and related) torsion
	K ₂ and the Brauer group	19J25	Surgery obstructions [See also 57R67]
	Excision for K_2	19J35	Obstructions to group actions
17し77	None of the above, but in this section	19J99	None of the above, but in this section
19Dxx	Higher algebraic <i>K</i> -theory	19Kxx	K-theory and operator algebras
	<i>Q</i> - and plus-constructions		[See mainly 46L80, and also 46M20]
19D10	Algebraic <i>K</i> -theory of spaces	19K14	K₀ as an ordered group, traces

	EXT and K-homology [See also 55N22]	20Bxx	Permutation groups
19K35	Kasparov theory (KK-theory)	20B05	General theory for finite groups
10VE6	[See also 58J22]	20B07	General theory for infinite groups
	Index theory [See also 58J20, 58J22]	20B10	Characterization theorems
19 N 99	None of the above, but in this section	20B15	Primitive groups
10T	Tanalastal V the same	20B20	Multiply transitive finite groups
19LXX	Topological <i>K</i> -theory [See also 55N15, 55R50, 55S25]	20B22	Multiply transitive infinite groups
191 10	Riemann-Roch theorems,	20B25	Finite automorphism groups of alge-
17110	Chern characters		braic, geometric, or combinatorial struc-
19L20	<i>J</i> -homomorphism, Adams operations [See also 55Q50]		tures [See also 05Bxx, 12F10, 20G40 20H30, 51-XX]
19L41	Connective <i>K</i> -theory, cobordism [See also 55N22]	20B27	Infinite automorphism groups [See also 12F10]
19L47	Equivariant K-theory [See also 55N91,	20B30	Symmetric groups
	55P91, 55Q91, 55R91, 55S91]		Subgroups of symmetric groups
19L50	Twisted <i>K</i> -theory; differential <i>K</i> -theory		Computational methods
19L64	Computations, geometric applications	20B99	None of the above, but in this section
19L99	None of the above, but in this section		
		20Cxx	Representation theory of groups
19Mxx	Miscellaneous applications of <i>K</i> -theory		[See also 19A22 (for representation
19M05	Miscellaneous applications of <i>K</i> -theory	20C05	rings and Burnside rings)] Group rings of finite groups and their
19M99	None of the above, but in this section	20003	modules [See also 16S34]
20-XX	Group theory and	20C07	Group rings of infinite groups and their
	generalizations	2000	modules [See also 16S34]
20-00	General reference works (handbooks,		Hecke algebras and their representations
	dictionaries, bibliographies, etc.)		Integral representations of finite groups
20-01	Instructional exposition		<i>p</i> -adic representations of finite groups
20.02	(textbooks, tutorial papers, etc.)	20C12	Integral representations of infinite
20-02	Research exposition (monographs, survey articles)	20015	groups Ordinary representations and characters
20.02			• •
20-03	Historical (must also be assigned at least one classification number from Section		Modular representations and characters Projective representations and multipli-
	01)	20023	ers
20-04	Explicit machine computation and pro-	20C30	Representations of finite symmetric
	grams (not the theory of computation or		groups
	programming)	20C32	Representations of infinite symmetric
20-06	Proceedings, conferences, collections,		groups
	etc.	20C33	Representations of finite groups of Lie
20Axx	Foundations		type
20A05	Axiomatics and elementary properties	20C34	Representations of sporadic groups
20A10	Metamathematical considerations (For word problems, see 20F10)	20C35	Applications of group representations to physics
20A15	Applications of logic to group theory	20C40	Computational methods
	None of the above, but in this section	20C99	None of the above, but in this section

20Dxx	Abstract finite groups	20E99	None of the above, but in this section
20D05	Finite simple groups and their classifica-		
20000	tion	20Fxx	Special aspects of infinite or finite
20D06	Simple groups: alternating groups and groups of Lie type [See also 20Gxx]	20F05	groups Generators, relations, and presentations
201708	Simple groups: sporadic groups		Cancellation theory; application of van
	Solvable groups, theory of formations,		Kampen diagrams [See also 57M05]
20010	Schunck classes, Fitting classes, π -length, ranks [See also 20F17]	20F10	Word problems, other decision prob- lems, connections with logic and au-
20D15	Nilpotent groups, <i>p</i> -groups		tomata [See also 03B25, 03D05, 03D40,
	Sylow subgroups, Sylow properties, π -groups, π -structure	20F11	06B25, 08A50, 68Q70] Groups of finite Morley rank
20D25	Special subgroups (Frattini, Fitting, etc.)	20E42	[See also 03C45, 03C60]
	Series and lattices of subgroups		Commutator calculus
	Subnormal subgroups	20F14	Derived series, central series, and generalizations
20D40	Products of subgroups	20F16	Solvable groups, supersolvable groups
20D45	Automorphisms		[See also 20D10]
	Arithmetic and combinatorial problems None of the above, but in this section	20F17	Formations of groups, Fitting classes [See also 20D10]
		20F18	Nilpotent groups [See also 20D15]
20Exx	Structure and classification of infinite or finite groups	20F19	Generalizations of solvable and nilpotent groups
20E05	Free nonabelian groups	20F22	Other classes of groups defined by sub-
20E06	Free products, free products with		group chains
	amalgamation, Higman-Neumann-		FC-groups and their generalizations
•••	Neumann extensions, and generalizations	20F28	Automorphism groups of groups [See also 20E36]
20E07	Subgroup theorems; subgroup growth	20F29	Representations of groups as automor-
	Groups acting on trees [See also 20F65]		phism groups of algebraic systems
20E10 20E15	Chains and lattices of subgroups, sub-	20F34	Fundamental groups and their automorphisms [See also 57M05, 57Sxx]
	normal subgroups [See also 20F22]	20F36	Braid groups; Artin groups
	Limits, profinite groups	20F38	Other groups related to topology or anal-
20E22	Extensions, wreath products, and other		ysis
OUESE	compositions [See also 20J05]		Associated Lie structures
	Local properties		Engel conditions
20E26	Residual properties and generalizations; residually finite groups	20F50	Periodic groups; locally finite groups
20E28	Maximal subgroups	20F55	Reflection and Coxeter groups [See also 22E40, 51F15]
	Simple groups [See also 20D05]	20F60	Ordered groups [See mainly 06F15]
	General structure theorems	20F65	Geometric group theory
20E36	Automorphisms of infinite groups		[See also 05C25, 20E08, 57Mxx]
	[For automorphisms of finite groups, see 20D45]	20F67	Hyperbolic groups and nonpositively curved groups
20E42	Groups with a BN-pair; buildings	20F69	Asymptotic properties of groups
	[See also 51E24]	20F70	Algebraic geometry over groups;
20E45	Conjugacy classes		equations over groups

20F99 None of the above, but in this section

20Gxx	Linear algebraic groups and related topics (For arithmetic theory, see 11E57,		
	11H56; for geometric theory, see 14Lxx,		
	22Exx; for other methods in represen-		
	tation theory, see 15A30, 22E45, 22E46,		
2000	22E47, 22E50, 22E55)		
	Representation theory		
	Structure theory		
20G10	Cohomology theory		
20G15	Linear algebraic groups over arbitrary		
	fields		
20G20	Linear algebraic groups over the reals, the complexes, the quaternions		
20G25	Linear algebraic groups over local fields and their integers		
20G30	Linear algebraic groups over global fields and their integers		
20G35	Linear algebraic groups over adèles and other rings and schemes		
20G40	Linear algebraic groups over finite fields		
20G41	Exceptional groups		
	Quantum groups (quantized function algebras) and their representations [See also 16T20, 17B37, 81R50]		

20Hxx Other groups of matrices [See also 15A30]

20G43 Schur and *q*-Schur algebras

20G44 Kac-Moody groups

20G45 Applications to physics

20H05 Unimodular groups, congruence subgroups [See also 11F06, 19B37, 22E40, 51F20]

20G99 None of the above, but in this section

20H10 Fuchsian groups and their generalizations [See also 11F06, 22E40, 30F35, 32Nxx]

20H15 Other geometric groups, including crystallographic groups [See also 51-XX, especially 51F15, and 82D25]

20H20 Other matrix groups over fields

20H25 Other matrix groups over rings

20H30 Other matrix groups over finite fields

20H99 None of the above, but in this section

20Jxx	Connections with homological algebra
	and category theory
20J05	Homological methods in group theory
20J06	Cohomology of groups
20J15	Category of groups
20J99	None of the above, but in this section

20Kxx Abelian groups

20K01 Finite abelian groups
[For sumsets, see 11B13 and 11P70]

20K10 Torsion groups, primary groups and generalized primary groups

20K15 Torsion-free groups, finite rank

20K20 Torsion-free groups, infinite rank

20K21 Mixed groups

20K25 Direct sums, direct products, etc.

20K27 Subgroups

20K30 Automorphisms, homomorphisms, endomorphisms, etc.

20K35 Extensions

20K40 Homological and categorical methods

20K45 Topological methods [See also 22A05, 22B05]

20K99 None of the above, but in this section

20Lxx Groupoids (i.e. small categories in which all morphisms are isomorphisms) (For sets with a single binary operation, see 20N02; for topological groupoids, see 22A22, 58H05)

20L05 Groupoids (i.e. small categories in which all morphisms are isomorphisms) (For sets with a single binary operation, see 20N02; for topological groupoids, see 22A22, 58H05)

20L99 None of the above, but in this section

20Mxx Semigroups

20M05 Free semigroups, generators and relations, word problems

20M07 Varieties and pseudovarieties of semigroups

20M10 General structure theory

20M11 Radical theory

20M12 Ideal theory

20M13 Arithmetic theory of monoids

20M14 Commutative semigroups

	Mappings of semigroups	22-04	Explicit machine computation and pro-
	Regular semigroups		grams (not the theory of computation or
	Inverse semigroups	22.06	programming)
	Orthodox semigroups	22-06	Proceedings, conferences, collections, etc.
20M20	Semigroups of transformations, etc. [See also 47D03, 47H20, 54H15]	22Axx	Topological and differentiable alge-
20M25	Semigroup rings, multiplicative semi- groups of rings [See also 16S36, 16Y60]		braic systems (For topological rings and fields, see 12Jxx, 13Jxx, 16W80)
20M30	Representation of semigroups; actions of	22A05	Structure of general topological groups
	semigroups on sets	22A10	Analysis on general topological groups
20M32	Algebraic monoids	22A15	Structure of topological semigroups
	Semigroups in automata theory, linguis-	22A20	Analysis on topological semigroups
	tics, etc. [See also 03D05, 68Q70, 68T50]	22A22	Topological groupoids (including differ-
20M50	Connections of semigroups with homological algebra and category theory		entiable and Lie groupoids) [See also 58H05]
20M99	None of the above, but in this section	22A25	Representations of general topological
			groups and semigroups
	Other generalizations of groups Sets with a single binary operation	22A26	Topological semilattices, lattices and applications [See also 06B30, 06B35, 06F30]
	(groupoids)	22A30	Other topological algebraic systems and their representations
	Loops, quasigroups [See also 05Bxx]	22A99	None of the above, but in this section
20N10	Ternary systems		Trone of the above, but in this section
203 14 5	(heaps, semiheaps, heapoids, etc.)	22Rvv	Locally compact abelian groups
	n -ary systems ($n \ge 3$)	ZZDXX	(LCA groups)
	Hypergroups	22B05	General properties and structure of LCA
	Fuzzy groups [See also 03E72]		groups
201199	None of the above, but in this section	22B10	Structure of group algebras of LCA groups
20Pxx	Probabilistic methods in group theory [See also 60Bxx]	22B99	None of the above, but in this section
20P05	Probabilistic methods in group theory	226	
	[See also 60Bxx]		Compact groups
20P99	None of the above, but in this section		Compact groups
22-XX	Topological groups, Lie groups	22C99	None of the above, but in this section
	(For transformation groups, see	22D	T 11
	54H15, 57Sxx, 58-XX.	22DXX	Locally compact groups and their algebras
	For abstract harmonic analysis,	22D05	General properties and structure of lo-
	see 43-XX)	22003	cally compact groups
22-00	General reference works (handbooks,	22D10	Unitary representations of locally com-
	dictionaries, bibliographies, etc.)	22010	pact groups
22-01	Instructional exposition	22D12	Other representations of locally compact
	(textbooks, tutorial papers, etc.)		groups
22-02	Research exposition (monographs, survey articles)	22D15	Group algebras of locally compact groups
22-03	Historical (must also be assigned at least	22D20	Representations of group algebras
	one classification number from Section		C*-algebras and W*-algebras in relation
	01)		to group representations [See also 46Lxx]

Real functions 31

	Induced representations Duality theorems	22E57	Geometric Langlands programs representation-theoretic aspects
	Ergodic theory on groups [See also 28Dxx]	22E60	[See also 14D24] Lie algebras of Lie groups (For the alge-
	Automorphism groups of locally compact groups	22E65	braic theory of Lie algebras, see 17Bxx) Infinite-dimensional Lie groups and
22D99	None of the above, but in this section	225((their Lie algebras: general properties [See also 17B65, 58B25, 58H05]
22Exx	Lie groups (For the topology of Lie groups and homogeneous spaces, see 57Sxx, 57Txx; for analysis thereon, see 43A80, 43A85, 43A90)	22E66	Analysis on and representations of infinite-dimensional Lie groups
•••		22E67	Loop groups and related constructions, group-theoretic treatment [See also 58D05]
	Local Lie groups [See also 34-XX, 35-XX, 58H05]	22E70	Applications of Lie groups to physics, explicit representations [See also 81R05,
22E10	General properties and structure of complex Lie groups [See also 32M05]	22E99	81R10] None of the above, but in this section
22E15	General properties and structure of real Lie groups		Non-comment branchouse the array of
22E20	General properties and structure of other Lie groups	22F05	Noncompact transformation groups General theory of group and pseudogroup actions (For topological prop-
22E25	Nilpotent and solvable Lie groups		erties of spaces with an action, see 57S20)
22E27	Representations of nilpotent and solvable Lie groups (special orbital integrals, non-type I representations, etc.)	22F10	Measurable group actions [See also 22D40, 28Dxx, 37Axx]
22E30	Analysis on real and complex Lie groups [See also 33C80, 43-XX]	22F30	Homogeneous spaces (For general actions on manifolds or preserving geo-
22E35	Analysis on <i>p</i> -adic Lie groups		metrical structures, see 57M60, 57Sxx,
22E40	Discrete subgroups of Lie groups [See also 20Hxx, 32Nxx]	•••	for discrete subgroups of Lie groups, see especially 22E40)
22E41	Continuous cohomology [See also 57R32, 57Txx, 58H10]	22F50	Groups as automorphisms of other structures
22E43	Structure and representation of the	22F99	None of the above, but in this section
22 210	Lorentz group		(Real functions [See also 54C30]
22E45	Representations of Lie and linear algebraic groups over real fields: analytic methods (For the purely algebraic the-	26-00 26-01	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition
	ory, see 20G05)		(textbooks, tutorial papers, etc.)
22E46	Semisimple Lie groups and their representations	26-02	Research exposition (monographs, survey articles)
22E47	Representations of Lie and real algebraic groups: algebraic methods (Verma modules, etc.) [See also 17B10]	26-03	Historical (must also be assigned at least one classification number from Section 01)
22E50	Representations of Lie and linear algebraic groups over local fields [See also 20G05]	26-04	Explicit machine computation and programs (not the theory of computation or programming)
22E55	Representations of Lie and linear algebraic groups over global fields and adèle rings [See also 20G05]	26-06	Proceedings, conferences, collections, etc.

Real functions

26Axx	Functions of one variable	26B20	Integral formulas (Stokes, Gauss, Green, etc.)
26A03	Foundations: limits and generalizations,	26B25	Convexity, generalizations
• • • • • •	elementary topology of the line	26B30	Absolutely continuous functions, func-
	One-variable calculus	20200	tions of bounded variation
	Elementary functions	26B35	Special properties of functions of several
26A12	Rate of growth of functions, orders of in-		variables, Hölder conditions, etc.
	finity, slowly varying functions [See also 26A48]	26B40	Representation and superposition of functions
26A15	Continuity and related questions (modulus of continuity, semicontinuity, dis-	26B99	None of the above, but in this section
	continuities, etc.) (For properties deter-	26Cxx	Polynomials, rational functions
	mined by Fourier coefficients, see 42A16;		Polynomials: analytic properties, etc.
	for those determined by approximation properties, see 41A25, 41A27)		[See also 12Dxx, 12Exx]
26A16	Lipschitz (Hölder) classes	26C10	Polynomials: location of zeros
	Iteration [See also 37Bxx, 37Cxx, 37Exx,		[See also 12D10, 30C15, 65H05]
201110	39B12, 47H10, 54H25]		Rational functions [See also 14Pxx]
26A21	Classification of real functions; Baire classification of sets and functions	26C99	None of the above, but in this section
	[See also 03E15, 28A05, 54C50]	26Dxx	Inequalities (For maximal function in-
26A24	Differentiation (functions of one vari-		equalities, see 42B25; for functional in-
	able): general theory, generalized deriva-		equalities, see 39B72; for probabilistic
	tives, mean-value theorems	2600	inequalities, see 60E15)
26A27	[See also 28A15] Nondifferentiability (nondifferentiable	26D05	Inequalities for trigonometric functions and polynomials
	functions, points of nondifferentiability), discontinuous derivatives	26D07	Inequalities involving other types of functions
26A30	Singular functions, Cantor functions, functions with other special properties	26D10	Inequalities involving derivatives and differential and integral operators
26A33	Fractional derivatives and integrals	26D15	Inequalities for sums, series and inte-
	Antidifferentiation		grals
	Denjoy and Perron integrals, other spe-	26D20	Other analytical inequalities
	cial integrals	26D99	None of the above, but in this section
26A42	Integrals of Riemann, Stieltjes and		
06 4 45	Lebesgue type [See also 28-XX]		Miscellaneous topics [See also 58Cxx]
26A45	Functions of bounded variation, generalizations	26E05	Real-analytic functions
26A46	Absolutely continuous functions	26F10	[See also 32B05, 32C05] C^{∞} -functions, quasi-analytic functions
	Monotonic functions, generalizations	20E10	[See also 58C25]
	Convexity, generalizations	26E15	Calculus of functions on infinite-
	None of the above, but in this section		dimensional spaces
	, a same and a same		[See also 46G05, 58Cxx]
26Bxx	Functions of several variables	26E20	Calculus of functions taking values in
	Continuity and differentiation questions		infinite-dimensional spaces
	Implicit function theorems, Jacobians,	26.525	[See also 46E40, 46G10, 58Cxx]
	transformations with several variables	26E25	Set-valued functions [See also 28B20, 54C60] (For nonsmooth analysis, see
	Calculus of vector functions		49J52, 58Cxx, 90Cxx)
26B15	Integration: length, area, volume [See also 28A75, 51M25]	26E30	Non-Archimedean analysis [See also 12J25]

Measure and integration 33

26E35	Nonstandard analysis	28A51	Lifting theory [See also 46G15]
26E40	[See also 03H05, 28E05, 54J05]	28A60	Measures on Boolean rings, measure al-
20E40	Constructive real analysis [See also 03F60]	28 4 75	gebras [See also 54H10] Length, area, volume, other geometric
26E50	Fuzzy real analysis	2011/3	measure theory [See also 26B15, 49Q15]
	[See also 03E72, 28E10]	28A78	Hausdorff and packing measures
	Means [See also 47A64]	28A80	Fractals [See also 37Fxx]
26E70	Real analysis on time scales or measure chains (For dynamic equations on time	28A99	None of the above, but in this section
26F99	scales or measure chains see 34N05) None of the above, but in this section	28Bxx	Set functions, measures and integrals
		20205	with values in abstract spaces
28-XX	Measure and integration (For analysis on manifolds,	28B05	Vector-valued set functions, measures and integrals [See also 46G10]
	see 58-XX)	28B10	
28-00	General reference works (handbooks,	28B15	tions, measures and integrals
28-01	dictionaries, bibliographies, etc.) Instructional exposition	28D13	Set functions, measures and integrals with values in ordered spaces
	(textbooks, tutorial papers, etc.)	28B20	Set-valued set functions and measures;
28-02	Research exposition (monographs, survey articles)		integration of set-valued functions; measurable selections [See also 26E25,
28-03	Historical (must also be assigned at least	28B00	54C60, 54C65, 91B14] None of the above, but in this section
	one classification number from Section 01)		None of the above, but in this section
28-04	Explicit machine computation and pro-	28Cxx	Set functions and measures on spaces
	grams (not the theory of computation or programming)		with additional structure [See also 46G12, 58C35, 58D20]
28-06	Proceedings, conferences, collections,	28C05	Integration theory via linear functionals
	etc.		(Radon measures, Daniell integrals, etc.), representing set functions and measures
	Classical measure theory	28C10	Set functions and measures on topolog-
28A05	Classes of sets (Borel fields, σ -rings, etc.), measurable sets, Suslin sets, analytic sets		ical groups or semigroups, Haar mea-
	[See also 03E15, 26A21, 54H05]		sures, invariant measures
28A10	Real- or complex-valued set functions	28C15	[See also 22Axx, 43A05]
28A12	Contents, measures, outer measures, ca-	20013	Set functions and measures on topological spaces (regularity of measures, etc.)
	pacities	28C20	Set functions and measures and integrals
28A15	Abstract differentiation theory, differentiation of set functions [See also 26 A 24]		in infinite-dimensional spaces (Wiener
28A20	tiation of set functions [See also 26A24] Measurable and nonmeasurable func-		measure, Gaussian measure, etc.)
201120	tions, sequences of measurable func-	28(-99	[See also 46G12, 58C35, 58D20, 60B11] None of the above, but in this section
	tions, modes of convergence	200))	Twole of the above, but in this section
28A25	Integration with respect to measures and	28Dxx	Measure-theoretic ergodic theory
28A33	other set functions Spaces of measures, convergence of mea-		[See also 11K50, 11K55, 22D40, 37Axx,
201100	sures [See also 46E27, 60Bxx]	2000	47A35, 54H20, 60Fxx, 60G10]
28A35	Measures and integrals in product		Measure-preserving transformations One parameter continuous families of
•••	spaces	20110	One-parameter continuous families of measure-preserving transformations
28A50	Integration and disintegration of measures	28D15	General groups of measure-preserving
			transformations

	Entropy and other invariants None of the above, but in this section		Continued fractions [See also 11A55, 40A15]
20Esas	Missellandana taningin	30B99	None of the above, but in this section
	Miscellaneous topics in measure theory Nonstandard measure theory [See also 03H05, 26E35] Fuzzy measure theory [See also 03E72, 26E50, 94D05] Other connections with logic and set the-	30C10	Geometric function theory Polynomials Zeros of polynomials, rational functions, and other analytic functions (e.g. zeros of functions with bounded Dirichlet integral) (For algebraic theory, see 12D10;
	ory None of the above, but in this section	30C20	for real methods, see 26C10) Conformal mappings of special domains
	Functions of a complex variable		Covering theorems in conformal mapping theory
	(For analysis on manifolds, see 58-XX)	30C30	Numerical methods in conformal mapping theory [See also 65E05]
30-00	General reference works (handbooks, dictionaries, bibliographies, etc.)		General theory of conformal mappings
30-01	Instructional exposition (textbooks, tutorial papers, etc.)		Kernel functions and applications Special classes of univalent and multiva- lent functions (starlike, convex, bounded
30-02	Research exposition (monographs, survey articles)	30C50	rotation, etc.) Coefficient problems for univalent and
30-03	Historical (must also be assigned at least one classification number from Section 01)		multivalent functions General theory of univalent and multivalent functions
30-04	Explicit machine computation and programs (not the theory of computation or programming)		Quasiconformal mappings in the plane Quasiconformal mappings in \mathbb{R}^n , other generalizations
30-06	Proceedings, conferences, collections, etc.	30C70	Extremal problems for conformal and quasiconformal mappings, variational
	General properties Monogenic properties of complex functions (including polygenic and areolar	30C75	methods Extremal problems for conformal and quasiconformal mappings, other meth- ods
	monogenic functions) Inequalities in the complex domain None of the above, but in this section		Maximum principle; Schwarz's lemma, Lindelöf principle, analogues and gen- eralizations; subordination
30Bxx	Series expansions	30C85	Capacity and harmonic measure in the complex plane [See also 31A15]
	Power series (including lacunary series) Random power series	30C99	None of the above, but in this section
30B30	Boundary behavior of power series, over-convergence	30Dxx	Entire and meromorphic functions, and related topics
30B40 30B50	Analytic continuation Dirichlet series and other series expansions, exponential series [See also 11M41, 42-XX]	30D05	Functional equations in the complex domain, iteration and composition of analytic functions [See also 34Mxx, 37Fxx, 39-XX]
30B60	Completeness problems, closure of a system of functions	30D10	Representations of entire functions by series and integrals

30D15	Special classes of entire functions and growth estimates	30Gxx	Generalized function theory
30D20	Entire functions, general theory	30G06	Non-Archimedean function theory [See
	Meromorphic functions, general theory		also 12J25]; nonstandard function theory
	Distribution of values, Nevanlinna the-	20C12	[See also 03H05]
00200	ory	30G12	Finely holomorphic functions and topological function theory
30D40	Cluster sets, prime ends, boundary be-	30G20	Generalizations of Bers or Vekua type
30D45	havior Bloch functions, normal functions, nor-		(pseudoanalytic, p-analytic, etc.)
30D43	mal families		Discrete analytic functions
30D60	Quasi-analytic and other classes of func-	30G30	Other generalizations of analytic functions
20000	tions		(including abstract-valued functions)
30D99	None of the above, but in this section	30G35	Functions of hypercomplex variables
205			and generalized variables
	Miscellaneous topics of analysis in the complex domain	30G99	None of the above, but in this section
30E05	Moment problems, interpolation prob-	30Hxx	Spaces and algebras of
30E10	lems Approximation in the complex domain	DOTEN	analytic functions
		30H05	Bounded analytic functions
00210	plex domain	30H10	Hardy spaces
30E20	Integration, integrals of Cauchy type, in-	30H15	Nevanlinna class and Smirnov class
	tegral representations of analytic func-	30H20	Bergman spaces, Fock spaces
	tions [See also 45Exx]	30H25	Besov spaces and Q_p -spaces
30E25	Boundary value problems	30H30	Bloch spaces
30E99	[See also 45Exx] None of the above, but in this section		BMO-spaces
SOL	Twole of the above, but in this section		Algebras of analytic functions
30Fxx	Riemann surfaces		Corona theorems
	Compact Riemann surfaces and uni-	30H99	None of the above, but in this section
	formization [See also 14H15, 32G15]	201	T 4 4 4 1
30F15	Harmonic functions on Riemann sur-	30J05	Function theory on the disc Inner functions
20520	faces	30J10	Blaschke products
30F20	Classification theory of Riemann sur-	30J15	Singular inner functions
30F25	taces Ideal boundary theory	30J99	None of the above, but in this section
30F30	Differentials on Riemann surfaces	50,77	Two it of the above, but in this section
30F35	Fuchsian groups and automorphic func-	30Kxx	Universal holomorphic functions
	tions [See also 11Fxx, 20H10, 22E40,		Universal Taylor series
	32Gxx, 32Nxx]		Universal Dirichlet series
30F40	Kleinian groups [See also 20H10]	30K15	Bounded universal functions
30F45	Conformal metrics (hyperbolic, Poinca-	30K20	Compositional universality
20050	ré, distance functions)	30K99	None of the above, but in this section
30F50	Klein surfaces		
30F60 30F99	Teichmüller theory [See also 32G15]	30Lxx	Analysis on metric spaces
JU1'77	None of the above, but in this section		Geometric embeddings of metric spaces
		30L10	Quasiconformal mappings in metric
		207.00	spaces
		30L99	None of the above, but in this section

31-XX	Potential theory	31Cxx	Other generalizations
	(For probabilistic potential the-	31C05	Harmonic, subharmonic, superhar-
	ory, see 60J45)	24.640	monic functions
31-00	General reference works (handbooks,	31C10	Pluriharmonic and plurisubharmonic functions [See also 32U05]
	dictionaries, bibliographies, etc.)	31/212	Potential theory on Riemannian mani-
31-01	Instructional exposition	31C12	folds [See also 53C20; for Hodge theory,
	(textbooks, tutorial papers, etc.)		see 58A14]
31-02	Research exposition (monographs,	31C15	Potentials and capacities
01 00	survey articles)	31C20	Discrete potential theory and numerical
31-03	Historical (must also be assigned at least one classification number from Section		methods
	01)		Dirichlet spaces
31-04	Explicit machine computation and pro-		Martin boundary theory [See also 60J50]
01 01	grams (not the theory of computation or		Fine potential theory
	programming)	31C45	Other generalizations
31-06	Proceedings, conferences, collections,	21.000	(nonlinear potential theory, etc.)
	etc.	31C99	None of the above, but in this section
31Axx	Two-dimensional theory	31Dvv	Axiomatic potential theory
31A05	Harmonic, subharmonic,		Axiomatic potential theory
	superharmonic functions		None of the above, but in this section
31A10	Integral representations, integral opera-	01277	Trone of the above, but in this section
21 Δ 15	tors, integral equations methods Potentials and capacity, harmonic mea-	31Exx	Potential theory on metric spaces
31A13	sure, extremal length [See also 30C85]		Potential theory on metric spaces
31A20	Boundary behavior		None of the above, but in this section
	(theorems of Fatou type, etc.)	32-XX	Several complex variables and
31A25	Boundary value and inverse problems	0270	analytic spaces (For infinite-
31A30	Biharmonic, polyharmonic functions		dimensional holomorphy, see
	and equations, Poisson's equation		46G20, 58B12)
	Connections with differential equations	32-00	General reference works (handbooks,
31A99	None of the above, but in this section		dictionaries, bibliographies, etc.)
		32-01	Instructional exposition
	Higher-dimensional theory		(textbooks, tutorial papers, etc.)
	Harmonic, subharmonic, superharmonic functions	32-02	Research exposition (monographs, survey articles)
31B10			
	Integral representations, integral operators, integral equations methods	32-03	Historical (must also be assigned at least one classification number from Section
31B15		32-03	
31B15	tors, integral equations methods	32-03	one classification number from Section 01) Explicit machine computation and pro-
31B15 31B20	tors, integral equations methods Potentials and capacities, extremal		one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or
31B20	tors, integral equations methods Potentials and capacities, extremal length Boundary value and inverse problems	32-04	one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming)
31B20	tors, integral equations methods Potentials and capacities, extremal length Boundary value and inverse problems		one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or
31B20 31B25 31B30	tors, integral equations methods Potentials and capacities, extremal length Boundary value and inverse problems Boundary behavior Biharmonic and polyharmonic equa-	32-04	one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. Holomorphic functions of several com-
31B20 31B25 31B30	tors, integral equations methods Potentials and capacities, extremal length Boundary value and inverse problems Boundary behavior Biharmonic and polyharmonic equations and functions	32-04 32-06 32Axx	one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc.

32A07	Special domains (Reinhardt, Hartogs, circular, tube)	32Bxx	Local analytic geometry [See also 13-XX and 14-XX]
32A10	Holomorphic functions	32B05	Analytic algebras and generalizations,
32A12	Multifunctions	0200	preparation theorems
32A15	Entire functions	32B10	Germs of analytic sets,
32A17	Special families of functions		local parametrization
32A18	Bloch functions, normal functions	32B15	Analytic subsets of affine space
32A19	Normal families of functions, mappings	32B20	Semi-analytic sets and subanalytic sets
32A20	Meromorphic functions		[See also 14P15]
32A22	Nevanlinna theory (local); growth esti-	32B25	Triangulation and related questions
	mates; other inequalities (For geometric theory, see 32H25, 32H30)	32B99	None of the above, but in this section
32A25	Integral representations; canonical ker-	32Cxx	Analytic spaces
32A26	nels (Szegő, Bergman, etc.) Integral representations, constructed	32C05	Real-analytic manifolds, real-analytic spaces [See also 14Pxx, 58A07]
	kernels (e.g. Cauchy, Fantappiè-type kernels)	32C07	Real-analytic sets, complex Nash functions [See also 14P15, 14P20]
	Local theory of residues [See also 32C30]	32C09	Embedding of real analytic manifolds
32A30	Other generalizations of function theory of one complex variable (should also	32C11	Complex supergeometry [See also 14A22, 14M30, 58A50]
	be assigned at least one classification number from Section 30) (For functions	32C15	Complex spaces
	of several hypercomplex variables, see	32C18	Topology of analytic spaces
	30G35)	32C20	Normal analytic spaces
32A35	H^p -spaces, Nevanlinna spaces	32C22	Embedding of analytic spaces
	[See also 32M15, 42B30, 43A85, 46J15]	32C25	Analytic subsets and submanifolds
32A36	Bergman spaces	32C30	Integration on analytic sets and spaces,
32A37	Other spaces of holomorphic functions (e.g. bounded mean oscillation (BMOA),		currents (For local theory, see 32A25 or 32A27)
	vanishing mean oscillation (VMOA)) [See also 46Exx]	32C35	Analytic sheaves and cohomology groups [See also 14Fxx, 18F20, 55N30]
32A38	Algebras of holomorphic functions	32C36	Local cohomology of analytic spaces
	[See also 30H05, 46J10, 46J15]		Duality theorems
32A40	Boundary behavior of holomorphic functions	32C38	Sheaves of differential operators and
32A45	Hyperfunctions [See also 46F15]		their modules, <i>D</i> -modules [See also 14F10, 16S32, 35A27, 58J15]
	Harmonic analysis of several complex	32C55	The Levi problem in complex spaces,
	variables	0_000	generalizations
	[See mainly 43-XX]	32C81	Applications to physics
32A55	Singular integrals		None of the above, but in this section
32A60	Zero sets of holomorphic functions		,
32A65	Banach algebra techniques [See mainly 46Jxx]	32Dxx	Analytic continuation
32 A 70	Functional analysis techniques		Domains of holomorphy
<i>52111</i> U	[See mainly 46Exx]		Envelopes of holomorphy
32A99	None of the above, but in this section		Continuation of analytic objects
	and the second		Removable singularities
			Riemann domains
		32D00	Mong of the above but in this section

32Exx	Holomorphic convexity	32Hxx	Holomorphic mappings and correspondences
	Holomorphically convex complex spaces, reduction theory	32H02	Holomorphic mappings, (holomorphic) embeddings and related questions
32E10	Stein spaces, Stein manifolds	32H04	Meromorphic mappings
	Polynomial convexity		Boundary uniqueness of mappings
32E30 32E35	Holomorphic and polynomial approximation, Runge pairs, interpolation		Picard-type theorems and generalizations (For function-theoretic properties,
32E33	Global boundary behavior of holomorphic functions	32H30	see 32A22) Value distribution theory in higher di-
32E40	The Levi problem		mensions (For function-theoretic properties, see 32A22)
32E99	None of the above, but in this section	32H35	Proper mappings, finiteness theorems
			Boundary regularity of mappings
	Geometric convexity		Iteration problems
32F10	<i>q</i> -convexity, <i>q</i> -concavity		None of the above, but in this section
	Other notions of convexity	3211))	Trone of the above, but in this section
32F18	Finite-type conditions	32Jxx	Compact analytic spaces (For Riemann
32F27	Topological consequences of geometric convexity	<i>52</i> ,777	surfaces, see 14Hxx, 30Fxx; for algebraic
32F32	Analytical consequences of geometric	32J05	theory, see 14Jxx) Compactification of analytic spaces
	convexity (vanishing theorems, etc.)	32J10	Algebraic dependence theorems
22545	•	32J15	Compact surfaces
	Invariant metrics and pseudodistances	32J17	Compact 3-folds
32F99	None of the above, but in this section	32J17	Compact n-folds
200	Defense Consellation International	32J25	Transcendental methods of algebraic ge-
	Deformations of analytic structures Deformations of complex structures		ometry [See also 14C30]
32G07	[See also 13D10, 16S80, 58H10, 58H15] Deformations of special (e.g. CR) struc-	32J27	Compact Kähler manifolds: generalizations, classification
	tures	32J81	Applications to physics
32G08	Deformations of fiber bundles	32J99	None of the above, but in this section
32G10	Deformations of submanifolds and sub-		
	spaces	32Kxx	Generalizations of analytic spaces
32G13	Analytic moduli problems (For algebraic moduli problems, see 14D20, 14D22, 14H10, 14J10) [See also 14H15, 14J15]		(should also be assigned at least one other classification number from Sec- tion 32 describing the type of problem)
32G15	Moduli of Riemann surfaces, Teich-		Banach analytic spaces [See also 58Bxx]
22/20	müller theory [See also 14H15, 30Fxx]	32K07	Formal and graded complex spaces
32G20	Period matrices, variation of Hodge structure; degenerations [See also 14D05, 14D07, 14K30]	32K15	[See also 58C50] Differentiable functions on analytic
32C34	Moduli and deformations for ordinary		spaces, differentiable spaces [See also 58C25]
32034	differential equations (e.g. Knizhnik- Zamolodchikov equation)	32K99	None of the above, but in this section
32G81	[See also 34Mxx] Applications to physics	32Lxx	Holomorphic fiber spaces
	None of the above, but in this section	221.05	[See also 55Rxx]
	- 12-10 of the table of but in this section	32L05	Holomorphic bundles and generaliza- tions

32L10	Sheaves and cohomology of sections of holomorphic vector bundles, general re-		Kähler manifolds
	sults [See also 14F05, 18F20, 55N30]	32Q20	Kähler-Einstein manifolds [See also 53Cxx]
32L15	Bundle convexity [See also 32F10]	32025	Calabi-Yau theory [See also 14J30]
	Vanishing theorems		Notions of stability
	Twistor theory, double fibrations		Stein manifolds
	[See also 53C28]		Uniformization
32L81	Applications to physics		Complex manifolds as subdomains of
	None of the above, but in this section	32Q33	Euclidean space
		32Q40	Embedding theorems
32Mxx	Complex spaces with a group of automorphisms	32Q45	Hyperbolic and Kobayashi hyperbolic manifolds
32M05	Complex Lie groups, automorphism groups acting on complex spaces	32Q55	Topological aspects of complex manifolds
	[See also 22E10]	32Q57	Classification theorems
32M10	Homogeneous complex manifolds	32Q60	Almost complex manifolds
	[See also 14M17, 57T15]	32Q65	Pseudoholomorphic curves
32M12	Almost homogeneous manifolds and spaces [See also 14M17]		None of the above, but in this section
32M15	Hermitian symmetric spaces, bounded	32Sxx	Singularities [See also 58Kxx]
	symmetric domains, Jordan algebras	32S05	Local singularities [See also 14J17]
	[See also 22E10, 22E40, 53C35, 57T15]	32S10	Invariants of analytic local rings
32M17	Automorphism groups of \mathbb{C}^n and affine	32S15	Equisingularity (topological and ana-
32M25	manifolds Complex vector fields		lytic) [See also 14E15]
32M99	None of the above, but in this section	32S20	Global theory of singularities; cohomological properties [See also 14E15]
32Nxx	Automorphic functions [See also 11Fxx, 20H10, 22E40, 30F35]	32S22	Relations with arrangements of hyperplanes [See also 52C35]
32N05	General theory of automorphic func- tions of several complex variables	32S25	Surface and hypersurface singularities [See also 14]17]
32N10	Automorphic forms	32S30	Deformations of singularities; vanishing
	Automorphic functions in symmetric		cycles [See also 14B07]
	domains None of the above, but in this section	32S35	Mixed Hodge theory of singular varieties [See also 14C30, 14D07]
321177	None of the above, but in this section	32S40	Monodromy; relations with differential
22D.c.	Non Auchimodon androis (charld		equations and <i>D</i> -modules
32PXX	Non-Archimedean analysis (should also be assigned at least one other classification number from Section 22 de	32S45	Modifications; resolution of singularities [See also 14E15]
	sification number from Section 32 describing the type of problem)	32S50	Topological aspects: Lefschetz theorems,
32P05	Non-Archimedean analysis (should also	0_000	topological classification, invariants
321 03	be assigned at least one other classifica-	32S55	Milnor fibration; relations with knot the-
	tion number from Section 32 describing		ory [See also 57M25, 57Q45]
	the type of problem)	32S60	Stratifications; constructible sheaves; in-
32P99	None of the above, but in this section		tersection cohomology [See also 58Kxx]
		32S65	Singularities of holomorphic vector
32Qxx	Complex manifolds		fields and foliations
	Negative curvature manifolds	32S70	Other operations on singularities
	Positive curvature manifolds	32S99	None of the above, but in this section

40 Special functions

		32W50	Other partial differential equations of
32Txx	Pseudoconvex domains		complex analysis
32T05	Domains of holomorphy	32W99	None of the above, but in this section
32T15	Strongly pseudoconvex domains	33-XX	Special functions (33-XX deals
32T20	Worm domains	00 75	with the properties of functions
32T25	Finite type domains		as functions) (For orthogonal
32T27	Geometric and analytic invariants on		functions, see 42Cxx; for aspects
	weakly pseudoconvex boundaries		of combinatorics see 05Axx; for
32T35	Exhaustion functions		number-theoretic aspects see 11-
32T40	Peak functions		XX; for representation theory see 22Exx)
32T99	None of the above, but in this section		, , , , , , , , , , , , , , , , , , ,
		33-00	General reference works (handbooks,
	Pluripotential theory	33-01	dictionaries, bibliographies, etc.)
32U05	Plurisubharmonic functions and gener-	33-01	Instructional exposition (textbooks, tutorial papers, etc.)
	alizations [See also 31C10]	33-02	Research exposition (monographs,
	Plurisubharmonic exhaustion functions	00 02	survey articles)
	General pluripotential theory	33-03	Historical (must also be assigned at least
	Capacity theory and generalizations		one classification number from Section
	Lelong numbers		01)
	Removable sets	33-04	Explicit machine computation and pro-
	Pluricomplex Green functions		grams (not the theory of computation or
	Currents		programming)
32099	None of the above, but in this section	33-06	Proceedings, conferences, collections, etc.
32Vxx	CR manifolds	33Bxx	Elementary classical functions
32V05	CR structures, CR operators, and gener-		Exponential and trigonometric func-
221140	alizations		tions
	CR functions		Gamma, beta and polygamma functions
	CR manifolds as boundaries of domains	33B20	Incomplete beta and gamma functions
	Analysis on CR manifolds		(error functions, probability integral,
32 V 25	Extension of functions and other analytic	33B30	Fresnel integrals)
221/20	objects from CR manifolds	33B99	Higher logarithm functions None of the above, but in this section
	Embeddings of CR manifolds	33099	None of the above, but in this section
	Finite type conditions on CR manifolds	22Cvv	Uzmargaomatria functions
32 V 40	Real submanifolds in complex manifolds		Hypergeometric functions Classical hypergeometric functions, $_2F_1$
32V99	None of the above, but in this section		Bessel and Airy functions, cylinder func-
		33C10	tions, $_0F_1$
32Wxx	Differential operators in several	33C15	Confluent hypergeometric functions,
	variables		Whittaker functions, $_1F_1$
32W05	$\overline{\partial}$ and $\overline{\partial}$ -Neumann operators	33C20	Generalized hypergeometric series, pF_q
32W10	$\bar{\partial}_b$ and $\bar{\partial}_b$ -Neumann operators	33C45	Orthogonal polynomials and functions
	Complex Monge-Ampère operators		of hypergeometric type (Jacobi, La-
	Pseudodifferential operators in several		guerre, Hermite, Askey scheme, etc.)
	complex variables		[See also 42C05 for general orthogonal polynomials and functions]
32W30	Heat kernels in several complex vari-	33C47	
	ables	JJC4/	Other special orthogonal polynomials and functions

33C50	Orthogonal polynomials and functions in several variables expressible in terms	33Exx	Other special functions
	of special functions in one variable		Elliptic functions and integrals
33C52	Orthogonal polynomials and functions	33E10	Lamé, Mathieu, and spheroidal wave
00002	associated with root systems	00E10	functions
33C55	Spherical harmonics	33E12	Mittag-Leffler functions and generaliza-
	Hypergeometric integrals and functions	33E15	other wave functions
	defined by them (E, G, H) and I functions)		Painlevé-type functions
33C65	Appell, Horn and Lauricella functions	33E20	Other functions defined by series and in-
	Hypergeometric functions associated	33 L 20	tegrals
	with root systems	33E30	_
33C70	Other hypergeometric functions and in-	00200	tial, difference and integral equations
	tegrals in several variables	33E50	Special functions in characteristic <i>p</i>
33C75	Elliptic integrals as hypergeometric		(gamma functions, etc.)
	functions	33E99	None of the above, but in this section
33C80	Connections with groups and algebras,		,
22.500	and related topics	33Fxx	Computational aspects
	Applications	33F05	Numerical approximation and evalua-
33C99	None of the above, but in this section		tion [See also 65D20]
		33F10	Symbolic computation (Gosper and Zeil-
	Basic hypergeometric functions		berger algorithms, etc.) [See also 68W30]
33D05	<i>q</i> -gamma functions, <i>q</i> -beta functions and	33F99	None of the above, but in this section
22D15	integrals Basic hypergeometric functions in one	34-XX	Ordinary differential equations
33D13	basic hypergeometric functions in one		J 1
		34-00	Canaral reference works (handbooks
	variable, $_r\phi_s$	34-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
	variable, $_r\phi_s$ Basic orthogonal polynomials and func-	34-00 34-01	dictionaries, bibliographies, etc.)
33D45	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.)		•
33D45	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions		dictionaries, bibliographies, etc.) Instructional exposition
33D45	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.)	34-01	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.)
33D45 33D50	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable	34-01	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs,
33D45 33D50	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and func-	34-01 34-02	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section
33D45 33D50	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems	34-01 34-02 34-03	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01)
33D45 33D50 33D52	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.)	34-01 34-02	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and pro-
33D45 33D50 33D52	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and	34-01 34-02 34-03	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or
33D45 33D50 33D52 33D60	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them	34-01 34-02 34-03 34-04	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming)
33D45 33D50 33D52 33D60 33D65	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases	34-01 34-02 34-03	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections,
33D45 33D50 33D52 33D60 33D65	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associ-	34-01 34-02 34-03 34-04 34-06	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc.
33D45 33D50 33D52 33D60 33D65 33D67	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems	34-01 34-02 34-03 34-04 34-06 34Axx	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory
33D45 33D50 33D52 33D60 33D65 33D67	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions	34-01 34-02 34-03 34-04 34-06 34Axx 34A05	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions
33D45 33D50 33D52 33D60 33D65 33D67 33D70	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions and integrals in several variables	34-01 34-02 34-03 34-04 34-06 34Axx 34A05 34A07	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions Fuzzy differential equations
33D45 33D50 33D52 33D60 33D65 33D67 33D70	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions and integrals in several variables Connections with quantum groups,	34-01 34-02 34-03 34-04 34-06 34Axx 34A05 34A07 34A08	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions Fuzzy differential equations Fractional differential equations
33D45 33D50 33D52 33D60 33D65 33D67 33D70	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions and integrals in several variables	34-01 34-02 34-03 34-04 34-06 34Axx 34A05 34A07 34A08	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions Fuzzy differential equations Fractional differential equations Implicit equations, differential-algebraic
33D45 33D50 33D52 33D60 33D65 33D67 33D70 33D80	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions and integrals in several variables Connections with quantum groups, Chevalley groups, p -adic groups, Hecke	34-01 34-02 34-03 34-04 34-06 34Axx 34A05 34A07 34A08 34A09	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions Fuzzy differential equations Fractional differential equations Implicit equations, differential-algebraic equations [See also 65L80]
33D45 33D50 33D52 33D60 33D65 33D67 33D70 33D80 33D90	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions and integrals in several variables Connections with quantum groups, Chevalley groups, p -adic groups, Hecke algebras, and related topics	34-01 34-02 34-03 34-04 34-06 34Axx 34A05 34A07 34A08 34A09	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions Fuzzy differential equations Fractional differential equations Implicit equations, differential-algebraic equations [See also 65L80] Initial value problems, existence,
33D45 33D50 33D52 33D60 33D65 33D67 33D70 33D80 33D90	variable, $_r\phi_s$ Basic orthogonal polynomials and functions (Askey-Wilson polynomials, etc.) Orthogonal polynomials and functions in several variables expressible in terms of basic hypergeometric functions in one variable Basic orthogonal polynomials and functions associated with root systems (Macdonald polynomials, etc.) Basic hypergeometric integrals and functions defined by them Bibasic functions and multiple bases Basic hypergeometric functions associated with root systems Other basic hypergeometric functions and integrals in several variables Connections with quantum groups, Chevalley groups, p -adic groups, Hecke algebras, and related topics Applications	34-01 34-02 34-03 34-04 34-06 34Axx 34A05 34A07 34A08 34A09	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General theory Explicit solutions and reductions Fuzzy differential equations Fractional differential equations Implicit equations, differential-algebraic equations [See also 65L80]

34A25	Analytical theory: series, transforma-	34B60	Applications
	tions, transforms, operational calculus, etc. [See also 44-XX]	34B99	None of the above, but in this section
34A26	Geometric methods in differential equa-	34Cxx	Qualitative theory [See also 37-XX]
34A30	tions Linear equations and systems, general	34C05	Location of integral curves, singular
	Lattice differential equations		points, limit cycles
	Nonlinear equations and systems, gen-	34C07	Theory of limit cycles of polynomial and
	eral		analytic vector fields (existence, uniqueness, bounds, Hilbert's 16th problem
34A35	Differential equations of infinite order		and ramifications)
34A36	Discontinuous equations	34C08	Connections with real algebraic geom-
34A37	Differential equations with impulses		etry (fewnomials, desingularization, ze-
34A38	Hybrid systems		ros of Abelian integrals, etc.)
34A40	Differential inequalities [See also 26D20]	34C10	Oscillation theory, zeros, disconjugacy
34A45	Theoretical approximation of solutions		and comparison theory
	(For numerical analysis, see 65Lxx)	34C11	Growth, boundedness
	Inverse problems	34C12	Monotone systems
34A60	Differential inclusions	34C14	Symmetries, invariants
34A99	[See also 49J21, 49K21] None of the above, but in this section	34C15	Nonlinear oscillations, coupled oscillators
		34C20	Transformation and reduction of equa-
34Bxx	Boundary value problems		tions and systems, normal forms
	(For ordinary differential operators,		Bifurcation [See also 37Gxx]
0 4 D 0 E	see 34Lxx)		Periodic solutions
	Linear boundary value problems	34C26	Relaxation oscillations
34B07	Linear boundary value problems with nonlinear dependence on the spectral		Almost and pseudo-almost periodic solutions
24B00	parameter	34C28	Complex behavior, chaotic systems
34B08	Parameter dependent boundary value problems	24620	[See also 37Dxx]
3/R00	-		Averaging method Homoclinic and heteroclinic solutions
34B10	Boundary eigenvalue problems Nonlocal and multipoint boundary		
J1D10	value problems		Equations and systems on manifolds Equivalence, asymptotic equivalence
34B15	Nonlinear boundary value problems		Invariant manifolds
	Singular nonlinear boundary value		
OIDIO	problems		Multifrequency systems
34B18	Positive solutions of nonlinear boundary value problems		Hysteresis Qualitative investigation and simulation
3/B20	Weyl theory and its generalizations	24600	of models
	Sturm-Liouville theory [See also 34Lxx]	34C99	None of the above, but in this section
	Green functions	24D-04	Ctability the same [Case also 27/77 02Daw]
	Special equations		Stability theory [See also 37C75, 93Dxx]
J4D30	(Mathieu, Hill, Bessel, etc.)		Asymptotic properties Synchronization
34B37	Boundary value problems with impulses		Characteristic and Lyapunov exponents
34B40	Boundary value problems on infinite in-		Dichotomy, trichotomy
	tervals		Perturbations
34B45	Boundary value problems on graphs and		Singular perturbations
	networks		Stability
		01020	Juliny

	Global stability Structural stability and analogous concepts [See also 37C20]	34Kxx	Functional-differential and differential-difference equations [See also 37-XX]
34D35	Stability of manifolds of solutions	34K05	General theory
	Attractors [See also 37C70, 37D45]	34K06	Linear functional-differential equations
34D99	None of the above, but in this section	34K07	Theoretical approximation of solutions
		34K08	Spectral theory of functional-differential
34Exx	Asymptotic theory		operators
34E05	Asymptotic expansions	34K09	Functional-differential inclusions
34E10	Perturbations, asymptotics	34K10	Boundary value problems
34E13	Multiple scale methods	34K11	Oscillation theory
34E15	Singular perturbations, general theory	34K12	Growth, boundedness, comparison of
34E17	Canard solutions	0.4764.0	solutions
34E18	Methods of nonstandard analysis		Periodic solutions
34E20	0 1		Almost and pseudo-periodic solutions
	theory, WKB methods	34K17	Transformation and reduction of equa-
34E99	None of the above, but in this section	211/1Q	tions and systems, normal forms Bifurcation theory
			Invariant manifolds
34Fxx	Equations and systems with random-		Stability theory
34E05	ness [See also 34K50, 60H10, 93E03]		Stationary solutions
34F05	Equations and systems with randomness [See also 34K50, 60H10, 93E03]		Complex (chaotic) behavior of solutions
34F10	Bifurcation		-
	Resonance phenomena		Asymptotic theory Singular perturbations
	None of the above, but in this section		Perturbations
011))	Trone of the above, but in this section		
34Gxx	Differential equations in abstract		Numerical approximation of solutions Inverse problems
JIGAA	spaces [See also 34Lxx, 37Kxx, 47Dxx, 47Hxx, 47Jxx, 58D25]		Equations in abstract spaces [See also 34Gxx, 35R09, 35R10, 47Jxx]
34G10	Linear equations [See also 47D06, 47D09]	34K31	Lattice functional-differential equations
34G20	Nonlinear equations		Implicit equations
	[See also 47Hxx, 47Jxx]		Averaging
	Evolution inclusions		Hybrid systems
34G99	None of the above, but in this section		Control problems [See also 49J21, 49K21, 93C23]
34Hxx	Control problems	34K36	Fuzzy functional-differential equations
	[See also 49J15, 49K15, 93C15]		Functional-differential equations with
34H05	Control problems		fractional derivatives
241110	[See also 49J15, 49K15, 93C15]	34K38	Functional-differential inequalities
	Chaos control		Neutral equations
	Stabilization Pifurgation control		Equations with impulses
	Bifurcation control	34K50	Stochastic functional-differential equa-
341199	None of the above, but in this section		tions [See also , 60Hxx]
			Qualitative investigation and simulation of models
		34K99	None of the above, but in this section

34Lxx	Ordinary differential operators [See also 47E05]	34Nxx	Dynamic equations on time scales or measure chains (For real analysis or
34L05	General spectral theory		time scales see 26E70)
34L10	Eigenfunctions, eigenfunction expansions, completeness of eigenfunctions	34N05	Dynamic equations on time scales of measure chains (For real analysis on time
34L15	Eigenvalues, estimation of eigenvalues, upper and lower bounds	34N99	scales or measure chains, see 26E70) None of the above, but in this section
34L16	Numerical approximation of eigenval-	35-XX	Partial differential equations
34L20	ues and of other parts of the spectrum Asymptotic distribution of eigenvalues,	35-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
34L25	asymptotic theory of eigenfunctions Scattering theory, inverse scattering	35-01	Instructional exposition (textbooks, tutorial papers, etc.)
	Nonlinear ordinary differential operators	35-02	Research exposition (monographs, survey articles)
34L40	Particular operators (Dirac, one-dimensional Schrödinger, etc.)	35-03	Historical (must also be assigned at leas one classification number from Section
34L99	None of the above, but in this section		01)
		35-04	Explicit machine computation and pro-
	Differential equations in the complex domain [See also 30Dxx, 32G34]		grams (not the theory of computation or programming)
	Linear equations and systems	35-06	Proceedings, conferences, collections,
	Entire and meromorphic solutions		etc.
	Oscillation, growth of solutions	35Axx	General topics
34M15	Algebraic aspects (differential-algebraic, hypertranscendence, group-theoretical)	35A01	Existence problems: global existence, local existence, non-existence
	Formal solutions, transform techniques	35A02	Uniqueness problems: global unique
	Asymptotics, summation methods	25 4 00	ness, local uniqueness, non-uniqueness
34IVI33	Singularities, monodromy, local behavior of solutions, normal forms		Fundamental solutions
34M40	Stokes phenomena and connection prob-		Classical solutions
J11 11 10	lems (linear and nonlinear)		Cauchy-Kovalevskaya theorems Variational methods
34M45	Differential equations on complex man-		
	ifolds		Topological and monotonicity methods
34M50	Inverse problems (Riemann-Hilbert, in-		Parametrices Wave front sets
	verse differential Galois, etc.)		
34M55	Painlevé and other special equations; classification, hierarchies;		Analytic methods, singularities Propagation of singularities
34M56	Isomonodromic deformations		Transform methods (e.g. integral trans-
	Singular perturbation problems in the	0011	forms)
011100	complex domain (complex WKB, turning points, steepest descent) [See also 34E20]	35A23	Inequalities involving derivatives and differential and integral operators, in- equalities for integrals
34M99	None of the above, but in this section	35A24	Methods of ordinary differential equations
		35A25	Other special methods
		35A27	Microlocal methods; methods of shear theory and homological algebra in PDE [See also 32C38, 58J15]

Partial differential equations 45

35A30	Geometric theory, characteristics, transformations [See also 58J70, 58J72]		Traveling wave solutions
35 <u>4</u> 35	Theoretical approximation to solutions		Soliton solutions
337 133	(For numerical analysis, see 65Mxx,		Trigonometric solutions
	65Nxx)		Series solutions
35A99	None of the above, but in this section		Polynomial solutions
	,		Integral representations of solutions
35Bxx	Qualitative properties of solutions		Asymptotic expansions
	Oscillation, zeros of solutions, mean value theorems, etc.	35C99 	None of the above, but in this section
35B06	Symmetries, invariants, etc.		Generalized solutions
	Axially symmetric solutions		Weak solutions
35B08	Entire solutions		Strong solutions
35B09	Positive solutions		Viscosity solutions
35B10	Periodic solutions	35D99	None of the above, but in this section
35B15	Almost and pseudo-almost periodic so-		
	lutions Perturbations	35Exx	Equations and systems with constant coefficients [See also 35N05]
35B25	Singular perturbations	35E05	Fundamental solutions
	Homogenization; equations in media	35E10	Convexity properties
	with periodic structure	35E15	Initial value problems
	[See also 74Qxx, 76M50]		General theory
35B30	Dependence of solutions on initial and boundary data, parameters	35E99	None of the above, but in this section
	ISOn also 37/CyvI		
2ED22	[See also 37Cxx]	35Fxx	General first-order equations
	Bifurcation [See also 37Gxx, 37K50]		and systems
35B33	Bifurcation [See also 37Gxx, 37K50] Critical exponents	35F05	and systems Linear first-order equations
35B33 35B34	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances	35F05	and systems Linear first-order equations Initial value problems for linear first-
35B33 35B34 35B35	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability	35F05 35F10	and systems Linear first-order equations Initial value problems for linear first-order equations
35B33 35B34 35B35 35B36	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation	35F05	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-
35B33 35B34 35B35 35B36 35B38	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points	35F05 35F10 35F15	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations
35B33 35B34 35B35 35B36 35B38 35B40	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions	35F05 35F10	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for lin-
35B33 35B34 35B35 35B36 35B38 35B40 35B41	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors	35F05 35F10 35F15 35F16	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds	35F05 35F10 35F15 35F16 35F20	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up	35F05 35F10 35F15 35F16 35F20 35F21	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates	35F05 35F10 35F15 35F16 35F20	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles	35F05 35F10 35F15 35F16 35F20 35F21 35F25	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles	35F05 35F10 35F15 35F16 35F20 35F21	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51 35B53	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems	35F05 35F10 35F15 35F16 35F20 35F21 35F25	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems Continuation and prolongation of solu-	35F05 35F10 35F15 35F16 35F20 35F21 35F25 35F30 35F31	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for nonlinear first-order equations
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51 35B53	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems Continuation and prolongation of solutions [See also 58A15, 58A17, 58Hxx]	35F05 35F10 35F15 35F16 35F20 35F21 35F25 35F30 35F31 35F35	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for nonlinear first-order equations Linear first-order systems
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51 35B53 35B60	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems Continuation and prolongation of solu-	35F05 35F10 35F15 35F16 35F20 35F21 35F25 35F30 35F31	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for nonlinear first-order equations
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51 35B53 35B60	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems Continuation and prolongation of solutions [See also 58A15, 58A17, 58Hxx] Smoothness and regularity of solutions	35F05 35F10 35F15 35F16 35F20 35F21 35F25 35F30 35F31 35F35	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for nonlinear first-order equations Linear first-order systems Initial value problems for linear first-order systems Boundary value problems for linear first-order systems Boundary value problems for linear first-order systems
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B44 35B45 35B50 35B51 35B53 35B60	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems Continuation and prolongation of solutions [See also 58A15, 58A17, 58Hxx] Smoothness and regularity of solutions	35F05 35F10 35F15 35F16 35F20 35F21 35F25 35F30 35F31 35F35 35F40 35F45	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for nonlinear first-order equations Linear first-order systems Initial value problems for linear first-order systems Boundary value problems for linear first-order systems Boundary value problems for linear first-order systems
35B33 35B34 35B35 35B36 35B38 35B40 35B41 35B42 35B45 35B50 35B51 35B53 35B60 35B65 35B65 35B99	Bifurcation [See also 37Gxx, 37K50] Critical exponents Resonances Stability Pattern formation Critical points Asymptotic behavior of solutions Attractors Inertial manifolds Blow-up A priori estimates Maximum principles Comparison principles Liouville theorems, Phragmén-Lindelöf theorems Continuation and prolongation of solutions [See also 58A15, 58A17, 58Hxx] Smoothness and regularity of solutions None of the above, but in this section	35F05 35F10 35F15 35F16 35F20 35F21 35F25 35F30 35F31 35F35 35F40	and systems Linear first-order equations Initial value problems for linear first-order equations Boundary value problems for linear first-order equations Initial-boundary value problems for linear first-order equations Nonlinear first-order equations Hamilton-Jacobi equations Initial value problems for nonlinear first-order equations Boundary value problems for nonlinear first-order equations Initial-boundary value problems for nonlinear first-order equations Linear first-order systems Initial value problems for linear first-order systems Boundary value problems for linear first-order systems Boundary value problems for linear first-order systems

35F50 35F55	Nonlinear first-order systems Initial value problems for nonlinear first-	35Jxx	Elliptic equations and systems [See also 58J10, 58J20]
35F60	order systems Boundary value problems for nonlinear first-order systems	35J05	Laplacian operator, reduced wave equation (Helmholtz equation), Poissor equation [See also 31Axx, 31Bxx]
35F61	Initial-boundary value problems for	35J08	Green's functions
25500	nonlinear first-order systems	35J10	Schrödinger operator [See also 35Pxx]
35F99	None of the above, but in this section	35J15	Second-order elliptic equations
25	C 11'1 1 "	35J20	Variational methods for second-order el
35GXX	General higher-order equations and systems	25125	liptic equations
35G05	Linear higher-order equations	35J25	Boundary value problems for second-
	Initial value problems for linear higher- order equations	35J30	order elliptic equations Higher-order elliptic equations [See also 31A30, 31B30]
35G15	Boundary value problems for linear higher-order equations	35J35	Variational methods for higher-order elliptic equations
35G16	Initial-boundary value problems for linear higher-order equations	35J40	Boundary value problems for higher- order elliptic equations
35G20	Nonlinear higher-order equations	35J46	First-order elliptic systems
35G25	Initial value problems for nonlinear	35J47	Second-order elliptic systems
25.00	higher-order equations	35J48	Higher-order elliptic systems
35 G 30	Boundary value problems for nonlinear	35J50	Variational methods for elliptic systems
25 <i>C</i> 21	higher-order equations Initial-boundary value problems for	35J56	Boundary value problems for first-order
JJGJ1	nonlinear higher-order equations	05155	elliptic systems
35G35	Linear higher-order systems	35J57	Boundary value problems for second- order elliptic systems
	Initial value problems for linear higher-	35J58	Boundary value problems for higher
	order systems	22,00	order elliptic systems
35G45	Boundary value problems for linear	35J60	Nonlinear elliptic equations
05046	higher-order systems	35J61	Semilinear elliptic equations
35G46	Initial-boundary value problems for linear higher-order systems	35J62	Quasilinear elliptic equations
35G50	Nonlinear higher-order systems	35J65	Nonlinear boundary value problems for
	Initial value problems for nonlinear	05144	linear elliptic equations
	higher-order systems	35J66	Nonlinear boundary value problems for nonlinear elliptic equations
35G60	Boundary value problems for nonlinear higher-order systems	35J67	Boundary values of solutions to elliptic equations
35G61	Initial-boundary value problems for	35J70	Degenerate elliptic equations
	nonlinear higher-order systems	35]75	Singular elliptic equations
35G99	None of the above, but in this section	35J86	Linear elliptic unilateral problems and
2511	Class (2.11) (2.11) (2.11)		linear elliptic variational inequalities
	Close-to-elliptic equations and systems Hypoelliptic equations	OFTOF	[See also 35R35, 49J40]
	Hypoelliptic equations Subelliptic equations	35J87	Nonlinear elliptic unilateral problems and nonlinear elliptic variational in-
	Quasi-elliptic equations		equalities [See also 35R35, 49J40]
	None of the above, but in this section	35J88	Systems of elliptic variational inequalities [See also 35R35, 49]40]

35J91	Semilinear elliptic equations with Laplacian, bi-Laplacian or poly-Laplacian	35K86	Nonlinear parabolic unilateral problems and nonlinear parabolic variational in-
35J92	Quasilinear elliptic equations with <i>p</i> -Laplacian	35K87	equalities [See also 35R35, 49J40] Systems of parabolic variational inequal-
35J93	Quasilinear elliptic equations with mean		ities [See also 35R35, 49J40]
	curvature operator		Abstract parabolic equations
35J96	Elliptic Monge-Ampère equations	35K91	Semilinear parabolic equations with
35J99	None of the above, but in this section		Laplacian, bi-Laplacian or poly-Laplacian
35Kxx	Parabolic equations and systems [See	35K92	Quasilinear parabolic equations with <i>p</i> -Laplacian
25V05	also 35Bxx, 35Dxx, 35R30, 35R35, 58J35]	35K93	Quasilinear parabolic equations with
	Heat equation Heat kernel		mean curvature operator
	Second-order parabolic equations		Parabolic Monge-Ampère equations
	Initial value problems for second-order	35K99	None of the above, but in this section
	parabolic equations	051	TT 1 11 10
35K20	Initial-boundary value problems for second-order parabolic equations		Hyperbolic equations and systems [See also 58J45]
35K25	Higher-order parabolic equations		First-order hyperbolic equations
	Initial value problems for higher-order parabolic equations		Initial value problems for first-order hyperbolic equations
35K35	Initial-boundary value problems for higher-order parabolic equations		Initial-boundary value problems for first-order hyperbolic equations
35K40	Second-order parabolic systems		Wave equation
	Higher-order parabolic systems	35L10	71 1
	Initial value problems for second-order parabolic systems	35L15	Initial value problems for second-order hyperbolic equations
35K46	Initial value problems for higher-order parabolic systems	35L20	Initial-boundary value problems for second-order hyperbolic equations
35K51	Initial-boundary value problems for	35L25	Higher-order hyperbolic equations
	second-order parabolic systems	35L30	Initial value problems for higher-order hyperbolic equations
	Initial-boundary value problems for higher-order parabolic systems	35L35	Initial-boundary value problems for higher-order hyperbolic equations
	Nonlinear parabolic equations	35L40	First-order hyperbolic systems
	Reaction-diffusion equations		Initial value problems for first-order hy-
	Semilinear parabolic equations		perbolic systems
	Quasilinear parabolic equations	35L50	Initial-boundary value problems for
33 K 60	Nonlinear initial value problems for linear parabolic equations		first-order hyperbolic systems
35K61	Nonlinear initial-boundary value prob-		Second-order hyperbolic systems
001101	lems for nonlinear parabolic equations	35L52	Initial value problems for second-order hyperbolic systems
	Degenerate parabolic equations	35L53	Initial-boundary value problems for
	Singular parabolic equations		second-order hyperbolic systems
35K70	Ultraparabolic equations, pseudoparabolic equations, etc.	35L55 35L56	Higher-order hyperbolic systems
35K85	Linear parabolic unilateral problems and linear parabolic variational inequalities [See also 35R35, 49J40]	JULJU	Initial value problems for higher-order hyperbolic systems

35L57	Initial-boundary value problems for higher-order hyperbolic systems	35M33	Initial-boundary value problems for systems of mixed type
35L60	Nonlinear first-order hyperbolic equations	35M85	Linear unilateral problems and variational inequalities of mixed type
35L65	Conservation laws		[See also 35R35, 49J40]
35L67	Shocks and singularities [See also 58Kxx, 76L05]	35M86	Nonlinear unilateral problems and non- linear variational inequalities of mixed
35L70	Nonlinear second-order hyperbolic		type [See also 35R35, 49J40]
	equations	35M87	Systems of variational inequalities
35L71	Semilinear second-order hyperbolic		of mixed type [See also 35R35, 49J40]
	equations	35M99	None of the above, but in this section
35L72	71		
251.75	equations	35Nxx	Overdetermined systems
35L75	Nonlinear higher-order hyperbolic	2ENIOE	[See also 58Hxx, 58J10, 58J15]
251.76	equations	331103	Overdetermined systems with constant coefficients
	Semilinear higher-order hyperbolic equations	35N10	Overdetermined systems with variable coefficients
35L77	~ 0	35N15	$\overline{\partial}$ -Neumann problem and generaliza-
251.00	equations	001110	tions; formal complexes [See also 32W05,
	Degenerate hyperbolic equations		32W10, 58J10]
35L81	0 11 1	35N20	Overdetermined initial value problems
	Pseudohyperbolic equations	35N25	Overdetermined boundary value prob-
33163	Linear hyperbolic unilateral problems and linear hyperbolic variational in- equalities [See also 35R35, 49J40]	35N30	lems Overdetermined initial-boundary value
35L86	Nonlinear hyperbolic unilateral prob-	25 100	problems
2220	lems and nonlinear hyperbolic variational inequalities [See also 35R35, 49J40]	35N99 	None of the above, but in this section
35L87	Unilateral problems and variational inequalities for hyperbolic systems	35Pxx	Spectral theory and eigenvalue prob- lems [See also 47Axx, 47Bxx, 47F05]
	[See also 35R35, 49J40]	35P05	General topics in linear spectral theory
35L90	Abstract hyperbolic equations	35P10	Completeness of eigenfunctions, eigen-
35L99	None of the above, but in this section		function expansions
		35P15	Estimation of eigenvalues, upper and lower bounds
	Equations and systems of special type (mixed, composite, etc.)	35P20	Asymptotic distribution of eigenvalues and eigenfunctions
	Equations of mixed type	35P25	Scattering theory [See also 47A40]
	Initial value problems for equations of mixed type		Nonlinear eigenvalue problems, nonlinear spectral theory
35M12	Boundary value problems for equations of mixed type	35P99	None of the above, but in this section
35M13	Initial-boundary value problems for equations of mixed type	35Qxx	Equations of mathematical physics and
35M30	Systems of mixed type		other areas of application [See also 35J05, 35J10, 35K05, 35L05]
	Initial value problems for systems	35005	Euler-Poisson-Darboux equations
	of mixed type		Riemann-Hilbert problems
35M32	Boundary value problems for systems	30 Q 10	[See also 30E25, 31A25, 31B20]
	of mixed type	35Q20	Boltzmann equations

35Q30 Navier-Stokes equations 35Q99 None of the above, but in this section [See also 76D05, 76D07, 76N10] 35Q31 Euler equations 35Rxx Miscellaneous topics (For equations on [See also 76D05, 76D07, 76N10] manifolds, see 58Jxx; for manifolds 35Q35 PDEs in connection with fluid mechanof solutions, see 58Bxx; for stochastic PDE, see also 60H15) 35Q40 PDEs in connection with quantum me-35R01 Partial differential equations on manifolds [See also 32Wxx, 53Cxx, 58Jxx] 35Q41 Time-dependent Schrödinger equations, 35R02 Partial differential equations on graphs Dirac equations and networks (ramified or polygonal 35Q51 Soliton-like equations [See also 37K40] spaces) 35Q53 KdV-like equations (Korteweg-de Vries) 35R03 Partial differential equations on Heisen-[See also 37K10] berg groups, Lie groups, Carnot groups, 35Q55 NLS-like equations (nonlinear Schrödinger) [See also 37K10] 35R05 Partial differential equations with discontinuous coefficients or data 35Q56 Ginzburg-Landau equations 35R06 Partial differential equations with mea-35Q60 PDEs in connection with optics and electromagnetic theory 35R09 Integro-partial differential equations 35Q61 Maxwell equations [See also 45Kxx] 35Q62 PDEs in connection with statistics 35R10 Partial functional-differential equations 35O68 PDEs in connection with 35R11 Fractional partial differential equations computer science 35R12 Impulsive partial differential equations 35Q70 PDEs in connection with mechanics of 35R13 Fuzzy partial differential equations particles and systems 35R15 Partial differential equations on infinite-35O74 PDEs in connection with mechanics of dimensional (e.g. function) spaces deformable solids (= PDE in infinitely many variables) 35Q75 PDEs in connection with relativity and [See also 46Gxx, 58D25] gravitational theory 35R20 Partial operator-differential equations 35Q76 Einstein equations (i.e., PDE on finite-dimensional spaces 35Q79 PDEs in connection with classical therfor abstract space valued functions) modynamics and heat transfer [See also 34Gxx, 47A50, 47D03, 47D06, 35Q82 PDEs in connection with statistical me-47D09, 47H20, 47Jxx] chanics 35R25 Improperly posed problems 35Q83 Vlasov-like equations 35R30 Inverse problems 35Q84 Fokker-Planck equations 35R35 Free boundary problems 35Q85 PDEs in connection with astronomy and 35R37 Moving boundary problems astrophysics 35R45 Partial differential inequalities 35Q86 PDEs in connection with geophysics 35R50 Partial differential equations of infinite 35Q90 PDEs in connection with mathematical order programming 35R60 Partial differential equations with ran-35Q91 PDEs in connection with game theory, domness, stochastic partial differential economics, social and behavioral sciequations [See also 60H15] ences 35R70 Partial differential equations with multi-35Q92 PDEs in connection with biology and valued right-hand sides other natural sciences 35R99 None of the above, but in this section 35Q93 PDEs in connection with control and optimization

35Q94 PDEs in connection with information

and communication

35Sxx	Pseudodifferential operators and other generalizations of partial differential	37A35	Entropy and other invariants, isomorphism, classification
25505	operators [See also 47G30, 58J40]	37A40	Nonsingular (and infinite-measure preserving) transformations
35S05 35S10	Pseudodifferential operators Initial value problems for pseudodifferential operators	37A45	Relations with number theory and harmonic analysis [See also 11Kxx]
35S11	Initial-boundary value problems for pseudodifferential operators	37A50	Relations with probability theory and stochastic processes [See also 60Fxx and 60G10]
35S15	Boundary value problems for pseudodifferential operators	37A55	Relations with the theory of <i>C</i> *-algebras [See mainly 46L55]
35S30	Fourier integral operators	27 / 60	•
35S35	Topological aspects: intersection coho-	37 A00	Dynamical systems in statistical mechanics [See also 82Cxx]
	mology, stratified sets, etc. [See also 32C38, 32S40, 32S60, 58J15]	37A99	None of the above, but in this section
35S50	Paradifferential operators	27P.m	Tamalarian damaning [Canalar E41120]
35S99	None of the above, but in this section		Transformations and group actions with
37-XX	Dynamical systems and ergodic theory [See also 26A18, 28Dxx,	37B05	Transformations and group actions with special properties (minimality, distality proximality, etc.)
	34Cxx, 34Dxx, 35Bxx, 46Lxx, 58Jxx, 70-XX]	37B10	Symbolic dynamics [See also 37Cxx, 37Dxx]
37-00	General reference works (handbooks,	37B15	Cellular automata [See also 68Q80]
	dictionaries, bibliographies, etc.)	37B20	Notions of recurrence
37-01	Instructional exposition (textbooks, tutorial papers, etc.)	37B25	Lyapunov functions and stability; attractors, repellers
37-02	Research exposition (monographs,	37B30	Index theory, Morse-Conley indices
37-03	survey articles) Historical (must also be assigned at least	37B35	Gradient-like and recurrent behavior isolated (locally maximal) invariant sets
	one classification number from Section	37B40	Topological entropy
27.04	01)	37B45	Continua theory in dynamics
37-04	Explicit machine computation and programs (not the theory of computation or programming)	37B50	Multi-dimensional shifts of finite type tiling dynamics
37-06	Proceedings, conferences, collections,	37B55	Nonautonomous dynamical systems
	etc.	37B99	
	Ergodic theory [See also 28Dxx]	37Cvv	Smooth dynamical systems, ganara
	Measure-preserving transformations	37 CXX	Smooth dynamical systems: general theory [See also 34Cxx, 34Dxx]
37A10	One-parameter continuous families of measure-preserving transformations		Smooth mappings and diffeomorphisms
37A15	General groups of measure-preserving transformations [See mainly 22Fxx]		Vector fields, flows, ordinary differential equations
37A17	Homogeneous flows [See also 22Fxx]	37C15	Topological and differentiable equiv-
	Orbit equivalence, cocycles, ergodic equivalence relations	27/20	alence, conjugacy, invariants, moduli classification
37A25	Ergodicity, mixing, rates of mixing		Generic properties, structural stability
	Ergodic theorems, spectral theory,	3/C23	Fixed points, periodic points, fixed-poin index theory
	Markov operators (For operator ergodic theory, see mainly 47A35)		Periodic orbits of vector fields and flows
	areory, occurring training	27C20	Uamadinia and hatavadinia arbita

37C30	Zeta functions, (Ruelle-Frobenius) trans-		Maps of the circle
	fer operators, and other functional analytic techniques in dynamical systems	37E15	Combinatorial dynamics (types of periodic orbits)
37C35	Orbit growth	37E20	Universality, renormalization
37C40	Smooth ergodic theory, invariant mea-		[See also 37F25]
	sures [See also 37Dxx]	37E25	Maps of trees and graphs
	Dimension theory of dynamical systems	37E30	Homeomorphisms and diffeomor-
37C50	Approximate trajectories		phisms of planes and surfaces
27055	(pseudotrajectories, shadowing, etc.)		Flows on surfaces
3/C55	Periodic and quasiperiodic flows and diffeomorphisms	37E40	Twist maps
37C60			Rotation numbers and vectors
37 C00	Nonautonomous smooth dynamical systems [See also 37B55]	37E99	None of the above, but in this section
37C65	Monotone flows	37Fxx	Complex dynamical systems
37C70	Attractors and repellers, topological	0.1701	[See also 30D05, 32H50]
27075	structure	37F05	Relations and correspondences
	Stability theory	37F10	Polynomials; rational maps; entire and
	Symmetries, equivariant dynamical systems		meromorphic functions [See also 32A10, 32A20, 32H02, 32H04]
37C85	Dynamics of group actions other than Z and R , and foliations [See mainly 22Fxx, and also 57R30, 57Sxx]	37F15	Expanding maps; hyperbolicity; structural stability
37C99	None of the above, but in this section	37F20	Combinatorics and topology
		37F25	Renormalization
37Dxx	Dynamical systems with hyperbolic behavior	37F30	Quasiconformal methods and Teichmüller theory; Fuchsian and Kleinian
37D05	Hyperbolic orbits and sets		groups as dynamical systems
	Invariant manifold theory	37F35	Conformal densities and Hausdorff di-
37D15	Morse-Smale systems	37F40	mension Geometric limits
37D20	Uniformly hyperbolic systems	37F45	Holomorphic families of dynamical sys-
	(expanding, Anosov, Axiom A, etc.)	07110	tems; the Mandelbrot set; bifurcations
37D25	Nonuniformly hyperbolic systems (Lyapunov exponents, Pesin theory, etc.)	37F50	Small divisors, rotation domains and linearization; Fatou and Julia sets
37D30	Partially hyperbolic systems and dominated splittings	37F75	Holomorphic foliations and vector fields [See also 32M25, 32S65, 34Mxx]
37D35	Thermodynamic formalism, variational principles, equilibrium states	37F99	None of the above, but in this section
37D40	Dynamical systems of geometric origin and hyperbolicity (geodesic and horocy-	37Gxx	Local and nonlocal bifurcation theory [See also 34C23, 34K18]
055 45	cle flows, etc.)	37G05	Normal forms
	Strange attractors, chaotic dynamics	37G10	Bifurcations of singular points
37D50	Hyperbolic systems with singularities (billiards, etc.)	37G15	Bifurcations of limit cycles and periodic orbits
37D99	None of the above, but in this section	37G20	Hyperbolic singular points with homo- clinic trajectories
37Exx	Low-dimensional dynamical systems	37G25	Bifurcations connected with non-
37E05	Maps of the interval (piecewise continuous, continuous, smooth)	37G30	transversal intersection Infinite nonwandering sets arising in bi- furcations

27/225	Atturations and their hitematics		
	Attractors and their bifurcations	37Kxx	Infinite-dimensional Hamiltonian sys-
3/G40	Symmetries, equivariant bifurcation theory	051405	tems [See also 35Axx, 35Qxx]
37G99	None of the above, but in this section	37K05	Hamiltonian structures, symmetries, variational principles, conservation laws
		37K10	Completely integrable systems, integra-
37Hxx	Random dynamical systems [See also 15B52, 34D08, 34F05, 47B80, 70L05, 82C05, 93Exx]		bility tests, bi-Hamiltonian structures, hierarchies (KdV, KP, Toda, etc.)
37H05	Foundations, general theory of cocycles, algebraic ergodic theory [See also 37Axx]	37K15	Integration of completely integrable systems by inverse spectral and scattering methods
37H10	Generation, random and stochastic difference and differential equations [See also 34F05, 34K50, 60H10, 60H15]	37K20	Relations with algebraic geometry, complex analysis, special functions [See also 14H70]
37H15	Multiplicative ergodic theory, Lyapunov	37K25	Relations with differential geometry
	exponents [See also 34D08, 37Axx, 37Cxx, 37Dxx]	37K30	Relations with infinite-dimensional Lie algebras and other algebraic structures
37H20	Bifurcation theory [See also 37Gxx]	37K35	Lie-Bäcklund and other transformations
37H99	None of the above, but in this section	37K40	Soliton theory, asymptotic behavior of solutions
37Jxx	Finite-dimensional Hamiltonian, La-	37K45	Stability problems
	grangian, contact, and nonholonomic	37K50	Bifurcation problems
37J05	systems [See also 53Dxx, 70Fxx, 70Hxx] General theory, relations with symplec-	37K55	Perturbations, KAM for infinite-dimensional systems
-	tic geometry and topology	37K60	Lattice dynamics [See also 37L60]
37J10	Symplectic mappings, fixed points		Hamiltonian systems on groups of dif-
37J15	Symmetries, invariants, invariant manifolds, momentum maps, reduction [See		feomorphisms and on manifolds of mappings and metrics
	also 53D20]	37K99	None of the above, but in this section
37J20	Bifurcation problems		
37J25	Stability problems	37Lxx	Infinite-dimensional dissipative dyna-
37J30	Obstructions to integrability (nonintegrability criteria)	37L05	mical systems [See also 35Bxx, 35Qxx] General theory, nonlinear semigroups,
37J35	Completely integrable systems, topolog-	37 L 03	evolution equations
·	ical structure of phase space, integration methods	37L10	Normal forms, center manifold theory, bifurcation theory
37J40	Perturbations, normal forms, small divisors, KAM theory, Arnol'd diffusion		Stability problems
37J45	Periodic, homoclinic and heteroclinic	37L20	Symmetries
·	orbits; variational methods, degree- theoretic methods	37L25	Inertial manifolds and other invariant attracting sets
37J50	Action-minimizing orbits and measures	37L30	Attractors and their dimensions, Lya-
37J55	Contact systems [See also 53D10]		punov exponents
37J60	Nonholonomic dynamical systems [See	37L40	Invariant measures
	also 70F25]		Hyperbolicity; Lyapunov functions
37J99	None of the above, but in this section	37L50	Noncompact semigroups; dispersive equations; perturbations of Hamiltonian

systems

37L55	Infinite-dimensional random dynamical	37P15	Global ground fields
	systems; stochastic equations [See also		Non-Archimedean local ground fields
	35R60, 60H10, 60H15]	37P25	Finite ground fields
	Lattice dynamics [See also 37K60]	37P30	Height functions; Green functions; in-
37L65	Special approximation methods (nonlinear Galerkin, etc.)		variant measures [See also 11G50, 14G40]
37L99	None of the above, but in this section	37P35	Arithmetic properties of periodic points
		37P40	Non-Archimedean Fatou and Julia sets
37Mxx	Approximation methods and numer-	37P45	Families and moduli spaces
	ical treatment of dynamical systems	37P50	Dynamical systems on Berkovich spaces
271/105	[See also 65Pxx] Simulation	37P55	Arithmetic dynamics on general alge-
		2 =D00	braic varieties
	Time series analysis	37P99	None of the above, but in this section
	Symplectic integrators Computational methods for hituration	39-XX	Difference and functional
3710120	Computational methods for bifurcation problems		equations
37M25	Computational methods for ergodic the-	39-00	General reference works (handbooks,
	ory (approximation of invariant mea-	39-01	dictionaries, bibliographies, etc.)
	sures, computation of Lyapunov exponents, entropy)	39-01	Instructional exposition (textbooks, tutorial papers, etc.)
37M99	None of the above, but in this section	39-02	Research exposition (monographs,
	Twole of the above, but in this section		survey articles)
	Applications	39-03	Historical (must also be assigned at least one classification number from Section
37N05	Dynamical systems in classical and ce-		01)
	lestial mechanics [See mainly 70Fxx, 70Hxx, 70Kxx]	39-04	Explicit machine computation and pro-
37NI10	Dynamical systems in fluid mechan-		grams (not the theory of computation or
371110	ics, oceanography and meteorology [See		programming)
	mainly 76-XX, especially 76D05, 76F20,	39-06	Proceedings, conferences, collections,
	86A05, 86A10]		etc.
37N15	Dynamical systems in solid mechanics	39Axx	Difference equations
	[See mainly 74Hxx]		(For dynamical systems, see 37-XX; for
37N20	Dynamical systems in other branches		dynamic equations on time scales, see
	of physics (quantum mechanics, general relativity, laser physics)	30 4 05	34N05) General theory
37NI25	Dynamical systems in biology		Linear equations
371123	[See mainly 92-XX, but also 91-XX]		Difference equations, additive
37N30	Dynamical systems in numerical analy-		Discrete version of topics in analysis
	sis		Difference equations, scaling
37N35	Dynamical systems in control	071110	(q-differences) [See also 33Dxx]
37N40	Dynamical systems in optimization and	39A14	Partial difference equations
27N 100	economics		Multiplicative and other generalized dif-
37N99	None of the above, but in this section		ference equations, e.g. of Lyness type
27D	Authoritican Joseph Audit	39A21	Oscillation theory
5/PXX	Arithmetic and non-Archimedean dynamical systems [See also 11S82,	39A22	Growth, boundedness, comparison
	37A45]	•0	of solutions
37P05	Polynomial and rational maps		Periodic solutions
37P10	Analytic and meromorphic maps	39A24	Almost periodic solutions

	Bifurcation theory	40Axx	Convergence and divergence of infinite
	Stability theory		limiting processes
	Complex (chaotic) behavior of solutions	40A05	Convergence and divergence of series
	Equations in the complex domain	10 1 10	and sequences
	Stochastic difference equations	40A10	Convergence and divergence of integrals
	Applications	40 A 1 E	grals
	Difference operators [See also 47B39] None of the above, but in this section	40A15	Convergence and divergence of continued fractions [See also 30B70]
		40A20	Convergence and divergence of infinite
39Bxx	Functional equations and inequalities [See also 30D05]	40A25	products Approximation to limiting values (sum-
39B05	General		mation of series, etc.) (For the Euler-
	Iteration theory, iterative and compos-		Maclaurin summation formula, see 65B15)
	ite equations [See also 26A18, 30D05, 37-XX]	40A30	Convergence and divergence of series and sequences of functions
39B22	Equations for real functions [See also 26A51, 26B25]	40A35	Ideal and statistical convergence
39B32	Equations for complex functions	10.1.00	[See also 40G15]
30R42	[See also 30D05]	40A99	None of the above, but in this section
39D 4 Z	Matrix and operator equations [See also 47]xx]	40Bxx	Multiple sequences and series
39B52	Equations for functions with more gen-		Multiple sequences and series (should
	eral domains and/or ranges		also be assigned at least one other classi-
39B55	Orthogonal additivity and other condi-		fication number in this section)
	tional equations	40B99	None of the above, but in this section
39B62	Functional inequalities, including sub-		
	additivity, convexity, etc.		General summability methods
20D72	[See also 26A51, 26B25, 26Dxx]		Matrix methods
39B72	Systems of functional equations and inequalities		Integral methods
39B82	Stability, separation, extension, and re-	40C15	Function-theoretic methods (including
37 D 02	lated topics [See also 46A22]		power series methods and semicontin- uous methods)
39B99	None of the above, but in this section	40C99	None of the above, but in this section
40-XX	(Sequences, series, summability		
40-00	General reference works (handbooks,		Direct theorems on summability
	dictionaries, bibliographies, etc.)		General theorems
40-01	Instructional exposition		Structure of summability fields
	(textbooks, tutorial papers, etc.)	40D10	Tauberian constants and oscillation lim-
40-02	Research exposition (monographs, survey articles)	40D15	its Convergence factors and summability
40-03	Historical (must also be assigned at least	40D20	factors
	one classification number from Section 01)		Summability and bounded fields of methods
40-04	Explicit machine computation and pro-		Inclusion and equivalence theorems
10 01	grams (not the theory of computation or programming)	40D99	None of the above, but in this section
40-06	Proceedings, conferences, collections,	40Exx	Inversion theorems
10 00	etc.	40E05	Tauberian theorems, general

40E10	Growth estimates	41-02	Research exposition (monographs,
40E15	Lacunary inversion theorems		survey articles)
40E20	Tauberian constants	41-03	Historical (must also be assigned at leas
40E99	None of the above, but in this section		one classification number from Section
		41-04	01) Explicit machine computation and pro-
40Fxx	Absolute and strong summability (should also be assigned at least one other classification number in Section	11 01	grams (not the theory of computation of programming)
40F05	40)	41-06	Proceedings, conferences, collections, etc.
401'05	Absolute and strong summability (should also be assigned at least one other classification number in Section 40)	41Axx	Approximations and expansions (For all approximation theory in the complex domain, see 30E05 and 30E10; for
40F99	None of the above, but in this section		all trigonometric approximation and interpolation, see 42A10 and 42A15; for
40Gxx	Special methods of summability	41 A OF	numerical approximation, see 65Dxx)
40G05	Cesàro, Euler, Nörlund and Hausdorff methods		Interpolation [See also 42A15 and 65D05]
40G10	Abel, Borel and power series methods	41A10	Approximation by polynomials (For ap
40G15	Summability methods using statistical convergence [See also 40A35]		proximation by trigonometric polynomials, see 42A10)
40G99	None of the above, but in this section		Spline approximation
	,	41A17	Inequalities in approximation
40Hxx	Functional analytic methods in summability		(Bernstein, Jackson, Nikol'skiĭ-type in equalities)
40H05	Functional analytic methods in summa-		Approximation by rational functions
	bility		Padé approximation
40H99	None of the above, but in this section		Rate of convergence, degree of approximation
40Jxx	Summability in abstract structures [See		Inverse theorems
10,111	also 43A55, 46A35, 46B15]		Simultaneous approximation
40J05	Summability in abstract structures [See		Approximation with constraints
	also 43A55, 46A35, 46B15] (should also be assigned at least one other classifica-		Approximation by other special function classes
	tion number in this section)	41A35	Approximation by operators
40J99	None of the above, but in this section	41 A 26	(in particular, by integral operators)
41-XX	Approximations and expansions		Approximation by positive operators Saturation
	(For all approximation theory in		Best constants
	the complex domain, see 30E05		
	and 30E10; for all trigonomet-	41743	Approximation by arbitrary linear expressions
	ric approximation and interpola- tion, see 42A10 and 42A15; for	41A46	Approximation by arbitrary nonlinear expressions; widths and entropy
	numerical approximation, see 65Dxx)	41A50	Best approximation, Chebyshev systems
41.00			Uniqueness of best approximation
41-00	General reference works (handbooks,		Approximate quadratures
41-01	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.)		Series expansions (e.g. Taylor, Lidstone series, but not Fourier series)

- 41A60 Asymptotic approximations, asymptotic expansions (steepest descent, etc.) [See also 30E15]
- 41A63 Multidimensional problems (should also be assigned at least one other classification number in this section)
- 41A65 Abstract approximation theory (approximation in normed linear spaces and other abstract spaces)
- 41A80 Remainders in approximation formulas
- 41A99 None of the above, but in this section

42-XX Harmonic analysis on Euclidean spaces

- 42-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 42-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 42-02 Research exposition (monographs, survey articles)
- 42-03 Historical (must also be assigned at least one classification number from Section 01)
- 42-04 Explicit machine computation and programs (not the theory of computation or programming)
- 42-06 Proceedings, conferences, collections, etc.

42Axx Harmonic analysis in one variable

- 42A05 Trigonometric polynomials, inequalities, extremal problems
- 42A10 Trigonometric approximation
- 42A15 Trigonometric interpolation
- 42A16 Fourier coefficients, Fourier series of functions with special properties, special Fourier series (For automorphic theory, see mainly 11F30)
- 42A20 Convergence and absolute convergence of Fourier and trigonometric series
- 42A24 Summability and absolute summability of Fourier and trigonometric series
- 42A32 Trigonometric series of special types (positive coefficients, monotonic coefficients, etc.)
- 42A38 Fourier and Fourier-Stieltjes transforms and other transforms of Fourier type
- 42A45 Multipliers
- 42A50 Conjugate functions, conjugate series, singular integrals

- 42A55 Lacunary series of trigonometric and other functions; Riesz products
- 42A61 Probabilistic methods
- 42A63 Uniqueness of trigonometric expansions, uniqueness of Fourier expansions, Riemann theory, localization
- 42A65 Completeness of sets of functions
- 42A70 Trigonometric moment problems
- 42A75 Classical almost periodic functions, mean periodic functions [See also 43A60]
- 42A82 Positive definite functions
- 42A85 Convolution, factorization
- 42A99 None of the above, but in this section

42Bxx Harmonic analysis in several variables (For automorphic theory, see mainly 11F30)

- 42B05 Fourier series and coefficients
- 42B08 Summability
- 42B10 Fourier and Fourier-Stieltjes transforms and other transforms of Fourier type
- 42B15 Multipliers
- 42B20 Singular and oscillatory integrals (Calderón-Zygmund, etc.)
- 42B25 Maximal functions, Littlewood-Paley theory
- 42B30 H^p -spaces
- 42B35 Function spaces arising in harmonic analysis
- 42B37 Harmonic analysis and PDE [See also 35-XX]
- 42B99 None of the above, but in this section

42Cxx Nontrigonometric harmonic analysis

- 42C05 Orthogonal functions and polynomials, general theory [See also 33C45, 33C50, 33D45]
- 42C10 Fourier series in special orthogonal functions (Legendre polynomials, Walsh functions, etc.)
- 42C15 General harmonic expansions, frames
- 42C20 Other transformations of harmonic type
- 42C25 Uniqueness and localization for orthogonal series
- 42C30 Completeness of sets of functions
- 42C40 Wavelets and other special systems
- 42C99 None of the above, but in this section

43-XX Abstract harmonic analysis
(For other analysis on topologi-
cal and Lie groups, see 22Exx)

- 43-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 43-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 43-02 Research exposition (monographs, survey articles)
- 43-03 Historical (must also be assigned at least one classification number from Section 01)
- 43-04 Explicit machine computation and programs (not the theory of computation or programming)
- 43-06 Proceedings, conferences, collections, etc.

43Axx Abstract harmonic analysis (For other analysis on topological and Lie groups, see 22Exx)

- 43A05 Measures on groups and semigroups, etc.
- 43A07 Means on groups, semigroups, etc.; amenable groups
- 43A10 Measure algebras on groups, semigroups, etc.
- 43A15 L^p -spaces and other function spaces on groups, semigroups, etc.
- 43A17 Analysis on ordered groups, H^p -theory
- 43A20 L^1 -algebras on groups, semigroups, etc.
- 43A22 Homomorphisms and multipliers of function spaces on groups, semigroups, etc.
- 43A25 Fourier and Fourier-Stieltjes transforms on locally compact and other abelian groups
- 43A30 Fourier and Fourier-Stieltjes transforms on nonabelian groups and on semi-groups, etc.
- 43A32 Other transforms and operators of Fourier type
- 43A35 Positive definite functions on groups, semigroups, etc.
- 43A40 Character groups and dual objects
- 43A45 Spectral synthesis on groups, semigroups, etc.
- 43A46 Special sets (thin sets, Kronecker sets, Helson sets, Ditkin sets, Sidon sets, etc.)

- 43A50 Convergence of Fourier series and of inverse transforms
- 43A55 Summability methods on groups, semigroups, etc. [See also 40J05]
- 43A60 Almost periodic functions on groups and semigroups and their generalizations (recurrent functions, distal functions, etc.); almost automorphic functions
- 43A62 Hypergroups
- 43A65 Representations of groups, semigroups, etc. [See also 22A10, 22A20, 22Dxx, 22E45]
- 43A70 Analysis on specific locally compact and other abelian groups [See also 11R56, 22B05]
- 43A75 Analysis on specific compact groups
- 43A77 Analysis on general compact groups
- 43A80 Analysis on other specific Lie groups [See also 22Exx]
- 43A85 Analysis on homogeneous spaces
- 43A90 Spherical functions [See also 22E45, 22E46, 33C55]
- 43A95 Categorical methods [See also 46Mxx]
- 43A99 None of the above, but in this section

44-XX Integral transforms, operational calculus (For fractional derivatives and integrals, see 26A33. For Fourier transforms, see 42A38, 42B10. For integral transforms in distribution spaces, see 46F12. For numerical methods, see 65R10)

- 44-00 General reference works (handbooks, dictionaries, bibliographies, etc.)
- 44-01 Instructional exposition (textbooks, tutorial papers, etc.)
- 44-02 Research exposition (monographs, survey articles)
- 44-03 Historical (must also be assigned at least one classification number from Section 01)
- 44-04 Explicit machine computation and programs (not the theory of computation or programming)
- 44-06 Proceedings, conferences, collections, etc.

58 Integral equations

44Axx	Integral transforms, operational calculus (For fractional derivatives and integrals, see 26A33. For Fourier trans-		Eigenvalue problems [See also 34Lxx, 35Pxx, 45P05, 47A75] Eigenvalue problems
	forms, see 42A38, 42B10. For inte-	43003	[See also 34Lxx, 35Pxx, 45P05, 47A75]
	gral transforms in distribution spaces, see 46F12. For numerical methods, see	45C99	None of the above, but in this section
	65R10) General transforms [See also 42A38]	45Dxx	Volterra integral equations [See also 34A12]
	Laplace transform	45D05	Volterra integral equations
	Radon transform [See also 92C55]		[See also 34A12]
44A15	Special transforms (Legendre, Hilbert, etc.)	45D99	None of the above, but in this section
44A20	Transforms of special functions	45Exx	Singular integral equations
	Multiple transforms		[See also 30E20, 30E25, 44A15, 44A35]
	Convolution	45E05	Integral equations with kernels of
44A40	Calculus of Mikusiński and other oper-		Cauchy type [See also 35J15]
	ational calculi Classical operational calculus	45E10	Integral equations of the convolution type
	Discrete operational calculus		(Abel, Picard, Toeplitz and Wiener-Hopf
	Moment problems		type) [See also 47B35]
44A99	None of the above, but in this section	45E99	None of the above, but in this section
45-XX	Integral equations	455	C(
45-00	General reference works (handbooks, dictionaries, bibliographies, etc.)	45F05	Systems of linear integral equations Systems of nonsingular linear integral equations
45-01	Instructional exposition (textbooks, tutorial papers, etc.)	45F10	Dual, triple, etc., integral and series equations
45-02	Research exposition (monographs, survey articles)	45F15	Systems of singular linear integral equations
45-03	Historical (must also be assigned at least one classification number from Section 01)	45F99	None of the above, but in this section
45-04	Explicit machine computation and programs (not the theory of computation or		Nonlinear integral equations [See also 47H30, 47Jxx]
	programming)	45G05	Singular nonlinear integral equations
45-06	Proceedings, conferences, collections,		Other nonlinear integral equations
	etc.		Systems of nonlinear integral equations
45Axx	Linear integral equations	45G99	None of the above, but in this section
45A05	Linear integral equations	4=77	
45A99	None of the above, but in this section		Miscellaneous special kernels [See also 44A15]
	Fredholm integral equations	45H05	Miscellaneous special kernels [See also 44A15]
	Fredholm integral equations	45H99	None of the above, but in this section
43D99	None of the above, but in this section		
		45Jxx	Integro-ordinary differential equations [See also 34K05, 34K30, 47G20]
		45J05	Integro-ordinary differential equations [See also 34K05, 34K30, 47G20]

45J99 	None of the above, but in this section	46-XX	(Functional analysis (For man- ifolds modeled on topological
45Kxx	Integro-partial differential equations [See also 34K30, 35R09, 35R10, 47G20]		linear spaces, see 57Nxx, 58Bxx)
45K05	Integro-partial differential equations [See also 34K30, 35R09, 35R10, 47G20]	46-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
45K99	None of the above, but in this section	46-01	Instructional exposition (textbooks, tutorial papers, etc.)
45Lxx	Theoretical approximation of solutions (For numerical analysis, see 65Rxx)	46-02	Research exposition (monographs, survey articles)
45L05	Theoretical approximation of solutions (For numerical analysis, see 65Rxx)	46-03	Historical (must also be assigned at least one classification number from Section
45L99	None of the above, but in this section	46-04	O1) Explicit machine computation and programs (not the theory of computation or
45Mxx	Qualitative behavior		programming)
	Asymptotics	46-06	Proceedings, conferences, collections,
	Stability theory	40-00	etc.
	Periodic solutions	16 1 200	
45M20	Positive solutions	40AXX	Topological linear spaces and related structures (For function spaces, see
	None of the above, but in this section		46Exx)
		46A03	General theory of locally convex spaces
45Nxx	Abstract integral equations, integral equations in abstract spaces		Locally convex Fréchet spaces and (DF)- spaces
45N05	Abstract integral equations,	46A08	Barrelled spaces, bornological spaces
	integral equations in abstract spaces		Spaces determined by compactness or
45N99	None of the above, but in this section		summability properties (nuclear spaces, Schwartz spaces, Montel spaces, etc.)
45Pxx	Integral operators [See also 47B38, 47G10]	46A13	Spaces defined by inductive or projective limits (LB, LF, etc.) [See also 46M40]
45P05	Integral operators [See also 47B38, 47G10]	46A16	Not locally convex spaces (metriz- able topological linear spaces, locally
45P99	None of the above, but in this section		bounded spaces, quasi-Banach spaces, etc.)
45Qxx	Inverse problems	46A17	Bornologies and related structures;
	Inverse problems		Mackey convergence, etc.
45Q99	None of the above, but in this section	46A19	Other "topological" linear spaces (convergence spaces, ranked spaces, spaces with a metric taking values in an ordered
45Rxx	Random integral equations [See also 60H20]	46 A 2 0	structure more general than R , etc.)
45R05	Random integral equations		Duality theory Theorems of Hahn-Banach type; exten-
	[See also 60H20]	101122	sion and lifting of functionals and oper-
45R99	None of the above, but in this section		ators [See also 46M10]
		46A25	Reflexivity and semi-reflexivity [See also 46B10]
		46A30	Open mapping and closed graph theorems; completeness (including B -, B_r -completeness)

- 46A32 Spaces of linear operators; topological tensor products; approximation properties [See also 46B28, 46M05, 47L05, 47L20]
- 46A35 Summability and bases [See also 46B15]
- 46A40 Ordered topological linear spaces, vector lattices [See also 06F20, 46B40, 46B42]
- 46A45 Sequence spaces (including Köthe sequence spaces) [See also 46B45]
- 46A50 Compactness in topological linear spaces; angelic spaces, etc.
- 46A55 Convex sets in topological linear spaces; Choquet theory [See also 52A07]
- 46A61 Graded Fréchet spaces and tame operators
- 46A63 Topological invariants ((DN), (Ω), etc.)
- 46A70 Saks spaces and their duals (strict topologies, mixed topologies, two-norm spaces, co-Saks spaces, etc.)
- 46A80 Modular spaces
- 46A99 None of the above, but in this section

46Bxx Normed linear spaces and Banach spaces; Banach lattices (For function spaces, see 46Exx)

- 46B03 Isomorphic theory (including renorming) of Banach spaces
- 46B04 Isometric theory of Banach spaces
- 46B06 Asymptotic theory of Banach spaces [See also 52A23]
- 46B07 Local theory of Banach spaces
- 46B08 Ultraproduct techniques in Banach space theory [See also 46M07]
- 46B09 Probabilistic methods in Banach space theory [See also 60Bxx]
- 46B10 Duality and reflexivity [See also 46A25]
- 46B15 Summability and bases [See also 46A35]
- 46B20 Geometry and structure of normed linear spaces
- 46B22 Radon-Nikodým, Kreĭn-Milman and related properties [See also 46G10]
- 46B25 Classical Banach spaces in the general theory
- 46B26 Nonseparable Banach spaces
- 46B28 Spaces of operators; tensor products; approximation properties [See also 46A32, 46M05, 47L05, 47L20]
- 46B40 Ordered normed spaces [See also 46A40, 46B42]

46B42 Banach lattices [See also 46A40, 46B40]

- 46B45 Banach sequence spaces [See also 46A45]
- 46B50 Compactness in Banach (or normed) spaces
- 46B70 Interpolation between normed linear spaces [See also 46M35]
- 46B80 Nonlinear classification of Banach spaces; nonlinear quotients
- 46B85 Embeddings of discrete metric spaces into Banach spaces; applications in topology and computer science [See also 05C12, 68Rxx]
- 46B99 None of the above, but in this section

46Cxx Inner product spaces and their generalizations, Hilbert spaces (For function spaces, see 46Exx)

- 46C05 Hilbert and pre-Hilbert spaces: geometry and topology (including spaces with semidefinite inner product)
- 46C07 Hilbert subspaces (= operator ranges); complementation (Aronszajn, de Branges, etc.) [See also 46B70, 46M35]
- 46C15 Characterizations of Hilbert spaces
- 46C20 Spaces with indefinite inner product (Kreĭn spaces, Pontryagin spaces, etc.) [See also 47B50]
- 46C50 Generalizations of inner products (semiinner products, partial inner products, etc.)
- 46C99 None of the above, but in this section

46Exx Linear function spaces and their duals [See also 30H05, 32A38, 46F05] (For function algebras, see 46J10)

- 46E05 Lattices of continuous, differentiable or analytic functions
- 46E10 Topological linear spaces of continuous, differentiable or analytic functions
- 46E15 Banach spaces of continuous, differentiable or analytic functions
- 46E20 Hilbert spaces of continuous, differentiable or analytic functions
- 46E22 Hilbert spaces with reproducing kernels (= [proper] functional Hilbert spaces, including de Branges-Rovnyak and other structured spaces) [See also 47B32]

46E25	Rings and algebras of continuous, differentiable or analytic functions (For Banach functions algebras and 46110, 46115)		Functional analytic lifting theory [See also 28A51]
46E27	nach function algebras, see 46J10, 46J15) Spaces of measures [See also 28A33,	46G20	Infinite-dimensional holomorphy [See also 32-XX, 46E50, 46T25, 58B12, 58C10]
46E30	46Gxx] Spaces of measurable functions	46G25	(Spaces of) multilinear mappings, polynomials [See also 46E50, 46G20, 47H60]
	$(L^p$ -spaces, Orlicz spaces, Köthe function spaces, Lorentz spaces, rearrangement	46G99	None of the above, but in this section
	invariant spaces, ideal spaces, etc.)	16Hvv	Tanalogical algebras narmed rings and
46E35	Sobolev spaces and other spaces of "smooth" functions, embedding theorems, trace theorems	4011XX	Topological algebras, normed rings and algebras, Banach algebras (For group algebras, convolution algebras and measure algebras, see 43A10, 43A20)
46E39	Sobolev (and similar kinds of) spaces of	46H05	General theory of topological algebras
46E40	functions of discrete variables	46H10	Ideals and subalgebras
46E40	Spaces of vector- and operator-valued functions	46H15	Representations of topological algebras
46E50	Spaces of differentiable or holomorphic functions on infinite-dimensional spaces	46H20	Structure, classification of topological algebras
46E99	[See also 46G20, 46G25, 47H60] None of the above, but in this section	46H25	Normed modules and Banach modules, topological modules (if not placed in 13-XX or 16-XX)
46Fxx	Distributions, generalized functions, distribution spaces [See also 46T30]	46H30	Functional calculus in topological algebras [See also 47A60]
46F05	Topological linear spaces of test functions, distributions and ultradistribu-	46H35	Topological algebras of operators [See mainly 47Lxx]
	tions [See also 46E10, 46E35]	46H40	Automatic continuity
46F10	Operations with distributions	46H70	Nonassociative topological algebras
46F12	Integral transforms in distribution		[See also 46K70, 46L70]
46F15	spaces [See also 42-XX, 44-XX]	46H99	None of the above, but in this section
40113	Hyperfunctions, analytic functionals [See also 32A25, 32A45, 32C35, 58J15]	46Jxx	Commutative Banach algebras and
46F20	Distributions and ultradistributions as	,	commutative topological algebras
	boundary values of analytic functions		[See also 46E25]
	[See also 30D40, 30E25, 32A40]	46J05	General theory of commutative topolog-
46F25	Distributions on infinite-dimensional	47110	ical algebras
46500	spaces [See also 58C35]	46J10	Banach algebras of continuous functions, function algebras [See also 46E25]
46F30	Generalized functions for nonlinear analysis (Rosinger, Colombeau, non-	46J15	Banach algebras of differentiable or an-
	standard, etc.)	40)13	alytic functions, H^p -spaces [See also
46F99	None of the above, but in this section	46120	30H10, 32A35, 32A37, 32A38, 42B30]
460		46J20	Ideals, maximal ideals, boundaries
46Gxx	Measures, integration, derivative, holo-	46J25	Representations of commutative topological algebras
	morphy (all involving infinite-dimensional spaces) [See also 28-XX, 46Txx]	46J30	Subalgebras
46G05	Derivatives [See also 46T20, 58C20,	46J40	Structure, classification of commutative
16010	58C25]		topological algebras
46G10	Vector-valued measures and integration [See also 28Bxx, 46B22]	46J45 46J99	Radical Banach algebras None of the above, but in this section
46G12	Measures and integration on abstract linear spaces [See also 28C20, 46T12]	•	,

	Topological (rings and) algebras with an involution [See also 16W10]	46L80	K-theory and operator algebras (including cyclic theory) [See also 18F25, 19Kxx, 46M20, 55Rxx, 58J22]
46K05	General theory of topological algebras with involution	46L85	Noncommutative topology
46K10	Representations of topological algebras with involution	46L87	[See also 58B32, 58B34, 58J22] Noncommutative differential geometry
46K15	Hilbert algebras		[See also 58B32, 58B34, 58J22]
	Nonselfadjoint (sub)algebras in algebras with involution	46L89	based on C*-algebra theory
46K70	Nonassociative topological algebras with an involution [See also 46H70, 46L70]	46L99	[See also 58B32, 58B34, 58J22] None of the above, but in this section
46K99	None of the above, but in this section	46Mxx	Methods of category theory in functional analysis [See also 18-XX]
46Lxx	Selfadjoint operator algebras (C*-algebras, von Neumann (W*-) alge-	46M05	Tensor products [See also 46A32, 46B28, 47A80]
	bras, etc.) [See also 22D25, 47Lxx]	46M07	Ultraproducts [See also 46B08, 46S20]
	General theory of <i>C</i> *-algebras Tensor products of <i>C</i> *-algebras	46M10	Projective and injective objects [See also 46A22]
	Operator spaces and completely	46M15	Categories, functors (For <i>K</i> -theory, EXT,
TOLO7	bounded maps [See also 47L25]		etc., see 19K33, 46L80, 46M18, 46M20)
46L08	C*-modules	46M18	Homological methods (exact sequences,
	Free products of <i>C</i> *-algebras	46M20	right inverses, lifting, etc.) Methods of algebraic topology (coho-
46L10	General theory of von Neumann algebras	401 V 120	mology, sheaf and bundle theory, etc.)
46L30	States		[See also 14F05, 18Fxx, 19Kxx, 32Cxx, 32Lxx, 46L80, 46M15, 46M18, 55Rxx]
	Classifications of <i>C</i> *-algebras	46M35	Abstract interpolation of topological
	Classification of factors	101/100	vector spaces [See also 46B70]
	Subfactors and their classification	46M40	Inductive and projective limits
46L40	Automorphisms		[See also 46A13]
	Decomposition theory for <i>C</i> *-algebras	46M99	None of the above, but in this section
46L51	Noncommutative measure and integration		
46L52	Noncommutative function spaces	46Nxx	Miscellaneous applications of functional analysis [See also 47Nxx]
46L53	Noncommutative probability and statistics	46N10	Applications in optimization, convex analysis, mathematical programming,
46L54	Free probability and free operator algebras	46NI20	economics
46L55	Noncommutative dynamical systems [See also 28Dxx, 37Kxx, 37Lxx, 54H20]	461NZU	Applications to differential and integral equations
46L57	Derivations, dissipations and positive	46N30	Applications in probability theory and statistics
46T 60	semigroups in <i>C</i> *-algebras	46N40	Applications in numerical analysis
+0L00	Applications of selfadjoint operator algebras to physics [See also 46N50,	460 150	[See also 65Jxx]
	46N55, 47L90, 81T05, 82B10, 82C10]		Applications in quantum physics
46L65	Quantizations, deformations		Applications in statistical physics
	Nonassociative selfadjoint operator al-	46IN6U	Applications in biology and other sciences
	gebras [See also 46H70, 46K70]	46N99	None of the above, but in this section

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		47-06	Proceedings, conferences, collections,
46Sxx	Other (nonclassical) types of functional		etc.
4CC10	analysis [See also 47Sxx]		General theory of linear operators
46S10	Functional analysis over fields other than R or C or the quaternions; non-	47A05	General (adjoints, conjugates, products,
	Archimedean functional analysis	47 4 0 6	inverses, domains, ranges, etc.)
	[See also 12J25, 32P05]	4/A06	Linear relations (multivalued linear operators)
46S20	Nonstandard functional analysis	47407	Forms
	[See also 03H05]	477107	(bilinear, sesquilinear, multilinear)
46S30	Constructive functional analysis	47A10	Spectrum, resolvent
46S40	[See also 03F60] Fuzzy functional analysis		Local spectral properties
10010	[See also 03E72]		Numerical range, numerical radius
46S50	Functional analysis in probabilistic metric linear spaces	47A13	Several-variable operator theory (spectral, Fredholm, etc.)
46S60	Functional analysis on superspaces	47A15	Invariant subspaces [See also 47A46]
	(supermanifolds) or graded spaces [See also 58A50 and 58C50]	47A16	Cyclic vectors, hypercyclic and chaotic operators
46S99	None of the above, but in this section	47A20	Dilations, extensions, compressions
		47A25	Spectral sets
46Txx	Nonlinear functional analysis [See also 47Hxx, 47Jxx, 58Cxx, 58Dxx]	47A30	Norms (inequalities, more than one norm, etc.)
46T05	Infinite-dimensional manifolds	47A35	Ergodic theory [See also 28Dxx, 37Axx]
46T10	[See also 53Axx, 57N20, 58Bxx, 58Dxx] Manifolds of mappings	47A40	Scattering theory [See also 34L25, 35P25, 37K15, 58J50, 81Uxx]
46T12	Measure (Gaussian, cylindrical, etc.) and	47A45	Canonical models for contractions and
	integrals (Feynman, path, Fresnel, etc.) on manifolds	47 4 4 6	nonselfadjoint operators
	[See also 28Cxx, 46G12, 60-XX]	47A46	Chains (nests) of projections or of invari-
46T20	Continuous and differentiable maps		ant subspaces, integrals along chains, etc.
	[See also 46G05]	47A48	Operator colligations (= nodes), vessels,
	Holomorphic maps [See also 46G20]		linear systems, characteristic functions,
46T30	Distributions and generalized functions	45 4 50	realizations, etc.
16T00	on nonlinear spaces [See also 46Fxx]	47A50	Equations and inequalities involving linear operators, with vector unknowns
	None of the above, but in this section	47A52	Ill-posed problems, regularization [See
	Operator theory	1,7102	also 35R25, 47J06, 65F22, 65J20, 65L08,
47-00	General reference works (handbooks,		65M30, 65R30]
47-01	dictionaries, bibliographies, etc.) Instructional exposition		(Semi-) Fredholm operators; index theories [See also 58B15, 58J20]
47.02	(textbooks, tutorial papers, etc.)	47A55	Perturbation theory
47-02	Research exposition (monographs, survey articles)	47 A 56	[See also 47H14, 58J37, 70H09, 81Q15]
47-03	Historical (must also be assigned at least	4/A36	Functions whose values are linear operators (operator and matrix valued func-
2. 00	one classification number from Section		tions, etc., including analytic and mero-
	01)		morphic ones)
47-04	Explicit machine computation and pro-	47A57	Operator methods in interpolation, mo-
	grams (not the theory of computation or		ment and extension problems
	programming)	17150	[See also 30E05, 42A70, 42A82, 44A60]
		1 / A30	Operator approximation theory

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47A60	Functional calculus	47B37	Operators on special spaces (weighted
47A62	Equations involving linear operators, with operator unknowns		shifts, operators on sequence spaces, etc.)
47A63	Operator inequalities	47B38	Operators on function spaces (general)
	Operator means, shorted operators, etc.		Difference operators [See also 39A70]
	Structure theory	47B40	Spectral operators, decomposable oper-
	Quasitriangular and nonquasitriangu-		ators, well-bounded operators, etc.
	lar, quasidiagonal and nonquasidiagonal operators	47B44	Accretive operators, dissipative operators, etc.
47A67	Representation theory	47B47	Commutators, derivations, elementary
	Factorization theory (including Wiener-		operators, etc.
2,7100	Hopf and spectral factorizations)		Operators on Banach algebras
47A70	(Generalized) eigenfunction expansions;	47B49	Transformers, preservers
	rigged Hilbert spaces	4 7 DF0	(operators on spaces of operators)
47A75	Eigenvalue problems [See also 47]10, 49R05]	47B50	Operators on spaces with an indefinite metric [See also 46C50]
47A80	Tensor products of operators		Operators on ordered spaces
	[See also 46M05]	47B65	Positive operators and order-bounded
47A99	None of the above, but in this section	 -	operators
		47B80	Random operators
	Special classes of linear operators	17B00	[See also 47H40, 60H25] None of the above, but in this section
47B06	Riesz operators; eigenvalue distri-	47 D//	None of the above, but in this section
	butions; approximation numbers, <i>s</i> -numbers, Kolmogorov numbers, en-	47Cxx	Individual linear operators as elements
	tropy numbers, etc. of operators	17 0,000	of algebraic systems
47B07	Operators defined by compactness prop-	47C05	Operators in algebras
	erties	47C10	Operators in *-algebras
47B10	1 0 0 1	47C15	Operators in C*- or von Neumann alge-
	(nuclear, <i>p</i> -summing, in the Schattenvon Neumann classes, etc.)	4 7 C00	bras
	[See also 47L20]	47C99	None of the above, but in this section
47B15	Hermitian and normal operators (spec-	47Dvv	Groups and semigroups of linear
	tral measures, functional calculus, etc.)	4/033	operators, their generalizations and
47B20	Subnormal operators, hyponormal operators at a second control of the second control operators and second control operators.		applications
47B25	ators, etc.	47D03	Groups and semigroups of linear opera-
47 D23	Symmetric and selfadjoint operators (unbounded)		tors (For nonlinear operators, see 47H20; see also 20M20)
47B32	Operators in reproducing-kernel Hilbert	47D06	One-parameter semigroups and linear
	spaces (including de Branges, de Branges-Rovnyak, and other structured		evolution equations
	spaces) [See also 46E22]	45005	[See also 34G10, 34K30]
47B33	Composition operators	47D07	Markov semigroups and applications to diffusion processes
	Kernel operators		(For Markov processes, see 60Jxx)
	Toeplitz operators, Hankel operators,	47D08	Schrödinger and Feynman-Kac semi-
	Wiener-Hopf operators [See also 45P05,		groups
	47G10 for other integral operators; see	47D09	Operator sine and cosine functions and
17R26	also 32A25, 32M15]		higher-order Cauchy problems
47B36	Jacobi (tridiagonal) operators (matrices) and generalizations	47D.00	[See also 34G10]
	and percentilation	4/11/60	C-semigroups, regularized semigroups

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47D62	Integrated semigroups	47H14	Perturbations of nonlinear operators
47D99	None of the above, but in this section		[See also 47A55, 58J37, 70H09, 70K60, 81Q15]
47Exx	Ordinary differential operators [See also 34Bxx, 34Lxx]	47H20	Semigroups of nonlinear operators [See also 37L05, 47J35, 54H15, 58D07]
47E05	Ordinary differential operators [See also 34Bxx, 34Lxx] (should also be assigned	47H25	Nonlinear ergodic theorems [See also 28Dxx, 37Axx, 47A35]
47E99	at least one other classification number in section 47) None of the above, but in this section	47H30	Particular nonlinear operators (superposition, Hammerstein, Nemytskiĭ, Uryson, etc.) [See also 45Gxx, 45P05]
—	None of the above, but in this section	47H40	Random operators [See also 47B80, 60H25]
47Fxx	Partial differential operators [See also 35Pxx, 58Jxx]	47H60	Multilinear and polynomial operators [See also 46G25]
47F05	Partial differential operators [See also 35Pxx, 58Jxx] (should also be assigned	47H99	None of the above, but in this section
	at least one other classification number in section 47)	47Jxx	Equations and inequalities involving
47F99	None of the above, but in this section		nonlinear operators [See also 46Txx] (For global and geometric aspects, see 58-XX)
47Gxx	Integral, integro-differential, and pseudodifferential operators [See also 58Jxx]	47J05	Equations involving nonlinear operators (general) [See also 47H10, 47J25]
47G10	Integral operators [See also 45P05]	47J06	Nonlinear ill-posed problems [See also
	Integral operators [See also 34K30, 35R09, 35R10, 45Jxx, 45Kxx]		35R25, 47A52, 65F22, 65J20, 65L08, 65M30, 65R30]
47G30	Pseudodifferential operators [See also 35Sxx, 58Jxx]	47J07	Abstract inverse mapping and implicit function theorems [See also 46T20 and 58C15]
47G40	Potential operators [See also 31-XX]	47J10	Nonlinear spectral theory, nonlinear
47G99	None of the above, but in this section)	eigenvalue problems [See also 49R05]
47Hyy	Nonlinear operators and their proper-	47J15	Abstract bifurcation theory
4/11//	ties (For global and geometric aspects,	47J20	[See also 34C23, 37Gxx, 58E07, 58E09] Variational and other types of inequali-
47H04	see 49J53, 58-XX, especially 58Cxx) Set-valued operators	47 J20	ties involving nonlinear operators (general) [See also 49J40]
	[See also 28B20, 54C60, 58C06]	47J22	Variational and other types of inclusions
	Monotone operators and generalizations		[See also 34A60, 49J21, 49K21]
47H06	Accretive operators, dissipative opera-	47J25	Iterative procedures [See also 65J15]
471107	tors, etc.	47J30	Variational methods [See also 58Exx]
4/HU/	Monotone and positive operators on or- dered Banach spaces or other ordered topological vector spaces	47J35	Nonlinear evolution equations [See also 34G20, 35K90, 35L90, 35Qxx, 35R20, 37Kxx, 37Lxx, 47H20, 58D25]
47H08	Measures of noncompactness and con- densing mappings, <i>K</i> -set contractions,	47J40	Equations with hysteresis operators [See also 34C55, 74N30]
47H09	etc. Contraction-type mappings, nonexpansive mappings. 4-proper mappings at	47J99 	None of the above, but in this section
47H10	sive mappings, <i>A</i> -proper mappings, etc. Fixed-point theorems [See also 37C25, 54H25, 55M20, 58C30]	47Lxx	Linear spaces and algebras of operators [See also 46Lxx]
47H11	Degree theory [See also 55M25, 58C30]	47L05	Linear spaces of operators

[See also 46A32 and 46B28]

47L07	Convex sets and cones of operators [See also 46A55]
47L10	Algebras of operators on Banach spaces and other topological linear spaces
47L15	Operator algebras with symbol structure
47L20	Operator ideals [See also 47B10]
47L22	Ideals of polynomials and of multilinear mappings
47L25	Operator spaces (= matricially normed spaces) [See also 46L07]
47L30	Abstract operator algebras on Hilbert spaces
47L35	Nest algebras, CSL algebras
47L40	Limit algebras, subalgebras of <i>C</i> *-algebras
47L45	Dual algebras; weakly closed singly generated operator algebras
47L50	Dual spaces of operator algebras
47L55	Representations of (nonselfadjoint) operator algebras
47L60	Algebras of unbounded operators; partial algebras of operators
47L65	Crossed product algebras (analytic crossed products)
47L70	Nonassociative nonselfadjoint operator algebras
47L75	Other nonselfadjoint operator algebras
47L80	Algebras of specific types of operators (Toeplitz, integral, pseudodifferential, etc.)
47L90	Applications of operator algebras to physics
47L99	None of the above, but in this section
47Nxx	Miscellaneous applications of operator
	theory [See also 46Nxx]
47N10	Applications in optimization, convex analysis, mathematical programming,
47N120	economics
	Applications to differential and integral equations
47N30	Applications in probability theory and statistics
47N40	Applications in numerical analysis [See also 65Jxx]

47N50 Applications in the physical sciences

ences

47N60 Applications in chemistry and life sci-

Calculu	s of variations and optimal control; optimization
47N70	Applications in systems theory, circuits, and control theory
47N99	None of the above, but in this section
47Sxx	Other (nonclassical) types of operator theory [See also 46Sxx]
47S10	Operator theory over fields other than R , C or the quaternions; non-Archimedean operator theory
47S20	Nonstandard operator theory [See also 03H05]
47S30	Constructive operator theory [See also 03F60]
47S40	Fuzzy operator theory [See also 03E72]
47S50	Operator theory in probabilistic metric linear spaces [See also 54E70]
47S99	None of the above, but in this section
49-XX	Calculus of variations and op-
	timal control; optimization [See also 34H05, 34K35, 65Kxx, 90Cxx, 93-XX]
49-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
49-01	Instructional exposition (textbooks, tutorial papers, etc.)
49-02	Research exposition (monographs, survey articles)
49-03	Historical (must also be assigned at least one classification number from Section 01)
49-04	Explicit machine computation and programs (not the theory of computation or programming)
49-06	Proceedings, conferences, collections, etc.
49Jxx	Existence theories
49J05	Free problems in one independent variable
49J10	Free problems in two or more independent variables
49J15	Optimal control problems involving ordinary differential equations
49J20	Optimal control problems involving partial differential equations
49J21	Optimal control problems involving relations other than differential equations

49J27 Problems in abstract spaces

[See also 90C48, 93C25]

49J30	Optimal solutions belonging to restricted classes	49Mxx	Numerical methods
	(Lipschitz controls, bang-bang controls,	103.50=	[See also 90Cxx, 65Kxx]
	etc.)		Methods based on necessary conditions
49J35	Minimax problems		Newton-type methods
49J40	Variational methods including varia-		Methods of relaxation type
	tional inequalities [See also 47J20]		Discrete approximations
49J45	Methods involving semicontinuity and		Decomposition methods
	convergence; relaxation		Methods involving duality
49J50	Fréchet and Gateaux differentiability		Other methods
	[See also 46G05, 58C20]	49M37	Methods of nonlinear programming
49J52	Nonsmooth analysis	103.500	type [See also 90C30, 65Kxx]
40150	[See also 46G05, 58C50, 90C56]	49M99	None of the above, but in this section
49J53	Set-valued and variational analysis	-	
10155	[See also 28B20, 47H04, 54C60, 58C06]		Miscellaneous topics
49J55	Problems involving randomness [See also 93E20]	49N05	Linear optimal control problems [See also 93C05]
49J99	None of the above, but in this section	49N10	Linear-quadratic problems
4075		49N15	Duality theory
	Optimality conditions	49N20	Periodic optimization
49KU5	Free problems in one independent variable		Impulsive optimal control problems
49K10	Free problems in two or more independent variables	49N30	Problems with incomplete information [See also 93C41]
49K15	Problems involving ordinary differential	49N35	Optimal feedback synthesis [See also 93B52]
40K20	equations Problems involving partial differential	49N45	Inverse problems
49K20	Problems involving partial differential equations	49N60	Regularity of solutions
49K21	Problems involving relations other than	49N70	Differential games
171121	differential equations	49N75	Pursuit and evasion games
49K27	Problems in abstract spaces [See also 90C48, 93C25]	49N90	Applications of optimal control and differential games [See also 90C90, 93C95]
49K30	Optimal solutions belonging to restricted classes	49N99	None of the above, but in this section
49K35	Minimax problems	49Oxx	Manifolds [See also 58Exx]
49K40	Sensitivity, stability, well-posedness		Minimal surfaces
	[See also 90C31]		[See also 53A10, 58E12]
49K45	Problems involving randomness [See also 93E20]	49Q10	Optimization of shapes other than minimal surfaces [See also 90C90]
49K99	None of the above, but in this section	49Q12	Sensitivity analysis
			Geometric measure and integration the-
49Lxx	Hamilton-Jacobi theories,	~ '	ory, integral and normal currents
	including dynamic programming		[See also 28A75, 32C30, 58A25, 58C35]
49L20	Dynamic programming method	49Q20	Variational problems in a geometric
49L25	Viscosity solutions		measure-theoretic setting
49L99	None of the above, but in this section	49Q99	None of the above, but in this section

Geometry Geometry

49Rxx	Variational methods for eigenvalues of	51Bxx	Nonlinear incidence geometry
	operators [See also 47A75]	51B05	General theory
49R05	Variational methods for eigenvalues of	51B10	Möbius geometries
	operators [See also 47A75] (should also be assigned at least one other classifica-	51B15	Laguerre geometries
	tion number in Section 49)	51B20	Minkowski geometries
49R99	None of the above, but in this section	51B25	Lie geometries
	,	51B99	None of the above, but in this section
49Sxx	Variational principles of physics	51Cxx	Ring geometry
49S05	Variational principles of physics (should	отеж	(Hjelmslev, Barbilian, etc.)
	also be assigned at least one other classi-	51C05	Ring geometry
4000	fication number in section 49)		(Hjelmslev, Barbilian, etc.)
49S99	None of the above, but in this section	51C99	None of the above, but in this section
51-XX	Geometry (For algebraic geome-		Coometrie electro existence
	try, see 14-XX)		Geometric closure systems Abstract (Maeda) geometries
51-00	General reference works (handbooks,		Abstract (Macda) geometries Abstract geometries with
5 1 01	dictionaries, bibliographies, etc.)	31D10	exchange axiom
51-01	Instructional exposition (textbooks, tutorial papers, etc.)	51D15	Abstract geometries with parallelism
51-02	Research exposition (monographs,		Combinatorial geometries
	survey articles)		[See also 05B25, 05B35]
51-03	Historical (must also be assigned at least		Lattices of subspaces [See also 05B35]
	one classification number from Section 01)	51D30	Continuous geometries and related topics [See also 06Cxx]
51-04	Explicit machine computation and pro-	51D99	None of the above, but in this section
	grams (not the theory of computation or	E1Evv	Finite geometry and special incidence
51 06	programming) Progradings conformers collections	SILXX	Finite geometry and special incidence structures
51-06	Proceedings, conferences, collections, etc.	51E05	General block designs [See also 05B05]
E1 A 200			Steiner systems
	Linear incidence geometry General theory and projective geome-		Generalized quadrangles, generalized
317103	tries		polygons
51A10	Homomorphism, automorphism and	51E14	(g
- 4	dualities		partial spreads
	Structures with parallelism		Affine and projective planes
	Configuration theorems	51E20	Combinatorial structures in finite projec-
	Algebraization [See also 12Kxx, 20N05]	E1E21	tive spaces [See also 05Bxx]
	Desarguesian and Pappian geometries		Blocking sets, ovals, <i>k</i> -arcs
31A33	Non-Desarguesian affine and projective planes	J1E22	Linear codes and caps in Galois spaces [See also 94B05]
51A40	Translation planes and spreads	51E23	Spreads and packing problems
51A45	Incidence structures imbeddable into	51E24	Buildings and the geometry of diagrams
	projective geometries		Other finite nonlinear geometries
51A50	Polar geometry, symplectic spaces, or-		Other finite linear geometries
= 4 4 0 5	thogonal spaces	51E30	Other finite incidence structures
51A99	None of the above, but in this section	5 1,700	[See also 05B30] None of the above, but in this section
		11099	THE COURT OF THE SHOWE THAT IN THIS COURTON

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		51Lxx	Geometric order structures
	Metric geometry		[See also 53C75]
51F05	Absolute planes	51L05	Geometry of orders of nondifferentiable
	Absolute spaces	- 47.40	curves
51F15	Reflection groups, reflection geometries		Directly differentiable curves
	[See also 20H10, 20H15; for Coxeter		<i>n</i> -vertex theorems via direct methods
	groups, see 20F55]	51L20	Geometry of orders of surfaces
51F20	Congruence and orthogonality [See also 20H05]	51L99	None of the above, but in this section
51F25	Orthogonal and unitary groups	51Mxx	Real and complex geometry
	[See also 20H05]		Elementary problems in Euclidean ge-
51F99	None of the above, but in this section		ometries
		51M05	Euclidean geometries (general) and gen-
51Gxx	Ordered geometries		eralizations
	(ordered incidence structures, etc.)	51M09	Elementary problems in hyperbolic and
51G05	Ordered geometries		elliptic geometries
E 1 C 00	(ordered incidence structures, etc.)	51M10	Hyperbolic and elliptic geometries (gen-
51G99	None of the above, but in this section		eral) and generalizations
			Geometric constructions
	Topological geometry	51M16	Inequalities and extremum problems
	General theory		(For convex problems, see 52A40)
	Topological linear incidence structures	51M20	Polyhedra and polytopes; regular fig-
51H15	Topological nonlinear incidence struc-		ures, division of spaces [See also 51F15]
54110 0	tures	51M25	Length, area and volume
51H20	Topological geometries on manifolds	F13.420	[See also 26B15]
51 LJ 25	[See also 57-XX] Geometries with differentiable structure	51M30	Line geometries and their generaliza-
311123	[See also 53Cxx, 53C70]	51N/25	tions [See also 53A25]
51H30	Geometries with algebraic manifold	311133	Synthetic treatment of fundamental manifolds in projective geometries
311130	structure [See also 14-XX]		(Grassmannians, Veronesians and their
51H99	None of the above, but in this section		generalizations) [See also 14M15]
0111/	Trone of the above, but in this section	51M99	None of the above, but in this section
51Jxx	Incidence groups		, a san
51J05	General theory	51Nxx	Analytic and descriptive geometry
	Projective incidence groups		Descriptive geometry
51J15	Kinematic spaces	011100	[See also 65D17, 68U07]
-	•	51N10	Affine analytic geometry
51J20	Representation by near-fields and near-algebras [See also 12K05, 16Y30]		Projective analytic geometry
51J99	None of the above, but in this section		Euclidean analytic geometry
31,77	None of the above, but in this section		Analytic geometry with other transfor-
F1 T/	D'atana and an	011120	mation groups
	Distance geometry	51N30	Geometry of classical groups
	General theory	2 = 1 , 0 0	[See also 20Gxx, 14L35]
	Synthetic differential geometry	51N35	Questions of classical algebraic geome-
51K99	None of the above, but in this section		try [See also 14Nxx]
		51N99	None of the above, but in this section

51Pxx	Geometry and physics (should also be assigned at least one other classification		Other problems of combinatorial convexity
51P05	number from Sections 70–86) Geometry and physics (should also be	52A38	Length, area, volume [See also 26B15, 28A75, 49Q20]
311 03	assigned at least one other classification	52A39	Mixed volumes and related topics
	number from Sections 70–86)	52A40	Inequalities and extremum problems
51P99	None of the above, but in this section	52A41	Convex functions and convex programs
52-XX	Convex and discrete geometry	52 A 55	[See also 26B25, 90C25] Spherical and hyperbolic convexity
52-00	General reference works (handbooks,		None of the above, but in this section
	dictionaries, bibliographies, etc.)	3211))	Trone of the above, but in this section
52-01	Instructional exposition	52Byy	Polytopes and polyhedra
	(textbooks, tutorial papers, etc.)	52B05	
52-02	Research exposition (monographs,	02000	(number of faces, shortest paths, etc.)
50 00	survey articles)		[See also 05Cxx]
52-03	Historical (must also be assigned at least	52B10	Three-dimensional polytopes
	one classification number from Section 01)	52B11	<i>n</i> -dimensional polytopes
52-04	Explicit machine computation and pro-	52B12	Special polytopes (linear programming,
32-04	grams (not the theory of computation or		centrally symmetric, etc.)
	programming)	52B15	Symmetry properties of polytopes
52-06	Proceedings, conferences, collections,	52B20	Lattice polytopes (including relations
	etc.		with commutative algebra and alge-
52Axx	General convexity		braic geometry) [See also 06A11, 13F20,
	Axiomatic and generalized convexity	EDPDD	13Hxx]
	Convex sets without dimension restric-		Shellability Calcardathan disagraps
	tions		Gale and other diagrams
52A07	Convex sets in topological vector spaces	52B40	Matroids (realizations in the context of convex polytopes, convexity in combi-
	[See also 46A55]		natorial structures, etc.)
52A10	Convex sets in 2 dimensions (including		[See also 05B35, 52Cxx]
	convex curves) [See also 53A04]	52B45	Dissections and valuations
52A15	Convex sets in 3 dimensions (including		(Hilbert's third problem, etc.)
E2 4 20	convex surfaces) [See also 53A05, 53C45]	52B55	Computational aspects related to con-
32A20	Convex sets in <i>n</i> dimensions (including convex hypersurfaces)		vexity (For computational geometry and
	[See also 53A07, 53C45]		algorithms, see 68Q25, 68U05; for nu-
52A21	Finite-dimensional Banach spaces		merical algorithms, see 65Yxx)
	(including special norms, zonoids, etc.)	52B60	[See also 68Uxx] Isoperimetric problems for polytopes
	[See also 46Bxx]	52B70	Polyhedral manifolds
52A22	Random convex sets and integral geom-	52B99	None of the above, but in this section
	etry [See also 53C65, 60D05]	32077	None of the above, but in this section
52A23	Asymptotic theory of convex bodies	52Cxx	Discrete geometry
52 A 27	[See also 46B06] Approximation by convex sets		Lattices and convex bodies in 2 dimen-
	Variants of convex sets	_	sions [See also 11H06, 11H31, 11P21]
041100	(star-shaped, (<i>m</i> , <i>n</i>)-convex, etc.)	52C07	Lattices and convex bodies in n dimen-
52A35	Helly-type theorems and geometric		sions [See also 11H06, 11H31, 11P21]
3_1100	transversal theory	52C10	Erdős problems and related topics of discrete geometry [See also 11Hxx]

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52C15	Packing and covering in 2 dimensions		Kinematics
E2C17	[See also 05B40, 11H31]		Projective differential geometry
52C17	Packing and covering in <i>n</i> dimensions [See also 05B40, 11H31]		Differential line geometry
52C20	Tilings in 2 dimensions		Conformal differential geometry
02020	[See also 05B45, 51M20]		Non-Euclidean differential geometry
52C22	Tilings in <i>n</i> dimensions		Other special differential geometries
	[See also 05B45, 51M20]		Vector and tensor analysis
52C23	Quasicrystals, aperiodic tilings	53A55	Differential invariants (local theory),
52C25	Rigidity and flexibility of structures	53 4 60	geometric objects Geometry of webs
	[See also 70B15]	33A00	[See also 14C21, 20N05]
52C26	Circle packings and discrete conformal geometry	53A99	None of the above, but in this section
52C30	Planar arrangements of lines and pseu-		T 1100 01
F0.C0F	dolines		Local differential geometry
52C35	Arrangements of points, flats, hyper-		Linear and affine connections
E2 C40	planes [See also 32S22] Oriented matroids		Projective connections
			Other connections
J2C4J	Combinatorial complexity of geometric structures [See also 68U05]		Local Riemannian geometry
52C99	None of the above, but in this section		Methods of Riemannian geometry
			Local submanifolds [See also 53C40] Lorentz metrics, indefinite metrics
53-XX	Differential geometry (For dif-		Hermitian and Kählerian structures
	ferential topology, see 57Rxx. For foundational questions of differ-	33 D 33	[See also 32Cxx]
	entiable manifolds, see 58Axx)	53B40	Finsler spaces and generalizations
52 00	· · · · · · · · · · · · · · · · · · ·		(areal metrics)
53-00	General reference works (handbooks, dictionaries, bibliographies, etc.)	53B50	Applications to physics
53-01	Instructional exposition	53B99	None of the above, but in this section
	(textbooks, tutorial papers, etc.)		
53-02	Research exposition (monographs,	53Cxx	Global differential geometry [See also
	survey articles)		51H25, 58-XX; for related bundle theory,
53-03	Historical (must also be assigned at least	F2C0F	see 55Rxx, 57Rxx]
	one classification number from Section		Connections, general theory
F2 04	01)	53C07	Special connections and metrics on vector bundles (Hermite-Einstein-Yang-
53-04	Explicit machine computation and programs (not the theory of computation or		Mills) [See also 32Q20]
	programming)	53C08	Gerbes, differential characters: differen-
53-06	Proceedings, conferences, collections,		tial geometric aspects
	etc.	53C10	G-structures
53 A xx	Classical differential geometry	53C12	Foliations (differential geometric as-
	Curves in Euclidean space		pects) [See also 57R30, 57R32]
	Surfaces in Euclidean space	53C15	General geometric structures on mani-
	Higher-dimensional and -codimension-		folds (almost complex, almost product
	al surfaces in Euclidean <i>n</i> -space	E2C1E	structures, etc.)
53A10	Minimal surfaces, surfaces with pre-		Sub-Riemannian geometry
	scribed mean curvature [See also 49Q05, 49Q10, 53C42]	53C20	Global Riemannian geometry, including pinching [See also 31C12, 58B20]

53A15 Affine differential geometry

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53C21	Methods of Riemannian geometry, including PDE methods; curvature restrictions [See also 58J60]	53Dxx	Symplectic geometry, contact geometry [See also 37]xx, 70Gxx, 70Hxx]
53C22	Geodesics [See also 58E10]	53D05	Symplectic manifolds, general
	Global geometric and topological meth-	53D10	Contact manifolds, general
JJC25	ods (à la Gromov); differential geometric	53D12	Lagrangian submanifolds; Maslov index
5 0.604	analysis on metric spaces	53D15	Almost contact and almost symplectic manifolds
	Rigidity results Special Riemannian manifolds	53D17	Poisson manifolds; Poisson groupoids and algebroids
	(Einstein, Sasakian, etc.)	53D18	Generalized geometries (à la Hitchin)
53C26	Hyper-Kähler and quaternionic Kähler geometry, "special" geometry	53D20	Momentum maps; symplectic reduction
53C27	Spin and Spin ^c geometry	53D22	Canonical transformations
	Twistor methods [See also 32L25]	53D25	Geodesic flows
	Issues of holonomy	53D30	Symplectic structures of moduli spaces
	Homogeneous manifolds [See also 14M15, 14M17, 32M10, 57T15]	53D35	Global theory of symplectic and contact manifolds [See also 57Rxx]
53C35	Symmetric spaces [See also 32M15, 57T15]	53D37	Mirror symmetry, symplectic aspects; homological mirror symmetry; Fukaya category [See also 14J33]
53C38	Calibrations and calibrated geometries	53D40	Floer homology and cohomology, sym-
53C40	Global submanifolds [See also 53B25]	33 D 40	plectic aspects
53C42	Immersions (minimal, prescribed curvature, tight, etc.) [See also 49Q05, 49Q10, 53A10, 57R40, 57R42]	53D42	Symplectic field theory; contact homology
53C43	Differential geometric aspects of harmonic maps [See also 58E20]	53D45	Gromov-Witten invariants, quantum co- homology, Frobenius manifolds [See also 14N35]
53C44	Geometric evolution equations	53D50	Geometric quantization
	(mean curvature flow, Ricci flow, etc.)		Deformation quantization, star products
53C45	Global surface theory		None of the above, but in this section
	(convex surfaces à la A. D. Aleksandrov)	33077	Notic of the above, but in this section
53C50	Lorentz manifolds, manifolds with in-	527vv	Applications to physics
53C55	definite metrics Hermitian and Kählerian manifolds		Applications to physics Applications to physics
33 C 33	[See also 32Cxx]		None of the above, but in this section
53C56	Other complex differential geometry [See also 32Cxx]	-	General topology
53C60	Finsler spaces and generalizations (areal metrics) [See also 58B20]		(For the topology of manifolds of all dimensions, see 57Nxx)
53C65	Integral geometry [See also 52A22, 60D05]; differential forms, currents, etc.	54-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
E0.050	[See mainly 58Axx]	54-01	Instructional exposition
53C70	Direct methods	E4 00	(textbooks, tutorial papers, etc.)
	(G-spaces of Busemann, etc.)	54-02	Research exposition (monographs,
53C/5	Geometric orders, order geometry	E4 00	survey articles)
53C90	[See also 51Lxx]	54-03	Historical (must also be assigned at least one classification number from Section
	Applications to physics None of the above, but in this section		01)
	There is the above that in this section		~ - ,

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54-04	Explicit machine computation and programs (not the theory of computation or	54C40	Algebraic properties of function spaces [See also 46J10]
	programming)	54C45	C- and C*-embedding
54-06	Proceedings, conferences, collections,		Special sets defined by functions
	etc.		[See also 26A21]
54Axx	Generalities	54C55	Absolute neighborhood extensor, abso-
54A05	Topological spaces and generalizations		lute extensor, absolute neighborhood
	(closure spaces, etc.)		retract (ANR), absolute retract spaces
54A10	Several topologies on one set (change of	0	(general properties) [See also 55M15]
	topology, comparison of topologies, lat-		Shape theory [See also 55P55, 57N25]
	tices of topologies)	54C60	Set-valued maps [See also 26E25, 28B20,
54A15	Syntopogeneous structures	F4C(F	47H04, 58C06]
54A20	Convergence in general topology		Selections [See also 28B20]
	(sequences, filters, limits, convergence		Entropy
	spaces, etc.)	54C99	None of the above, but in this section
54A25	Cardinality properties (cardinal func-		
	tions and inequalities, discrete subsets)		Fairly general properties
	[See also 03Exx] (For ultrafilters, see 54D80)	54D05	Connected and locally connected spaces
54 Δ 35	Consistency and independence results	F4D10	(general aspects)
J -11 1 JJ	[See also 03E35]		Lower separation axioms (T_0 – T_3 , etc.)
54A40	Fuzzy topology [See also 03E72]	54D15	Higher separation axioms (completely
	None of the above, but in this section		regular, normal, perfectly or collection- wise normal, etc.)
0 11 177	There of the above, and he had been en	54D20	Noncompact covering properties
		01020	
54Bxx	Basic constructions		(paracompact, Lindelöt, etc.)
	Basic constructions Subspaces	54D25	(paracompact, Lindelöf, etc.) "P-minimal" and "P-closed" spaces
54B05	Subspaces		"P-minimal" and "P-closed" spaces
54B05 54B10	Subspaces Product spaces	54D30	"P-minimal" and "P-closed" spaces Compactness
54B05 54B10	Subspaces Product spaces Quotient spaces, decompositions	54D30	"P-minimal" and "P-closed" spaces
54B05 54B10 54B15	Subspaces Product spaces	54D30	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifica-
54B05 54B10 54B15	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar construc-	54D30 54D35	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifica- tions, supercompactifications, comple-
54B05 54B10 54B15 54B17	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions	54D30 54D35 54D40	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifica- tions, supercompactifications, comple- tions, etc.)
54B05 54B10 54B15 54B17 54B20	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces	54D30 54D35 54D40 54D45	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifica- tions, supercompactifications, comple- tions, etc.) Remainders
54B05 54B10 54B15 54B17 54B20 54B30 54B35	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30]	54D30 54D35 54D40 54D45 54D50	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra	54D30 54D35 54D40 54D45 54D50 54D55	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ -compactness k -spaces
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20]	54D30 54D35 54D40 54D45 54D50 54D55 54D60	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ -compactness k -spaces Sequential spaces Realcompactness and realcompactification
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20]	54D30 54D35 54D40 54D45 54D50 54D55 54D60	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ -compactness k -spaces Sequential spaces Realcompactness and realcompactification Separability
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70	" P -minimal" and " P -closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ -compactness k -spaces Sequential spaces Realcompactness and realcompactification Separability
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces de-	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ -compactness k -spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.)
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ -compactness k -spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08 54C10	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps Weak and generalized continuity Special maps on topological spaces (open, closed, perfect, etc.)	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.) None of the above, but in this section
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08 54C10	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps Weak and generalized continuity Special maps on topological spaces	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80 54D99	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.) None of the above, but in this section
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08 54C10	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps Weak and generalized continuity Special maps on topological spaces (open, closed, perfect, etc.)	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80 54D99	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.) None of the above, but in this section Spaces with richer structures Proximity structures and generaliza-
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08 54C10 54C15 54C20	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps Weak and generalized continuity Special maps on topological spaces (open, closed, perfect, etc.) Retraction	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80 54D99 54Exx 54E05	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.) None of the above, but in this section Spaces with richer structures Proximity structures and generalizations
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08 54C10 54C15 54C20 54C20	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps Weak and generalized continuity Special maps on topological spaces (open, closed, perfect, etc.) Retraction Extension of maps	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80 54D99 54Exx 54E05	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.) None of the above, but in this section Spaces with richer structures Proximity structures and generalizations Uniform structures and generalizations
54B05 54B10 54B15 54B17 54B20 54B30 54B35 54B40 54B99 54Cxx 54C05 54C08 54C10 54C15 54C20 54C20 54C25 54C30	Subspaces Product spaces Quotient spaces, decompositions Adjunction spaces and similar constructions Hyperspaces Categorical methods [See also 18B30] Spectra Presheaves and sheaves [See also 18F20] None of the above, but in this section Maps and general types of spaces defined by maps Continuous maps Weak and generalized continuity Special maps on topological spaces (open, closed, perfect, etc.) Retraction Extension of maps Embedding	54D30 54D35 54D40 54D45 54D50 54D55 54D60 54D65 54D70 54D80 54D99 54Exx 54E05 54E15 54E17	"P-minimal" and "P-closed" spaces Compactness Extensions of spaces (compactifications, supercompactifications, completions, etc.) Remainders Local compactness, σ-compactness k-spaces Sequential spaces Realcompactness and realcompactification Separability Base properties Special constructions of spaces (spaces of ultrafilters, etc.) None of the above, but in this section Spaces with richer structures Proximity structures and generalizations

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54E25	Stratifiable spaces, cosmic spaces, etc. Semimetric spaces	54H13	Topological fields, rings, etc. [See also 12Jxx] (For algebraic aspects, see 13Jxx, 16W80)
54E30 54E35	Moore spaces Metric spaces, metrizability	54H15	Transformation groups and semigroups [See also 20M20, 22-XX, 57Sxx]
54E40 54E45	Special maps on metric spaces Compact (locally compact) metric spaces	54H20	Topological dynamics [See also 28Dxx, 37Bxx]
54E50 54E52	Complete metric spaces Baire category, Baire spaces	54H25	Fixed-point and coincidence theorems [See also 47H10, 55M20]
54E55 54E70	Bitopologies Probabilistic metric spaces	54H99	None of the above, but in this section
54E99	None of the above, but in this section	54Jxx 54J05	Nonstandard topology [See also 03H05] Nonstandard topology [See also 03H05]
	Special properties	54J99	None of the above, but in this section
54F05	Linearly ordered topological spaces, generalized ordered spaces, and par-	55-XX	Algebraic topology
	tially ordered spaces [See also 06B30, 06F30]	55-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
54F15 54F35	Continua and generalizations Higher-dimensional local connected-	55-01	Instructional exposition (textbooks, tutorial papers, etc.)
54F45	ness [See also 55Mxx, 55Nxx] Dimension theory [See also 55M10]	55-02	Research exposition (monographs, survey articles)
54F50	Spaces of dimension ≤ 1; curves, dendrites [See also 26A03]	55-03	Historical (must also be assigned at least one classification number from Section
54F55	Unicoherence, multicoherence	FF 0.4	01)
54F65	Topological characterizations of particular spaces	55-04	Explicit machine computation and programs (not the theory of computation or programming)
54F99	None of the above, but in this section	55-06	Proceedings, conferences, collections, etc.
	Peculiar spaces		
	Extremally disconnected spaces, <i>F</i> -spaces, etc.	SSIVIXX	Classical topics (For the topology of Euclidean spaces and manifolds, see 57Nxx)
	P-spaces	55M05	Duality
	Scattered spaces		Dimension theory [See also 54F45]
	Pathological spaces		Absolute neighborhood retracts
	Counterexamples		[See also 54C55]
	None of the above, but in this section	55M20	Fixed points and coincidences [See also 54H25]
54Hxx	Connections with other structures,	55M25	Degree, winding number
E4110E	applications	55M30	Ljusternik-Schnirelman (Lyusternik-
341103	Descriptive set theory (topological aspects of Borel, analytic, projective, etc. sets) [See also 03E15, 26A21, 28A05]	55M35	Shnirel'man) category of a space Finite groups of transformations
54H10	Topological representations of algebraic systems [See also 22-XX]	55M99	(including Smith theory) [See also 57S17] None of the above, but in this section
54H11	Topological groups [See also 22A05]		
	Topological lattices, etc. [See also 06B30, 06F30]		Homology and cohomology theories [See also 57Txx]
	[222	55N05	Čech types

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55N07	Steenrod-Sitnikov homologies	55P65	Homotopy functors
55N10	Singular theory	55P91	Equivariant homotopy theory
55N15	<i>K</i> -theory [See also 19Lxx] (For algebraic <i>K</i> -theory, see 18F25, 19-XX)	55P92	[See also 19L47] Relations between equivariant and
55N20	Generalized (extraordinary) homology and cohomology theories	55P99	nonequivariant homotopy theory None of the above, but in this section
55N22	Bordism and cobordism theories, formal group laws [See also 14L05, 19L41, 57R75, 57R77, 57R85, 57R90]	55Qxx	Homotopy groups Homotopy groups, general;
55N25	Homology with local coefficients, equivariant cohomology		sets of homotopy classes
55N30	Sheaf cohomology [See also 18F20, 32C35, 32L10]	55Q10	Shape groups Stable homotopy groups
55N32	Orbifold cohomology	55Q15	Whitehead products and generalizations
	Intersection homology and cohomology	55O20	Homotopy groups of wedges, joins, and
	Elliptic cohomology	~~~	simple spaces
	Other homology theories	55Q25	Hopf invariants
	Axioms for homology theory and		Operations in homotopy groups
	uniqueness theorems		Homotopy groups of spheres
55N45	Products and intersections	55Q45	Stable homotopy of spheres
55N91	Equivariant homology and cohomology	55Q50	J-morphism [See also 19L20]
> 100	[See also 19L47]	55Q51	v_n -periodicity
55N99	None of the above, but in this section	55Q52	Homotopy groups of special spaces
		55055	C-1
		33 Q 33	Cohomotopy groups
	Homotopy theory (For simple homotopy type, see 57Q10)		Homotopy groups of special types [See also 55N05, 55N07]
55P05	topy type, see 57Q10) Homotopy extension properties, cofibrations	55Q70	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups
55P05 55P10	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences	55Q70 55Q91	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47]
55P05 55P10 55P15	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type	55Q70 55Q91	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups
55P05 55P10 55P15 55P20	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces	55Q70 55Q91 55Q99	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section
55P05 55P10 55P15 55P20 55P25	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality	55Q70 55Q91 55Q99	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47]
55P05 55P10 55P15 55P20 55P25 55P30	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality	55Q70 55Q91 55Q99 55Rxx	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25]
55P05 55P10 55P15 55P20 55P25 55P30 55P35	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces	55Q70 55Q91 55Q99 55Rxx 55R05	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions	55Q70 55Q91 55Q99 55Rxx 55R05 55R10	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R15	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R15	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R15 55R20	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx]
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43 55P43	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals Infinite loop spaces	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R15 55R20 55R25	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx] Sphere bundles and vector bundles
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43 55P45 55P47 55P48	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals Infinite loop spaces Loop space machines, operads [See also 18D50]	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R15 55R20 55R25	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx]
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43 55P45 55P47 55P48	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals Infinite loop spaces Loop space machines, operads [See also 18D50] String topology	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R15 55R20 55R25 55R35	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx] Sphere bundles and vector bundles Classifying spaces of groups and
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43 55P45 55P47 55P48 55P50 55P55	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals Infinite loop spaces Loop space machines, operads [See also 18D50] String topology Shape theory [See also 54C56, 55Q07]	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R20 55R25 55R35 55R37	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx] Sphere bundles and vector bundles Classifying spaces of groups and H-spaces Maps between classifying spaces Homology of classifying spaces, charac-
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43 55P45 55P47 55P48 55P50 55P55 55P57	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals Infinite loop spaces Loop space machines, operads [See also 18D50] String topology Shape theory [See also 54C56, 55Q07] Proper homotopy theory	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R25 55R25 55R35 55R37 55R40	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx] Sphere bundles and vector bundles Classifying spaces of groups and H-spaces Maps between classifying spaces Homology of classifying spaces, characteristic classes [See also 57Txx, 57R20]
55P05 55P10 55P15 55P20 55P25 55P30 55P35 55P40 55P42 55P43 55P45 55P47 55P48 55P50 55P55 55P57 55P60	topy type, see 57Q10) Homotopy extension properties, cofibrations Homotopy equivalences Classification of homotopy type Eilenberg-Mac Lane spaces Spanier-Whitehead duality Eckmann-Hilton duality Loop spaces Suspensions Stable homotopy theory, spectra Spectra with additional structure $(E_{\infty}, A_{\infty}, \text{ring spectra, etc.})$ H -spaces and duals Infinite loop spaces Loop space machines, operads [See also 18D50] String topology Shape theory [See also 54C56, 55Q07]	55Q70 55Q91 55Q99 55Rxx 55R05 55R10 55R12 55R25 55R25 55R35 55R37 55R40	Homotopy groups of special types [See also 55N05, 55N07] Equivariant homotopy groups [See also 19L47] None of the above, but in this section Fiber spaces and bundles [See also 18F15, 32Lxx, 46M20, 57R20, 57R22, 57R25] Fiber spaces Fiber bundles Transfer Classification Spectral sequences and homology of fiber spaces [See also 55Txx] Sphere bundles and vector bundles Classifying spaces of groups and H-spaces Maps between classifying spaces Homology of classifying spaces, charac-

55R50	Stable classes of vector space bundles, <i>K</i> -theory [See also 19Lxx] (For algebraic		Simplicial sets and complexes Chain complexes
	K-theory, see 18F25, 19-XX)		Universal coefficient theorems,
55R55	Fiberings with singularities		Bockstein operator
55R60	Microbundles and block bundles [See also 57N55, 57Q50]	55U25	Homology of a product, Künneth formula
55R65		55U30	Duality
	dles		Abstract and axiomatic
	Fibrewise topology		homotopy theory
55R80	Discriminantal varieties, configuration spaces	55U40	Topological categories, foundations of homotopy theory
55R91	Equivariant fiber spaces and bundles [See also 19L47]	55U99	None of the above, but in this section
55R99	None of the above, but in this section	57-XX	Manifolds and cell complexes (For complex manifolds, see
55Svv	Operations and obstructions		32Qxx)
55S05	Primary cohomology operations	57-00	General reference works (handbooks,
55S10	Steenrod algebra	0. 00	dictionaries, bibliographies, etc.)
	Dyer-Lashof operations	57-01	Instructional exposition
55S15	Symmetric products, cyclic products		(textbooks, tutorial papers, etc.)
55S20	Secondary and higher cohomology operations	57-02	Research exposition (monographs, survey articles)
55S25	K-theory operations and generalized co- homology operations [See also 19D55, 19Lxx]	57-03	Historical (must also be assigned at least one classification number from Section 01)
55S30	Massey products	57-04	Explicit machine computation and pro-
55S35	Obstruction theory		grams (not the theory of computation or
55S36	Extension and compression of mappings	FF 06	programming)
55S37	Classification of mappings	57-06	Proceedings, conferences, collections, etc.
55S40	Sectioning fiber spaces and bundles		
55S45	Postnikov systems, k-invariants		Low-dimensional topology
55S91	Equivariant operations and obstructions	37 W103	Fundamental group, presentations, free differential calculus
FFC00	[See also 19L47]	57M07	Topological methods in group theory
55599	None of the above, but in this section		Covering spaces
FETTAGE	Constral as success	57M12	Special coverings, e.g. branched
	Spectral sequences [See also 18G40, 55R20]	57M15	Relations with graph theory [See also 05Cxx]
	General	57M20	Two-dimensional complexes
	Serre spectral sequences		Knots and links in S^3
	Adams spectral sequences		(For higher dimensions, see 57Q45)
55T20	Eilenberg-Moore spectral sequences [See also 57T35]		Invariants of knots and 3-manifolds
55T25	Generalized cohomology	3/1VI3U	Wild knots and surfaces, etc., wild embeddings
55T99	None of the above, but in this section	57M35	Dehn's lemma, sphere theorem, loop
55Uxx	Applied homological algebra and category theory [See also 18Gxx]	57M40	theorem, asphericity Characterizations of E^3 and S^3
55U05	Abstract complexes		(Poincaré conjecture) [See also 57N12]

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57M50	Geometric structures on low-dimensional manifolds		Triangulating manifolds
57M60	Group actions in low dimensions		Cobordism
	None of the above, but in this section	37Q23	Comparison of PL-structures: classification, Hauptvermutung
	,	57()3()	Engulfing
57Nxx	Topological manifolds		Embeddings and immersions
	Topology of E^2 , 2-manifolds		Isotopy
	Topology of general 3-manifolds		Regular neighborhoods
	[See also 57Mxx]		
57N12	Topology of E^3 and S^3 [See also 57M40]	37Q43	Knots and links (in high dimensions) (For the low-dimensional case, see
	Topology of E^4 , 4-manifolds		57M25)
	[See also 14Jxx, 32Jxx]	57Q50	Microbundles and block bundles
57N15	Topology of E^n , n -manifolds $(4 < n < \infty)$	~	[See also 55R60, 57N55]
57N16	Geometric structures on manifolds	57Q55	Approximations
	[See also 57M50]	57Q60	Cobordism and concordance
	Topology of topological vector spaces	57Q65	General position and transversality
57N20	Topology of infinite-dimensional mani-		Equivariant PL-topology
EZNIGE	folds [See also 58Bxx]	57Q99	None of the above, but in this section
	Shapes [See also 54C56, 55P55, 55Q07]		
	Engulfing Embaddings and immersions	57Rxx	Differential topology (For foundational
	Embeddings and immersions		questions of differentiable manifolds,
	Isotopy and pseudo-isotopy		see 58Axx; for infinite-dimensional
	Neighborhoods of submanifolds	E7D0E	manifolds, see 58Bxx)
	Flatness and tameness		Triangulating
	$S^{n-1} \subset E^n$, Schoenflies problem		Smoothing
57N55	Microbundles and block bundles [See also 55R60, 57Q50]		Smooth approximations
57NI60	Cellularity	5/K15	Specialized structures on manifolds (spin manifolds, framed manifolds, etc.)
	-	57D17	-
	Algebraic topology of manifolds Cobordism and concordance	57R17	Symplectic and contact topology
			Topology and geometry of orbifolds
	General position and transversality Stratifications		Algebraic topology on manifolds
			Characteristic classes and numbers
3/11/99	None of the above, but in this section	5/K22	Topology of vector bundles and fiber bundles [See also 55Rxx]
E7Dvv	Generalized manifolds [See also 18F15]	57R25	Vector fields, frame fields
			Controllability of vector fields on C^{∞} and
3/1 03	Local properties of generalized manifolds	071127	real-analytic manifolds [See also 49Qxx,
57P10	Poincaré duality spaces		37C10, 93B05]
	None of the above, but in this section	57R30	Foliations; geometric theory
	,		Classifying spaces for foliations;
57Oxx	PL-topology		Gelfand-Fuks cohomology
	General topology of complexes		[See also 58H10]
	Simple homotopy type, Whitehead tor-	57R35	Differentiable mappings
	sion, Reidemeister-Franz torsion, etc.	57R40	Embeddings
	[See also 19B28]	57R42	Immersions
57Q12	Wall finiteness obstruction for	57R45	Singularities of differentiable mappings
	CW-complexes		Diffeomorphisms

57R52	Isotopy	57T20	Homotopy groups of topological groups
57R55	Differentiable structures		and homogeneous spaces
57R56	Topological quantum field theories		Homology and cohomology of <i>H</i> -spaces
57R57	Applications of global analysis to struc-	57T30	Bar and cobar constructions
	tures on manifolds, Donaldson and	FFTOF	[See also 18G55, 55Uxx]
	Seiberg-Witten invariants [See also 58-XX]	57135	Applications of Eilenberg-Moore spec-
57R58	Floer homology	57T99	tral sequences [See also 55R20, 55T20] None of the above, but in this section
	Homotopy spheres, Poincaré conjecture		
	Surgery and handlebodies	58-XX	Global analysis, analysis on
57R67	Surgery obstructions, Wall groups [See also 19]25]		manifolds [See also 32Cxx, 32Fxx, 32Wxx, 46-XX, 47Hxx, 53Cxx] (For geometric integra-
57R70	Critical points and critical submanifolds		tion theory, see 49Q15)
57R75	O- and SO-cobordism	<u> </u>	•
57R77	Complex cobordism (U- and SU-cobord-	58-00	General reference works (handbooks, dictionaries, bibliographies, etc.)
	ism) [See also 55N22]	58-01	Instructional exposition
	<i>h</i> - and <i>s</i> -cobordism		(textbooks, tutorial papers, etc.)
	Equivariant cobordism	58-02	Research exposition (monographs,
57R90	Other types of cobordism [See also 55N22]	5 0.02	survey articles)
57R91	Equivariant algebraic topology of manifolds	58-03	Historical (must also be assigned at least one classification number from Section 01)
57R95	Realizing cycles by submanifolds	58-04	Explicit machine computation and pro-
57R99	None of the above, but in this section		grams (not the theory of computation or programming)
57Sxx	Topological transformation groups [See also 20F34, 22-XX, 37-XX, 54H15, 58D05]	58-06	Proceedings, conferences, collections, etc.
57S05	Topological properties of groups of	58Axx	General theory of differentiable mani-
	homeomorphisms or diffeomorphisms	E8 V U3	folds [See also 32Cxx]
57S10	Compact groups of homeomorphisms	36A03	Topos-theoretic approach to differentiable manifolds
57S15	Compact Lie groups of differentiable	58A05	Differentiable manifolds, foundations
E7C17	transformations	58A07	Real-analytic and Nash manifolds
57S17	Finite transformation groups		[See also 14P20, 32C07]
3/320	Noncompact Lie groups of transformations		Differential forms
57S25	Groups acting on specific manifolds		de Rham theory [See also 14Fxx]
57S30	Discontinuous groups of transforma-	58A14	Hodge theory [See also 14C30, 14Fxx, 32J25, 32S35]
57S99	tions None of the above, but in this section	58A15	Exterior differential systems
0.000	Thore of the above, but in this section		(Cartan theory)
57Txx	Homology and homotopy of topologi-		Pfaffian systems
	cal groups and related structures	58A20	•
57T05	Hopf algebras [See also 16T05]		Currents [See also 32C30, 53C65]
57T10	Homology and cohomology of	58A30	Vector distributions
	Lie groups	E0 4 22	(subbundles of the tangent bundles)
57T15	Homology and cohomology of homoge-		Natural bundles
	neous spaces of Lie groups		Stratified sets [See also 32S60]
		38A4U	Differential spaces

58A50	Supermanifolds and graded manifolds [See also 14A22, 32C11]	58D07	Groups and semigroups of nonlinear operators [See also 17B65, 47H20]
58A99	None of the above, but in this section	58D10	Spaces of imbeddings and immersions
EQRyy	Infinite-dimensional manifolds	58D15	Manifolds of mappings [See also 46T10 54C35]
58B05	Homotopy and topological questions	58D17	Manifolds of metrics (esp. Riemannian)
	Differentiability questions		Group actions and symmetry properties
	Questions of holomorphy		Measures (Gaussian, cylindrical, etc.)
	[See also 32-XX, 46G20]		on manifolds of maps [See also 28Cxx 46T12]
58B15	Fredholm structures [See also 47A53]	58D25	Equations in function spaces; evolution
58B20	Riemannian, Finsler and other geometric structures [See also 53C20, 53C60]		equations [See also 34Gxx, 35K90, 35L90 35R15, 37Lxx, 47Jxx]
58B25	Group structures and generalizations on	58D27	
	infinite-dimensional manifolds [See also 22E65, 58D05]		metric structures
58B32	Geometry of quantum groups	58D29	Moduli problems for topological struc-
	Noncommutative geometry	E0D20	tures
	(à la Connes)	38D30	Applications (in quantum mechanics (Feynman path integrals), relativity
58B99	None of the above, but in this section		fluid dynamics, etc.)
î		58D99	None of the above, but in this section
58Cxx	Calculus on manifolds; nonlinear oper-		,
	ators [See also 46Txx, 47Hxx, 47Jxx]	58Exx	Variational problems in infinite-di-
	Real-valued functions		mensional spaces
58C06	Set valued and function-space valued	58E05	Abstract critical point theory (Morse
58C07	mappings [See also 47H04, 54C60]		theory, Ljusternik-Schnirelman (Lyus-
	Continuity properties of mappings	E0E07	ternik-Shnirel'man) theory, etc.)
	Holomorphic maps [See also 32-XX] Implicit function theorems;	58E07 58E09	Abstract bifurcation theory
30 C 13	global Newton methods	58E10	Group-invariant bifurcation theory Applications to the theory of geodesics
58C20	Differentiation theory (Gateaux, Fréchet,	JOL 10	(problems in one independent variable)
	etc.) [See also 26Exx, 46G05]	58E11	Critical metrics
58C25	Differentiable maps	58E12	Applications to minimal surfaces (prob-
58C30	Fixed point theorems on manifolds		lems in two independent variables)
	[See also 47H10]		[See also 49Q05]
58C35	Integration on manifolds; measures on manifolds [See also 28Cxx]	58E15	Application to extremal problems ir several variables; Yang-Mills functionals
58C40	Spectral theory; eigenvalue problems [See also 47J10, 58E07]	58E17	[See also 81T13], etc. Pareto optimality, etc., applications to
58C50	Analysis on supermanifolds or graded manifolds	58E20	economics [See also 90C29] Harmonic maps [See also 53C43], etc.
58C99	None of the above, but in this section	58E25	Applications to control theory
	0 1 (11 () ([See also 49-XX, 93-XX]
58DXX	Spaces and manifolds of mappings (in-	58E30	Variational principles
	cluding nonlinear versions of 46Exx) [See also 46Txx, 53Cxx]	58E35	Variational inequalities
58D05	Groups of diffeomorphisms and homeo-	58E40	(global problems) Group actions
	morphisms as manifolds [See also 22E65,	58E50	Applications
	57S05]		None of the above, but in this section

		58J60	Relations with special manifold struc-
58Hxx	Pseudogroups, differentiable groupo-		tures
	ids and general structures on manifolds		(Riemannian, Finsler, etc.)
58H05	Pseudogroups and differentiable groupoids [See also 22A22, 22E65]	58J65	Diffusion processes and stochastic analysis on manifolds
58H10	Cohomology of classifying spaces		[See also 35R60, 60H10, 60J60]
	for pseudogroup structures (Spencer, Gelfand-Fuks, etc.) [See also 57R32]	58J70	Invariance and symmetry properties [See also 35A30]
58H15	Deformations of structures [See also 32Gxx, 58J10]	58J72	Correspondences and other transformation methods (e.g. Lie-Bäcklund)
58H99	None of the above, but in this section	58J90	[See also 35A22] Applications
58Jxx	Partial differential equations on mani-	58J99	None of the above, but in this section
<i>30jxx</i>	folds; differential operators		
	[See also 32Wxx, 35-XX, 53Cxx]	58Kxx	Theory of singularities and catastrophe
58J05	Elliptic equations on manifolds, general		theory [See also 32Sxx, 37-XX]
	theory [See also 35-XX]	58K05	Critical points of functions and
58J10	Differential complexes [See also 35Nxx];		mappings
	elliptic complexes	58K10	Monodromy
58J15	Relations with hyperfunctions		Topological properties of mappings
58J20	Index theory and related fixed point theorems [See also 19K56, 46L80]	58K20	Algebraic and analytic properties of mappings
58J22	Exotic index theories [See also 19K56,	58K25	Stability
	46L05, 46L10, 46L80, 46M20]	58K30	Global theory
58J26	Elliptic genera	58K35	Catastrophe theory
58J28	Eta-invariants, Chern-Simons invariants	58K40	Classification; finite determinacy of map
58J30	Spectral flows		germs
58J32	Boundary value problems on manifolds	58K45	Singularities of vector fields, topological
58J35	Heat and other parabolic equation meth-		aspects
58J37	ods Perturbations; asymptotics		Normal forms
58J40	Pseudodifferential and Fourier integral		Asymptotic behavior
30,40	operators on manifolds [See also 35Sxx]		Deformation of singularities
58J42	Noncommutative global analysis, non-		Topological invariants
00,12	commutative residues		Symmetries, equivariance
58J45	Hyperbolic equations [See also 35Lxx]	58K99	None of the above, but in this section
58J47	Propagation of singularities; initial value problems	58Zxx	Applications to physics
58J50	Spectral problems; spectral geometry;	58Z05	Applications to physics
-	scattering theory [See also 35Pxx]	58 Z 99	None of the above, but in this section
58J51	Relations between spectral theory and ergodic theory, e.g. quantum unique ergodicity		
58J52	Determinants and determinant bundles, analytic torsion		
58J53	Isospectrality		
58J55	Bifurcation [See also 35B32]		

60-YY	(Probability theory and stochas-		
00-XX	tic processes (For additional applications, see 11Kxx, 62-XX, 90-		Geometric probability and stochastic geometry [See also 52A22, 53C65]
	XX, 91-XX, 92-XX, 93-XX, 94-XX)	601005	Geometric probability and stochastic geometry [See also 52A22, 53C65]
60-00	General reference works (handbooks, dictionaries, bibliographies, etc.)	60D99	None of the above, but in this section
60-01	Instructional exposition (textbooks, tutorial papers, etc.)	60Exx	Distribution theory [See also 62Exx, 62Hxx]
60-02	Research exposition (monographs, survey articles)	60E05	Distributions: general theory
60-03	Historical (must also be assigned at least one classification number from Section 01)		Infinitely divisible distributions; stable distributions Characteristic functions;
60-04	Explicit machine computation and programs (not the theory of computation or programming)	60E15 60E99	other transforms Inequalities; stochastic orderings None of the above, but in this section
60-06 60-08	Proceedings, conferences, collections, etc. Computational methods (not classified at a more specific level) [See also 65C50]	60F05	Limit theorems [See also 28Dxx, 60B12] Central limit and other weak theorems Large deviations
60 A v v			Strong theorems
60A05	Axioms; other general questions	60F17	Functional limit theorems; invariance principles
60A10	Probabilistic measure theory (For ergodic theory, see 28Dxx and 60Fxx)	60F20 60F25	Zero-one laws L^p -limit theorems
	Fuzzy probability None of the above, but in this section	60F99	None of the above, but in this section
60Bxx	Probability theory on algebraic and		Stochastic processes
60B05	topological structures Probability measures on topological	60G07	Foundations of stochastic processes General theory of processes
60 R 10	spaces		Exchangeability Stationary processes
60B10 60B11	Convergence of probability measures Probability theory on linear topological spaces [See also 28C20]	60G12	General second-order processes Gaussian processes
60B12	Limit theorems for vector-valued ran- dom variables (infinite-dimensional case)	60G17 60G18	Sample path properties Self-similar processes
60B15	Probability measures on groups or semi- groups, Fourier transforms, factoriza-	60G22	Generalized stochastic processes Fractional processes, including fractional Brownian motion
60B20	tion Random matrices (probabilistic aspects; for algebraic aspects see 15B52)		Prediction theory [See also 62M20] Continuity and singularity of induced measures
60B99	None of the above, but in this section	60G35	Signal detection and filtering [See also 62M20, 93E10, 93E11, 94Axx]
60C05	Combinatorial probability Combinatorial probability None of the above, but in this section	60G40	Stopping times; optimal stopping prob- lems; gambling theory [See also 62L15, 91A60]
	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	60G42	Martingales with discrete parameter

	Martingales with continuous parameter	60J28	Applications of continuous-time Mar-
	Martingales and classical analysis Generalizations of martingales	60J35	kov processes on discrete state spaces Transition functions, generators and re-
	Sums of independent random variables;	00,00	solvents [See also 47D03, 47D07]
	random walks	60J40	Right processes
60G51	Processes with independent increments;	60J45	Probabilistic potential theory
	Lévy processes		[See also 31Cxx, 31D05]
60G52	Stable processes	60J50	Boundary theory
60G55	Point processes	60J55	Local time and additive functionals
60G57	Random measures	60J57	Multiplicative functionals
60G60	Random fields	60J60	Diffusion processes [See also 58J65]
60G70	Extreme value theory;	60J65	Brownian motion [See also 58J65]
	extremal processes	60J67	Stochastic (Schramm-)Loewner
60G99	None of the above, but in this section		evolution (SLE)
		60J68	Superprocesses
60Hxx	Stochastic analysis [See also 58J65]	60J70	Applications of Brownian motions and
60H05	Stochastic integrals		diffusion theory (population genetics,
60H07	Stochastic calculus of variations and the		absorption problems, etc.) [See also 92Dxx]
60H10	Malliavin calculus	60J75	Jump processes
001110	Stochastic ordinary differential equations [See also 34F05]	60J80	Branching processes (Galton-Watson,
60H15	Stochastic partial differential equations		birth-and-death, etc.)
	[See also 35R60]	60J85	Applications of branching processes
60H20	Stochastic integral equations		[See also 92Dxx]
60H25	Random operators and equations [See also 47B80]	60J99 	None of the above, but in this section
60H30	Applications of stochastic analysis	60Kxx	Special processes
	(to PDE, etc.)	60K05	Renewal theory
60H35	Computational methods for stochastic	60K10	Applications
(01140	equations [See also 65C30]		(reliability, demand theory, etc.)
		COT/15	· · · · · · · · · · · · · · · · · · ·
ひいコララ	White noise theory	60K15	Markov renewal processes,
	None of the above, but in this section		Markov renewal processes, semi-Markov processes
	None of the above, but in this section		Markov renewal processes, semi-Markov processes Applications of Markov renewal pro-
60Jxx	None of the above, but in this section Markov processes		Markov renewal processes, semi-Markov processes Applications of Markov renewal pro- cesses (reliability, queueing networks,
	None of the above, but in this section Markov processes Discrete-time Markov processes on	60K20	Markov renewal processes, semi-Markov processes Applications of Markov renewal pro- cesses (reliability, queueing networks, etc.) [See also 90Bxx]
60Jxx 60J05	Markov processes Discrete-time Markov processes on general state spaces	60K20	Markov renewal processes, semi-Markov processes Applications of Markov renewal pro- cesses (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory
60Jxx	None of the above, but in this section Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov	60K20 60K25	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation,
60Jxx 60J05	None of the above, but in this section Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces)	60K20 60K25 60K30	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx]
60Jxx 60J05 60J10	None of the above, but in this section Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov	60K20 60K25 60K30	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical
60Jxx 60J05 60J10	Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces) Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learn-	60K20 60K25 60K30	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical mechanics type models; percolation the-
60Jxx 60J05 60J10	Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces) Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.)	60K25 60K30 60K35	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43]
60Jxx 60J05 60J10 60J20	Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces) Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.) [See also 90B30, 91D10, 91D35, 91E40]	60K25 60K30 60K35 60K37	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43] Processes in random environments
60Jxx 60J05 60J10	Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces) Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.)	60K25 60K30 60K35 60K37	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43]
60Jxx 60J05 60J10 60J20	Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces) Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.) [See also 90B30, 91D10, 91D35, 91E40] Computational methods in Markov	60K25 60K30 60K35 60K37 60K40	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43] Processes in random environments Other physical applications of random
60Jxx 60J05 60J10 60J20	Markov processes Discrete-time Markov processes on general state spaces Markov chains (discrete-time Markov processes on discrete state spaces) Applications of Markov chains and discrete-time Markov processes on general state spaces (social mobility, learning theory, industrial processes, etc.) [See also 90B30, 91D10, 91D35, 91E40] Computational methods in Markov chains [See also 65C40]	60K25 60K30 60K35 60K37 60K40	Markov renewal processes, semi-Markov processes Applications of Markov renewal processes (reliability, queueing networks, etc.) [See also 90Bxx] Queueing theory [See also 68M20, 90B22] Applications (congestion, allocation, storage, traffic, etc.) [See also 90Bxx] Interacting random processes; statistical mechanics type models; percolation theory [See also 82B43, 82C43] Processes in random environments Other physical applications of random processes

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62-XX	(Statistics	62D99	None of the above, but in this section
62-00	General reference works (handbooks,	62Fyy	Distribution theory [See also 60Exx]
	dictionaries, bibliographies, etc.)		Characterization and structure theory
62-01	Instructional exposition		Exact distribution theory
60.00	(textbooks, tutorial papers, etc.)		Approximations to distributions
62-02	Research exposition (monographs, survey articles)	02117	(nonasymptotic)
62-03	Historical (must also be assigned at least	62E20	Asymptotic distribution theory
02 00	one classification number from Section 01)		Fuzziness in connection with the topics on distributions in this section
62-04	Explicit machine computation and programs (not the theory of computation or	62E99	None of the above, but in this section
	programming)	62Fxx	Parametric inference
62-06	Proceedings, conferences, collections,	62F03	Hypothesis testing
60.05	etc.	62F05	Asymptotic properties of tests
62-07	Data analysis	62F07	Ranking and selection
62-09	Graphical methods	62F10	Point estimation
		62F12	Asymptotic properties of estimators
	Foundational and philosophical topics	62F15	Bayesian inference
	Foundations and philosophical topics	62F25	Tolerance and confidence regions
	Fuzzy analysis in statistics	62F30	Inference under constraints
62A99	None of the above, but in this section	62F35	Robustness and adaptive procedures
62Byy	Sufficiency and information	62F40	Bootstrap, jackknife and other
	Sufficient statistics and fields	62F86	resampling methods Parametric inference and fuzziness
	Information-theoretic topics		
02210	[See also 94A17]	02599	None of the above, but in this section
62B15	Theory of statistical experiments	62Gyy	Nonparametric inference
62B86	Fuzziness, sufficiency, and information		Estimation
62B99	None of the above, but in this section		Density estimation
			Nonparametric regression
62Cxx	Decision theory [See also 90B50, 91B06;		Resampling methods
	for game theory, see 91A35]		Hypothesis testing
	General considerations		Tolerance and confidence regions
	Complete class results		Asymptotic properties
62C10	Bayesian problems; characterization of Bayes procedures		Order statistics; empirical distribution
62C12	Empirical decision procedures;		functions
02012	empirical Bayes procedures		Statistics of extreme values; tail inference
62C15	Admissibility		Robustness
	Minimax procedures		Nonparametric inference and fuzziness
	Compound decision problems	62G99	None of the above, but in this section
	Decision theory and fuzziness		
	None of the above, but in this section		Multivariate analysis [See also 60Exx]
			Characterization and structure theory
62Dxx	Sampling theory, sample surveys		Distribution of statistics
	Sampling theory, sample surveys	62H11	Directional data; spatial statistics

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62H12	Estimation	62M05	Markov processes: estimation
62H15	Hypothesis testing	62M07	Non-Markovian processes:
	Contingency tables		hypothesis testing
62H20	Measures of association	62M09	Non-Markovian processes: estimation
	(correlation, canonical correlation, etc.)	62M10	Time series, auto-correlation, regression,
62H25	Factor analysis and principal compo-		etc. [See also 91B84]
	nents; correspondence analysis		Spectral analysis
62H30	Classification and discrimination;	62M20	Prediction [See also 60G25]; filtering
	cluster analysis [See also 68T10, 91C20]		[See also 60G35, 93E10, 93E11]
62H35	Image analysis		Spatial processes
62H86	Multivariate analysis and fuzziness		Random fields; image analysis
62H99	None of the above, but in this section		Neural nets and related approaches
		62M86	Inference from stochastic processes and
62Jxx	Linear inference, regression	621/100	fuzziness None of the above, but in this section
62J02	General nonlinear regression	0210199	None of the above, but in this section
62J05	Linear regression	62NIva	Curringlandrysis and concound data
62J07	Ridge regression; shrinkage estimators		Survival analysis and censored data Censored data models
62J10	Analysis of variance and covariance		Estimation
62J12	Generalized linear models		Testing
62J15	Paired and multiple comparisons		8
62J20	Diagnostics	021103	Reliability and life testing [See also 90B25]
62J86	Fuzziness, and linear inference	62N86	Fuzziness, and survival analysis and
	and regression	0 100	censored data
(O T O O			cerisorea data
62J99	None of the above, but in this section	62N99	None of the above, but in this section
			None of the above, but in this section
62Kxx	Design of experiments [See also 05Bxx]		None of the above, but in this section Applications
62Kxx 62K05	Design of experiments [See also 05Bxx] Optimal designs	62Pxx	None of the above, but in this section Applications [See also 90-XX, 91-XX, 92-XX]
62Kxx 62K05 62K10	Design of experiments [See also 05Bxx] Optimal designs Block designs		None of the above, but in this section Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and
62Kxx 62K05 62K10 62K15	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs	62Pxx 62P05	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics
62Kxx 62K05 62K10 62K15 62K20	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs	62Pxx	None of the above, but in this section Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and
62Kxx 62K05 62K10 62K15 62K20 62K25	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs	62Pxx 62P05	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments	62Pxx 62P05 62P10 62P12	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs	62Pxx 62P05 62P10 62P12 62P15	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section	62Pxx 62P05 62P10 62P12 62P15	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods	62Pxx 62P05 62P10 62P12 62P15 62P20	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx]
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis Sequential estimation	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry Applications to physics
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12 62L15	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis Sequential estimation Optimal stopping	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12 62L15	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis Sequential estimation Optimal stopping [See also 60G40, 91A60]	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30 62P35 62P99	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry Applications to physics None of the above, but in this section
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12 62L15	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis Sequential estimation Optimal stopping [See also 60G40, 91A60] Stochastic approximation	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30 62P35 62P99	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry Applications to physics None of the above, but in this section Statistical tables
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12 62L15	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis Sequential estimation Optimal stopping [See also 60G40, 91A60] Stochastic approximation Fuzziness and sequential methods	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30 62P35 62P99	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry Applications to physics None of the above, but in this section Statistical tables Statistical tables
62Kxx 62K05 62K10 62K15 62K20 62K25 62K86 62K99 62Lxx 62L05 62L10 62L12 62L15 62L20 62L86 62L99	Design of experiments [See also 05Bxx] Optimal designs Block designs Factorial designs Response surface designs Robust parameter designs Fuzziness and design of experiments None of the above, but in this section Sequential methods Sequential design Sequential analysis Sequential estimation Optimal stopping [See also 60G40, 91A60] Stochastic approximation Fuzziness and sequential methods	62Pxx 62P05 62P10 62P12 62P15 62P20 62P25 62P30 62P35 62P99	Applications [See also 90-XX, 91-XX, 92-XX] Applications to actuarial sciences and financial mathematics Applications to biology and medical sciences Applications to environmental and related topics Applications to psychology Applications to economics [See also 91Bxx] Applications to social sciences Applications in engineering and industry Applications to physics None of the above, but in this section Statistical tables

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65-XX	(Numerical analysis	65Dxx	Numerical approximation and com-
65-00	General reference works (handbooks, dictionaries, bibliographies, etc.)		putational geometry (primarily algorithms) (For theory, see 41-XX and 68Uxx)
65-01	Instructional exposition	65D05	Interpolation
(5.00	(textbooks, tutorial papers, etc.)		Splines
65-02	Research exposition (monographs, survey articles)		Smoothing, curve fitting
65-03			Algorithms for functional approxima-
03-03	Historical (must also be assigned at least one classification number from Section		tion
	01)	65D17	Computer aided design (modeling of
65-04	Explicit machine computation and pro-	(F D10	curves and surfaces) [See also 68U07]
	grams (not the theory of computation or	65D18	Computer graphics, image analysis, and computational geometry
	programming)		[See also 51N05, 68U05]
65-05	Experimental papers	65D19	Computational issues in computer and
65-06	Proceedings, conferences, collections,		robotic vision
	etc.	65D20	Computation of special functions, con-
	Tables	(=5.4=	struction of tables [See also 33F05]
	Tables		Numerical differentiation
65A99	None of the above, but in this section		Numerical integration
(FD	A see Leve Compact comments and		Quadrature and cubature formulas
	Acceleration of convergence	65D99	None of the above, but in this section
03003	Extrapolation to the limit, deferred corrections	6EEras	Nivers and seal are of the dealers as a sealers
65B10	Summation of series	OSEXX	Numerical methods in complex analysis (potential theory, etc.) (For numeri-
65B15	Euler-Maclaurin formula		cal methods in conformal mapping, see
65B99	None of the above, but in this section		also 30C30)
		65E05	Numerical methods in complex analy-
65Cxx	Probabilistic methods, simulation and		sis (potential theory, etc.) For numerical
	stochastic differential equations (For		methods in conformal mapping, see also 30C30
	theoretical aspects, see 68U20 and	65E99	None of the above, but in this section
65C05	60H35) Monte Carlo methods		, a same and a same
	Random number generation	65Fxx	Numerical linear algebra
	Models, numerical methods		Direct methods for linear systems and
00 020	[See also 68U20]		matrix inversion
65C30	Stochastic differential and integral equa-	65F08	Preconditioners for iterative methods
	tions	65F10	Iterative methods for linear systems
65C35	Stochastic particle methods	65F15	[See also 65N22] Eigenvalues, eigenvectors
6EC40	[See also 82C80]	65F18	Inverse eigenvalue problems
	Computational Markov chains	65F20	Overdetermined systems,
63C30	Other computational problems in probability	031 20	pseudoinverses
65C60	Computational problems in statistics	65F22	Ill-posedness, regularization
65C99	None of the above, but in this section	65F25	Orthogonalization
		65F30	Other matrix algorithms
		65F35	Matrix norms, conditioning, scaling [See also 15A12, 15A60]
		65F40	Determinants

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65F50	Sparse matrices	65L04	Stiff equations
65F60	Matrix exponential and similar matrix		Initial value problems
	functions		Multistep, Runge-Kutta and
65F99	None of the above, but in this section		extrapolation methods
		65L07	Numerical investigation of stability of
	Error analysis and interval analysis		solutions
65G20	Algorithms with automatic result verifi-		Improperly posed problems
65C30	cation Interval and finite arithmetic	65L09	1
	General methods in interval analysis		Boundary value problems
	Roundoff error	65L11	0 11 1
	None of the above, but in this section		Finite difference methods
000)	Trone of the above, but in this section		Eigenvalue problems
65Hxx	Nonlinear algebraic or transcendental	65L20	Stability and convergence of numerical methods
OOTIAA	equations	65L50	Mesh generation and refinement
65H04	Roots of polynomial equations	65L60	Finite elements, Rayleigh-Ritz, Galerkir
	Single equations		and collocation methods
65H10	Systems of equations	65L70	Error bounds
	Eigenvalues, eigenvectors [See also	65L80	Methods for differential-algebraic equa-
(- 7.700	47Hxx, 47Jxx, 58C40, 58E07, 90C30]	651.99	None of the above, but in this section
65H20	Global methods, including homotopy approaches [See also 58C30, 90C30]		Twolle of the above, but in this section
65H99	None of the above, but in this section	65Mxx	Partial differential equations, initial value and time-dependent initial
65Jxx	Numerical analysis in abstract spaces		boundary value problems
65J05	General theory	65M06	Finite difference methods
65J08	Abstract evolution equations	65M08	Finite volume methods
65J10	Equations with linear operators	65M12	Stability and convergence of numerical
00,10	(do not use 65Fxx)	6EN/1E	methods
65J15	Equations with nonlinear operators		Error bounds
-	(do not use 65Hxx)		Method of lines
65J20	Improperly posed problems; regulariza-	031V122	Solution of discretized equations [See also 65Fxx, 65Hxx]
65122	tion Inverse problems	65M25	Method of characteristics
	None of the above, but in this section	65M30	Improperly posed problems
00,77	Trone of the above, but in this section	65M32	Inverse problems
65Kyy	Mathematical programming, optimiza-	65M38	Boundary element methods
ODICAX	tion and variational techniques	65M50	Mesh generation and refinement
65K05	Mathematical programming methods	65M55	Multigrid methods; domain decomposi-
	[See also 90Cxx]	65M60	tion Finite elements Rayleigh-Ritz and
65K10	Optimization and variational techniques [See also 49Mxx, 93B40]	031 v1 00	Finite elements, Rayleigh-Ritz and Galerkin methods, finite methods
65K15	Numerical methods for variational in-	65M70	Spectral, collocation and related meth-
	equalities and related problems	(F) (77	ods
65K99	None of the above, but in this section	021/1/2	Probabilistic methods, particle methods etc.
		65M80	Fundamental solutions, Green's func-
65Lxx	Ordinary differential equations	222,100	tion methods, etc.
	Functional-differential equations	(F) (OF	Fictitious domain mothods

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65M99	None of the above, but in this section	65Rxx	Integral equations, integral transforms
		65R10	Integral transforms
65Nxx	Partial differential equations, bound- ary value problems	65R20	Integral equations
65NI06	Finite difference methods	65R30	Improperly posed problems
	Finite volume methods	65R32	Inverse problems
	Stability and convergence of numerical	65R99	None of the above, but in this section
031112	methods		
65N15	Error bounds	65Sxx	Graphical methods
65N20	Ill-posed problems	65S05	Graphical methods
65N21	Inverse problems	65S99	None of the above, but in this section
65N22	Solution of discretized equations		
	[See also 65Fxx, 65Hxx]	65Txx	Numerical methods in Fourier analysis
65N25	Eigenvalue problems	65T40	0 11
65N30	Finite elements, Rayleigh-Ritz and		polation
	Galerkin methods, finite methods		Discrete and fast Fourier transforms
65N35	Spectral, collocation and related meth-		Wavelets
6EN129	ods Roundamy element methods	65T99	None of the above, but in this section
	Boundary element methods Method of lines		
		65Yxx	Computer aspects of
	Method of contraction of the boundary	(F)/04	numerical algorithms
	Mesh generation and refinement	65 Y U4	Algorithms for computer arithmetic, etc. [See also 68M07]
031133	Multigrid methods; domain decomposition	65Y05	Parallel computation
65N75	Probabilistic methods, particle methods,		Algorithms for specific classes of archi-
	etc.	03110	tectures
65N80	Fundamental solutions, Green's func-	65Y15	Packaged methods
(F) 10 F	tion methods, etc.	65Y20	Complexity and performance of numer-
	Fictitious domain methods		ical algorithms [See also 68Q25]
65N99	None of the above, but in this section	65Y99	None of the above, but in this section
65Pxx	Numerical problems in dynamical sys-	65Zxx	Applications to physics
	tems [See also 37Mxx]		Applications to physics
65P10	Hamiltonian systems including sym-		None of the above, but in this section
65P20	plectic integrators Numerical chaos		Computer science (For papers in-
	Bifurcation problems	00-A	volving machine computations
	Nonlinear stabilities		and programs in a specific math-
			ematical area, see Section -04 in
03199	None of the above, but in this section		that area)
65Oxx	Difference and functional equations,	68-00	General reference works (handbooks,
00 Q	recurrence relations		dictionaries, bibliographies, etc.)
65Q10	Difference equations	68-01	Instructional exposition
	Functional equations	(0.0 2	(textbooks, tutorial papers, etc.)
	Recurrence relations	68-02	Research exposition (monographs,
-	None of the above, but in this section	60.02	survey articles)
~	,	68-03	Historical (must also be assigned at least one classification number from Section 01)

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68-04	Explicit machine computation and pro-		
	grams (not the theory of computation or programming)		Theory of computing
68-06	Proceedings, conferences, collections,	-	General
00-00	etc.	68Q05	Models of computation (Turing machines, etc.)
68Mvv			[See also 03D10, 68Q12, 81P68]
	Computer system organization General	68O10	Modes of computation (nondetermin
	Mathematical problems of computer ar-	~~~	istic, parallel, interactive, probabilistic
0011107	chitecture		etc.) [See also 68Q85]
68M10	Network design and communication [See also 68R10, 90B18]	68Q12	Quantum algorithms and complexity [See also 68Q05, 81P68]
68M11	Internet topics [See also 68U35]	68Q15	Complexity classes (hierarchies, rela
	Network protocols		tions among complexity classes, etc.
68M14	Distributed systems	49 <u>0</u> 17	[See also 03D15, 68Q17, 68Q19]
68M15	Reliability, testing and fault tolerance	68Q17	Computational difficulty of problems (lower bounds, completeness, difficulty
	[See also 94C12]		of approximation, etc.) [See also 68Q15]
68M20	Performance evaluation; queueing; scheduling [See also 60K25, 90Bxx]	68Q19	Descriptive complexity and finite models [See also 03C13]
68M99	None of the above, but in this section	68Q25	Analysis of algorithms and problem
68Nxx	Software	68020	complexity [See also 68W40]
	General	06Q30	Algorithmic information theory (Kolmo gorov complexity, etc.) [See also 03D32]
68N15	Programming languages	68O32	Computational learning theory
	Logic programming	00 202	[See also 68T05]
	Functional programming and lambda	68Q42	Grammars and rewriting systems
	calculus [See also 03B40]		Formal languages and automata
68N19	Other programming techniques (object-		[See also 03D05, 68Q70, 94A45]
	oriented, sequential, concurrent, auto-	68Q55	Semantics [See also 03B70, 06B35, 18C50
68NI20	matic, etc.)	68Q60	Specification and verification
	Compilers and interpreters		(program logics, model checking, etc.)
	Operating systems Mathematical aspects of software engi-	68065	[See also 03B70] Abstract data types; algebraic specifica
001130	neering (specification, verification, met-	00000	tion [See also 18C50]
	rics, requirements, etc.)	68Q70	Algebraic theory of languages and au
68N99	None of the above, but in this section	~	tomata [See also 18B20, 20M35]
		68Q80	Cellular automata [See also 37B15]
68Pxx	Theory of data	68Q85	Models and methods for concurrent and
68P01	General		distributed computing (process alge-
68P05	Data structures	(9097	bras, bisimulation, transition nets, etc.)
68P10	Searching and sorting	66Q67	Probability in computer science (algorithm analysis, random structures
68P15	Database theory		phase transitions, etc.) [See also 68W20
68P20	Information storage and retrieval		68W40]
	Data encryption [See also 94A60, 81P94]	68Q99	None of the above, but in this section
68P30	Coding and information theory (com-		
	paction, compression, models of com-	68Rxx	Discrete mathematics in relation to
	munication, encoding schemes, etc.) [See also 94Axx]	(0705	computer science
	F	68R()1	General

68R01 General

68P99 None of the above, but in this section

	Combinatorics	68Wxx	Algorithms (For numerical algorithms
68R10	Graph theory (including graph drawing) [See also 05Cxx, 90B10, 90B35, 90C35]		see 65-XX; for combinatorics and graph theory, see 05C85, 68Rxx)
68R15	Combinatorics on words	68W01	General
68R99	None of the above, but in this section	68W05	Nonnumerical algorithms
			Parallel algorithms
	Artificial intelligence	68W15	Distributed algorithms
68T01	General	68W20	Randomized algorithms
68T05	Learning and adaptive systems [See also 68Q32, 91E40]		Approximation algorithms Online algorithms
68T10	Pattern recognition, speech recognition (For cluster analysis, see 62H30)		Symbolic computation and algebraic computation [See also 11Yxx, 12Y05
68T15	Theorem proving (deduction, resolution, etc.) [See also 03B35]	6911122	13Pxx, 14Qxx, 16Z05, 17-08, 33F10]
68T20	Problem solving		Algorithms on strings VLSI algorithms
	(heuristics, search strategies, etc.)		C
68T27	Logic in artificial intelligence		Analysis of algorithms [See also 68Q25] None of the above, but in this section
68T30	Knowledge representation	-	
68T35	Languages and software systems (knowledge-based systems, expert systems, etc.)	70-XX	Mechanics of particles and systems (For relativistic mechanics see 83A05 and 83C10; for statistics
68T37	Reasoning under uncertainty		cal mechanics, see 82-XX)
68T40	Robotics [See also 93C85]	70-00	General reference works (handbooks,
	Agent technology	7 0.01	dictionaries, bibliographies, etc.)
68T45	Machine vision and	70-01	Instructional exposition (textbooks, tutorial papers, etc.)
	scene understanding	70-02	
68T50	Natural language processing [See also 03B65]		Research exposition (monographs, survey articles)
68T99	None of the above, but in this section	70-03	Historical (must also be assigned at leasone classification number from Section
68Uxx	Computing methodologies and applications	70-04	01) Explicit machine computation and pro-
681 101	General		grams (not the theory of computation or
	Computer graphics; computational		programming)
00000	geometry [See also 65D18]	70-05	Experimental work
68U07	Computer-aided design [See also 65D17]	70-06	Proceedings, conferences, collections,
	Image processing	70-08	etc. Computational methods
68U15	Text processing;	70 00	Companional methods
	mathematical typography	70Axx	Axiomatics, foundations
68U20	Simulation [See also 65Cxx]		Axiomatics, foundations
68U35	Information systems (hypertext navigation, interfaces, decision support, etc.)		None of the above, but in this section
681 100	[See also 68M11] None of the above, but in this section	70Bxx	Kinematics [See also 53A17]
00099	rotic of the above, but in this section		Kinematics of a particle
			Kinematics of a rigid body
			Mechanisms, robots
			[See also 68T40, 70Q05, 93C85]

<i>7</i> 0			Wechanics of particles and systems
70B99	None of the above, but in this section	70G45	Differential-geometric methods (tensors, connections, symplectic, Poisson, con-
70Cxx	Statics		tact, Riemannian, nonholonomic, etc.)
70C20	Statics	5 0.055	[See also 53Cxx, 53Dxx, 58Axx]
70C99	None of the above, but in this section		Algebraic geometry methods
			Dynamical systems methods
70Exx	Dynamics of a rigid body and of	70G65	Symmetries, Lie-group and Lie-algebra
	multibody systems	70G70	methods Functional-analytic methods
70E05	Motion of the gyroscope		Variational methods
70E15	Free motion of a rigid body [See also 70M20]		None of the above, but in this section
70E17	Motion of a rigid body with a fixed point		TT 11. 1 1 1 1
70E18	Motion of a rigid body in contact with a solid surface [See also 70F25]		Hamiltonian and Lagrangian mechanics [See also 37Jxx]
70E20	Perturbation methods for rigid body dy-		Lagrange's equations
	namics		Hamilton's equations
	Integrable cases of motion	70H06	Completely integrable systems and
	Higher-dimensional generalizations	701107	methods of integration
70E50	Stability problems		Nonintegrable systems Nearly integrable Hamiltonian systems,
70E55	Dynamics of multibody systems	701100	KAM theory
70E60	Robot dynamics and control [See also 68T40, 70Q05, 93C85]	70H09	Perturbation theories
70E99			Adiabatic invariants
, 02,	Trone of the above, but in this section		Periodic and almost periodic solutions
70Fxx	Dynamics of a system of particles, in-		Stability problems
	cluding celestial mechanics		Canonical and symplectic
70F05	Two-body problems		transformations
70F07	Three-body problems		Hamilton-Jacobi equations
70F10	<i>n</i> -body problems		Hamilton's principle
70F15	Celestial mechanics		Other variational principles
70F16	Collisions in celestial mechanics, regularization	70H33	Symmetries and conservation laws, reverse symmetries, invariant manifolds
70F17	Inverse problems	701140	and their bifurcations, reduction
70F20	Holonomic systems		Relativistic dynamics
70F25	Nonholonomic systems	70H45	Constrained dynamics, Dirac's theory of constraints [See also 70F20, 70F25,
70F35	Collision of rigid or pseudo-rigid bodies		70Gxx]
70F40	Problems with friction	70H50	Higher-order theories
70F45	Infinite particle systems		None of the above, but in this section
70F99	None of the above, but in this section		, and the same of
		70Jxx	Linear vibration theory
70Gxx	General models, approaches, and	70J10	Modal analysis
	methods [See also 37-XX]	70J25	Stability
70G10	Generalized coordinates; event, impul-	70J30	Free motions
	-		
	se-energy, configuration, state, or phase	70J35	Forced motions
70 <i>C4</i> 0	se-energy, configuration, state, or phase space	70J35 70J40	Forced motions Parametric resonances
70G40	se-energy, configuration, state, or phase		

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70J99	None of the above, but in this section		Yang-Mills and other gauge theories
70Kxx	Nonlinear dynamics	70S20 70S99	More general nonquantum field theories None of the above, but in this section
TOTEXX	[See also 34Cxx, 37-XX]		
70K05	Phase plane analysis, limit cycles	74-XX	Mechanics of deformable
70K20	Stability		solids
70K25	Free motions	74-00	General reference works (handbooks,
70K28	Parametric resonances	74-01	dictionaries, bibliographies, etc.)
70K30	Nonlinear resonances	/ 4- 01	Instructional exposition (textbooks, tutorial papers, etc.)
70K40	Forced motions	74-02	Research exposition (monographs,
70K42	Equilibria and periodic trajectories	, 1 02	survey articles)
70K43	Quasi-periodic motions and invariant tori	74-03	Historical (must also be assigned at least one classification number from Section
70K44	Homoclinic and heteroclinic trajectories		01)
70K45	Normal forms	74-04	Explicit machine computation and pro-
	Bifurcations and instability		grams (not the theory of computation or
70K55	Transition to stochasticity		programming)
7 01//0	(chaotic behavior) [See also 37D45]	74-05	Experimental work
	General perturbation schemes	74-06	Proceedings, conferences, collections,
	Averaging of perturbations		etc.
	Systems with slow and fast motions Nonlinear modes	74Axx	Generalities, axiomatics, foundations
	None of the above, but in this section	74405	of continuum mechanics of solids
70K)	Twolle of the above, but in this section		Kinematics of deformation Stress
	Random vibrations [See also 74H50]	74A15	Thermodynamics
	Random vibrations [See also 74H50]	74A20	Theory of constitutive functions
70L99	None of the above, but in this section	74A25	Molecular, statistical, and kinetic theories
70Myy	Orbital mechanics	74A30	Nonsimple materials
	Orbital mechanics		Polar materials
	None of the above, but in this section	74A40	Random materials and
			composite materials
70Pxx	Variable mass, rockets		Theories of fracture and damage
70P05	Variable mass, rockets	74A50	Structured surfaces and interfaces,
70P99	None of the above, but in this section	74455	coexistent phases
			Theories of friction (tribology)
70Qxx	Control of mechanical systems		Micromechanical theories
5 000 5	[See also 60Gxx, 60Jxx]		Reactive materials
70Q05	Control of mechanical systems [See also 60Gxx, 60Jxx]	74A99	None of the above, but in this section
70Q99	None of the above, but in this section	74Bxx	Elastic materials
			Classical linear elasticity
70Sxx	Classical field theories [See also 37Kxx,		Linear elasticity with initial stresses
70005	37Lxx, 78-XX, 81Txx, 83-XX]	74B15	Equations linearized about a deformed
70S05	Lagrangian formalism and Hamiltonian formalism		state (small deformations superposed on large)
70S10	Symmetries and conservation laws	74B20	Nonlinear elasticity

Mechanics of deformable solids

74B99	None of the above, but in this section	74Gxx	Equilibrium (steady-state) problems
			Explicit solutions
74Cxx	Plastic materials, materials of stress- rate and internal-variable type		Analytic approximation of solutions (perturbation methods, asymptotic
74C05	Small-strain, rate-independent theories		methods, series, etc.)
	(including rigid-plastic and elasto-	74G15	Numerical approximation of solutions
	plastic materials)		Local existence of solutions (near a given
74C10	Small-strain, rate-dependent theories		solution)
	(including theories of viscoplasticity)	74G25	Global existence of solutions
74C15	Large-strain, rate-independent theories	74G30	Uniqueness of solutions
74620	(including nonlinear plasticity)	74G35	Multiplicity of solutions
	Large-strain, rate-dependent theories	74G40	Regularity of solutions
/4C99	None of the above, but in this section	74G45	Bounds for solutions
		74G50	Saint-Venant's principle
74Dxx	Materials of strain-rate type and history type, other materials with mem-		Qualitative behavior of solutions
	ory (including elastic materials with	74G60	Bifurcation and buckling
	viscous damping, various viscoelastic		Energy minimization
	materials)		Stress concentrations, singularities
74D05	Linear constitutive equations		Inverse problems
74D10	Nonlinear constitutive equations		None of the above, but in this section
74D99	None of the above, but in this section		
		74Hxx	Dynamical problems
74Exx	Material properties given special		Explicit solutions
	treatment	74H10	Analytic approximation of solutions
74E05	Inhomogeneity		(perturbation methods, asymptotic
74E10	Anisotropy		methods, series, etc.)
74E15	Crystalline structure	74H15	Numerical approximation of solutions
74E20	Granularity	74H20	Existence of solutions
74E25	Texture		Uniqueness of solutions
74E30	Composite and mixture properties	74H30	Regularity of solutions
74E35	Random structure	74H35	Singularities, blowup,
74E40	Chemical structure	741140	stress concentrations
74E99	None of the above, but in this section		Long-time behavior of solutions
			Vibrations
74Fxx	Coupling of solid mechanics with other		Random vibrations
	effects		Stability
74F05	Thermal effects		Dynamical bifurcation
74F10	Fluid-solid interactions		Chaotic behavior
	(including aero- and hydro-elasticity, porosity, etc.)	74H99	None of the above, but in this section
74F15	Electromagnetic effects	74Jxx	Waves
74F20	Mixture effects	74J05	Linear waves
74F25	Chemical and reactive effects	74J10	Bulk waves
74F99	None of the above, but in this section	74J15	Surface waves
		74J20	Wave scattering
		74J25	Inverse problems

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74J30	Nonlinear waves	74P15	Topological methods
74J35	Solitary waves		Geometrical methods
74J40	Shocks and related discontinuities	74P99	None of the above, but in this section
74J99	None of the above, but in this section		,
,	, a care	74Qxx	Homogenization, determination of
74Kxx	Thin bodies, structures		effective properties
	Strings	74Q05	Homogenization in equilibrium
	Rods (beams, columns, shafts, arches,		problems
	rings, etc.)	74Q10	Homogenization and oscillations in
74K15	Membranes		dynamical problems
74K20	Plates		Effective constitutive equations
74K25	Shells		Bounds on effective properties
74K30	Junctions	74Q99	None of the above, but in this section
74K35	Thin films		
74K99	None of the above, but in this section	74Rxx	Fracture and damage
		74R05	Brittle damage
74Lxx	Special subfields of solid mechanics	74R10	Brittle fracture
74L05	-	74R15	High-velocity fracture
	[See also 86-XX]	74R20	Anelastic fracture and damage
74L10	Soil and rock mechanics	74R99	None of the above, but in this section
74L15	Biomechanical solid mechanics		
	[See also 92C10]	74Sxx	Numerical methods [See also 65-XX]
74L99	None of the above, but in this section		74G15, 74H15]
			Finite element methods
	Special kinds of problems		Finite volume methods
74M05	Control, switches and devices	74S15	Boundary element methods
	("smart materials") [See also 93Cxx]	74S20	Finite difference methods
	Friction	74S25	Spectral and related methods
	Contact	74S30	Other numerical methods
	Impact	74S60	Stochastic methods
74M25	Micromechanics	74S70	Complex variable methods
74M99	None of the above, but in this section	74S99	None of the above, but in this section
		76-XX	(Fluid mechanics
74Nxx	Phase transformations in solids	70 70	(For general continuum mechan-
	[See also 74A50, 80Axx, 82B26, 82C26]		ics, see 74Axx, or other parts of
	Crystals		74-XX)
	Displacive transformations	76-00	General reference works (handbooks,
	Analysis of microstructure	70-00	dictionaries, bibliographies, etc.)
74N20	Dynamics of phase boundaries	76-01	Instructional exposition
74N25	Transformations involving diffusion		(textbooks, tutorial papers, etc.)
74N30	Problems involving hysteresis	76-02	Research exposition (monographs,
74N99	None of the above, but in this section		survey articles)
		76-03	Historical (must also be assigned at least
74Pxx	Optimization [See also 49Qxx]		one classification number from Section
74P05	Compliance or weight optimization		01)
74P10	Optimization of other properties		

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76-04	Explicit machine computation and pro-	76D07	Stokes and related (Oseen, etc.) flows
	grams (not the theory of computation or	76D08	Lubrication theory
5 6.05	programming)		Viscous-inviscid interaction
76-05	Experimental work	76D10	Boundary-layer theory, separation and
76-06	Proceedings, conferences, collections, etc.		reattachment, higher-order effects
			Viscous vortex flows
76Axx	Foundations, constitutive equations,		Wakes and jets
76 4 02	rheology Foundations of fluid mechanics	76D27	Other free-boundary flows; Hele-Shaw flows
	Non-Newtonian fluids	76D33	Waves
	Viscoelastic fluids		Capillarity (surface tension)
	Liquid crystals [See also 82D30]	70210	[See also 76B45]
	Thin fluid films	76D50	Stratification effects in viscous fluids
	Superfluids (classical aspects)	76D55	Flow control and optimization [See also
	None of the above, but in this section		49Q10, 93C20, 93C95]
,011,,	Trong of the above, but in this section	76D99	None of the above, but in this section
76Bxx	Incompressible inviscid fluids		
76B03	Existence, uniqueness, and regularity		Hydrodynamic stability
	theory [See also 35Q35]		Parallel shear flows
76B07	Free-surface potential flows		Convection
76B10	•		Rotation
	streamline theory, water-entry prob-	76E09	Stability and instability of nonparallel flows
	lems, airfoil and hydrofoil theory, sloshing	76E15	
76B15	Water waves, gravity waves; disper-		stability
70013	sion and scattering, nonlinear interac-	76E17	Interfacial stability and instability
	tion [See also 35Q30]		Compressibility effects
76B20	Ship waves	76E20	Stability and instability of geophysical
76B25	Solitary waves [See also 35C11]		andastrophysical flows
76B45	Capillarity (surface tension)	76E25	Stability and instability of magnetohy-
	[See also 76D45]		drodynamic and electrohydrodynamic
	Vortex flows	76E30	flows Nonlinear effects
76B55	Internal waves		None of the above, but in this section
76B60	Atmospheric waves [See also 86A10]	701222	Notic of the above, but in this section
	Rossby waves [See also 86A05, 86A10]	76Evv	Turbulence
	Stratification effects in inviscid fluids	7017.	[See also 37-XX, 60Gxx, 60Jxx]
76B75	Flow control and optimization	76F02	Fundamentals
7/P00	[See also 49Q10, 93C20, 93C95]		Isotropic turbulence;
76B99	None of the above, but in this section		homogeneous turbulence
76Dvv	Incompressible viscous fluids	76F06	Transition to turbulence
	Incompressible viscous fluids Existence, uniqueness, and regularity	76F10	Shear flows
70000	theory [See also 35Q30]	76F20	Dynamical systems approach to turbu-
76D05	Navier-Stokes equations	T/FOF	lence [See also 37-XX]
	[See also 35Q30]	76F25	Turbulent transport, mixing
76D06	Statistical solutions of Navier-Stokes	76F30	Renormalization and other field-theoretical methods [See also 81T99]
	and related equations		icai incurous [occ aiso 01177]
	[See also 60H30, 76M35]		

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76F35	Convective turbulence [See also 76E15, 76Rxx]	76M28	Particle methods and lattice-gas methods
76F40	Turbulent boundary layers	76M30	Variational methods
	Stratification effects	76M35	Stochastic analysis
76F50	Compressibility effects		Complex-variables methods
76F55	Statistical turbulence modeling [See also 76M35]		Asymptotic methods, singular perturbations
76F60	k - ε modeling	76M50	Homogenization
76F65	Direct numerical and large eddy simula-		Dimensional analysis and similarity
	tion of turbulence		Symmetry analysis, Lie group and
76F70	Control of turbulent flows		algebra methods
76F99	None of the above, but in this section	76M99	None of the above, but in this section
76Gxx	General aerodynamics and subsonic flows	76Nxx	Compressible fluids and gas dynamics, general
	General aerodynamics and subsonic flows	76N10	Existence, uniqueness, and regularity theory [See also 35L60, 35L65, 35Q30]
76G99	None of the above, but in this section	76N15	Gas dynamics, general
	T		Viscous-inviscid interaction
	Transonic flows	76N20	Boundary-layer theory
	Transonic flows	76N25	Flow control and optimization
/6H99	None of the above, but in this section		None of the above, but in this section
76Jxx	Supersonic flows	76 Dags	Daniel and Garage Polymore
76J20	Supersonic flows	76FXX	Rarefied gas flows, Boltzmann equation [See also 82B40, 82C40, 82D05]
76J99	None of the above, but in this section		Rarefied gas flows, Boltzmann equation
		76P05	· · · · · · · · · · · · · · · · · · ·
	Hypersonic flows		[See also 82B40, 82C40, 82D05]
76Kxx			· · · · · · · · · · · · · · · · · · ·
76Kxx 76K05	Hypersonic flows	76P99	[See also 82B40, 82C40, 82D05] None of the above, but in this section
76Kxx 76K05	Hypersonic flows Hypersonic flows	76P99 76Qxx	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics
76Kxx 76K05 76K99	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67]	76P99 76Qxx 76Q05	[See also 82B40, 82C40, 82D05] None of the above, but in this section
76Kxx 76K05 76K99	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves	76P99 76Qxx 76Q05 76Q99	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics
76K xx 76K05 76K99 76L xx 76L05	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67]	76P99 76Qxx 76Q05 76Q99 76Rxx	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section
76K xx 76K05 76K99 76L xx 76L05	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection
76Kxx 76K05 76K99 76Lxx 76L05 76L99	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection
76Kxx 76K05 76K99 76Lxx 76L05 76L99	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67]	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection
76Kxx 76K05 76K99 76Lxx 76L05 76L99	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section Basic methods in fluid mechanics	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50 76R99	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection Diffusion [See also 60J60] None of the above, but in this section
76Kxx 76K05 76K99 76Lxx 76L05 76L99 76Mxx 76M10	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section Basic methods in fluid mechanics [See also 65-XX]	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50 76R99	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection Diffusion [See also 60]60] None of the above, but in this section Flows in porous media; filtration;
76Kxx 76K05 76K99 76Lxx 76L05 76L99 76Mxx 76M10 76M12	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section Basic methods in fluid mechanics [See also 65-XX] Finite element methods	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50 76R99	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection Diffusion [See also 60]60] None of the above, but in this section Flows in porous media; filtration; seepage
76Kxx 76K05 76K99 76Lxx 76L05 76L99 76Mxx 76M10 76M12 76M15	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section Basic methods in fluid mechanics [See also 65-XX] Finite element methods Finite volume methods	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50 76R99	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection Diffusion [See also 60J60] None of the above, but in this section Flows in porous media; filtration; seepage Flows in porous media; filtration;
76Kxx 76K05 76K99 76Lxx 76L05 76L99 76Mxx 76M10 76M12 76M15 76M20	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section Basic methods in fluid mechanics [See also 65-XX] Finite element methods Finite volume methods Boundary element methods	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50 76R99 76Sxx	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection Diffusion [See also 60J60] None of the above, but in this section Flows in porous media; filtration; seepage Flows in porous media; filtration; seepage
76Kxx 76K05 76K99 76Lxx 76L05 76L99 76Mxx 76M10 76M12 76M15 76M20 76M22	Hypersonic flows Hypersonic flows None of the above, but in this section Shock waves and blast waves [See also 35L67] Shock waves and blast waves [See also 35L67] None of the above, but in this section Basic methods in fluid mechanics [See also 65-XX] Finite element methods Finite volume methods Boundary element methods Finite difference methods	76P99 76Qxx 76Q05 76Q99 76Rxx 76R05 76R10 76R50 76R99	[See also 82B40, 82C40, 82D05] None of the above, but in this section Hydro- and aero-acoustics Hydro- and aero-acoustics None of the above, but in this section Diffusion and convection Forced convection Free convection Diffusion [See also 60J60] None of the above, but in this section Flows in porous media; filtration; seepage Flows in porous media; filtration;

76M27 Visualization algorithms

76Txx 76T10	Two-phase and multiphase flows Liquid-gas two-phase flows,	78-XX	Optics, electromagnetic theory (For quantum optics, see 81V80)
	bubbly flows	78-00	General reference works (handbooks,
76T15	Dusty-gas two-phase flows	70 00	dictionaries, bibliographies, etc.)
76T20	Suspensions	78-01	Instructional exposition
76T25	Granular flows [See also 74C99, 74E20]		(textbooks, tutorial papers, etc.)
76T30 76T99	Three or more component flows None of the above, but in this section	78-02	Research exposition (monographs, survey articles)
		78-03	Historical (must also be assigned at least
76Uxx	Rotating fluids		one classification number from Section
76U05	Rotating fluids		01)
76U99	None of the above, but in this section	78-04	Explicit machine computation and programs (not the theory of computation or programming)
76Vxx	Reaction effects in flows	78-05	Experimental work
	[See also 80A32]	78-06	Proceedings, conferences, collections,
	Reaction effects in flows [See also 80A32]	70 00	etc.
76 (99	None of the above, but in this section	78Axx	General
76M/vv	Magnetohydrodynamics and electro-	78A02	Foundations
7077 XX	hydrodynamics and electro-	78A05	Geometric optics
76W05	Magnetohydrodynamics and electrohy-		Physical optics
	drodynamics		Electron optics
76W99	None of the above, but in this section		Space charge waves
	•		Electromagnetic theory, general
76Xxx	Ionized gas flow in electromagnetic		Electro- and magnetostatics
	fields; plasmic flow [See also 82D10]		Motion of charged particles
76X05	Ionized gas flow in electromagnetic		Ion traps
	fields; plasmic flow [See also 82D10]		Waves and radiation
76X99	None of the above, but in this section	78A45	Diffraction, scattering [See also 34E20 for WKB methods]
76Yxx	Quantum hydrodynamics and relati-	78A46	Inverse scattering problems
	vistic hydrodynamics		Composite media; random media
	[See also 82D50, 83C55, 85A30]		Antennas, wave-guides
76Y05	Quantum hydrodynamics and relativis-		Technical applications
	tic hydrodynamics		Electrochemistry
76Y99	[See also 82D50, 83C55, 85A30] None of the above, but in this section		Lasers, masers, optical bistability, non-linear optics [See also 81V80]
76Zxx	Biological fluid mechanics	78A70	Biological applications
	[See also 74F10, 74L15, 92Cxx]	70 4 07	[See also 91D30, 92C30]
76Z05	Physiological flows [See also 92C35]	78A97	T
	Biopropulsion in water and in air		electromagnetic theory (must also be assigned at least one other classification
76Z99	None of the above, but in this section		number in this section)
		78A99	Miscellaneous topics
			•

78Mxx Basic methods

78M05 Method of moments

	Finite element methods	80A32	Chemically reacting flows
78M12	Finite volume methods,	90 A E0	[See also 92C45, 92E20]
70) / 1 E	finite integration techniques		Chemistry (general) [See mainly 92Exx] None of the above, but in this section
	Boundary element methods Multipole methods	00A99	None of the above, but in this section
	Finite difference methods	80Mvv	Basic methods
	Spectral methods		Finite element methods
	Other numerical methods		Finite volume methods
	Variational methods		Boundary element methods
	Monte Carlo methods		Finite difference methods
	Neural and heuristic methods		Spectral methods
	Model reduction		Other numerical methods
	Asymptotic analysis		Variational methods
	Homogenization		Monte Carlo methods
	Optimization		Asymptotic analysis
	None of the above, but in this section		Homogenization
	·		Optimization
80-XX	Classical thermodynamics,		None of the above, but in this section
	heat transfer (For thermodynam-	-	
	ics of solids, see 74A15)		Quantum theory
80-00	General reference works (handbooks,	81-00	General reference works (handbooks,
80-01	dictionaries, bibliographies, etc.) Instructional exposition	81-01	dictionaries, bibliographies, etc.) Instructional exposition
00 01	(textbooks, tutorial papers, etc.)	01 01	(textbooks, tutorial papers, etc.)
80-02	Research exposition (monographs, survey articles)	81-02	Research exposition (monographs, survey articles)
80-03	Historical (must also be assigned at least one classification number from Section 01)	81-03	Historical (must also be assigned at least one classification number from Section 01)
80-04	Explicit machine computation and programs (not the theory of computation or programming)	81-04	Explicit machine computation and programs (not the theory of computation or programming)
80-05	Experimental work	81-05	Experimental papers
80-06	Proceedings, conferences, collections,	81-06	Proceedings, conferences, collections,
	etc.	04.00	etc.
80Axx	Thermodynamics and heat transfer	81-08	Computational methods
80A05	Foundations	01 D	A
80A10	Classical thermodynamics,		Axiomatics, foundations, philosophy
	including relativistic		General and philosophical
80A17	Thermodynamics of continua [See also 74A15]	61110	Logical foundations of quantum mechanics; quantum logic [See also 03G12, 06C15]
	Heat and mass transfer, heat flow	81P13	Contextuality
80A22	Stefan problems, phase changes, etc. [See also 74Nxx]	81P15	Quantum measurement theory
80A23	Inverse problems	811716	Quantum state spaces, operational and
80A25	Combustion	Q1 D20	probabilistic concepts Stochastic machanics
80A30	Chemical kinetics [See also 76V05, 92C45, 92E20]	81P20	Stochastic mechanics (including stochastic electrodynamics)

98 Quantum theory

81P40	Quantum coherence, entanglement, quantum correlations	81Rxx	Groups and algebras in quantum theory
81P45	Quantum information, communication, networks [see also 94A15, 94A17]	81R05	Finite-dimensional groups and algebras motivated by physics and their represen-
81P50	Quantum state estimation, approximate cloning	81R10	tations [See also 20C35, 22E70]
81P68	Quantum computation [See also 68Q05, 68Q12]	OIKIU	bras motivated by physics, including Virasoro, Kac-Moody, W-algebras and
81P70	Quantum coding (general)		other current algebras and their repre-
81P94	Quantum cryptography [See also 94A60]		sentations [See also 17B65, 17B67, 22E65,
	None of the above, but in this section		22E67, 22E70]
	,	81R12	Relations with integrable systems
81Qxx	General mathematical topics and meth-	04745	[See also 17Bxx, 37J35]
	ods in quantum theory	81R15	Operator algebra methods
81Q05	Closed and approximate solutions to the	81D20	[See also 46Lxx, 81T05]
	Schrödinger, Dirac, Klein-Gordon and		Covariant wave equations Spinor and twistor methods
81010	other equations of quantum mechanics Selfadjoint operator theory in quantum	011125	[See also 32L25]
	theory, including spectral analysis	81R30	Coherent states [See also 22E45]; squeezed states [See also 81V80]
61Q12	Non-selfadjoint operator theory in quantum theory	81R40	Symmetry breaking
81015	Perturbation theories for operators and	81R50	Quantum groups and related algebraic
01Q10	differential equations		methods [See also 16T20, 17B37]
81Q20	Semiclassical techniques, including	81R60	Noncommutative geometry
~	WKB and Maslov methods	81R99	None of the above, but in this section
81Q30	Feynman integrals and graphs; applica-		
	tions of algebraic topology and algebraic geometry [See also 14D05, 32S40]	81Sxx	General quantum mechanics and prob- lems of quantization
81Q35	Quantum mechanics on special spaces: manifolds, fractals, graphs, etc.	81S05	Canonical quantization, commutation relations and statistics
81Q37	Quantum dots, waveguides, ratchets, etc.	81S10	Geometry and quantization, symplectic methods [See also 53D50]
81Q40	Bethe-Salpeter and other integral equa-	81S20	Stochastic quantization
	tions	81S22	Open systems, reduced dynamics, mas-
	Quantum chaos [See also 37Dxx]		ter equations, decoherence
81Q60	Supersymmetry and quantum mechan-	01005	[See also 82C31]
81065	ics Alternative quantum mechanics		Quantum stochastic calculus
	Differential-geometric methods, includ-	81S30	Phase-space methods including Wigner distributions, etc.
01Q/0	ing holonomy, Berry and Hannay pha-	81S40	Path integrals [See also 58D30]
	ses, etc.	81S99	None of the above, but in this section
81Q80	Special quantum systems, such as solvable systems		
81Q93	Quantum control	811xx	Quantum field theory; related classical field theories [See also 70Sxx]
81Q99	None of the above, but in this section	81T05	Axiomatic quantum field theory; operator algebras
		81T08	Constructive quantum field theory
			Model quantum field theories

81T13	Yang-Mills and other gauge theories [See also 53C07, 58E15]	81V10	Electromagnetic interaction; quantum electrodynamics
81T15	Perturbative methods of renormaliza-	81V15	Weak interaction
04.004.6	tion	81V17	Gravitational interaction
81T16	Nonperturbative methods of renormal-		[See also 83Cxx and 83Exx]
81T17	ization Renormalization group methods		Other fundamental interactions
	Feynman diagrams	81V22	Unified theories
	Quantum field theory on curved space	81V25	Other elementary particle theory
01120	backgrounds		Nuclear physics
81T25	Quantum field theory on lattices		Atomic physics
	Continuum limits		Molecular physics [See also 92E10]
	Thermal quantum field theory		Quantum dots [See also 82D20]
	[see also 82B30]		Many-body theory; quantum Hall effect
81T30	String and superstring theories; other ex-		Quantum optics
	tended objects (e.g., branes)	81V99	None of the above, but in this section
047540	[See also 83E30]	82-XX	Statistical mechanics, structure
81T40	Two-dimensional field theories, conformal field theories, etc.		of matter
81T45	Topological field theories	82-00	General reference works (handbooks,
	[See also 57R56, 58Dxx]	00.01	dictionaries, bibliographies, etc.)
81T50	Anomalies	82-01	Instructional exposition
81T55	Casimir effect	02.02	(textbooks, tutorial papers, etc.)
81T60	Supersymmetric field theories	82-02	Research exposition (monographs, survey articles)
81T70	Quantization in field theory; cohomo-	82-03	Historical (must also be assigned at least
	logical methods [See also 58D29]	02-03	one classification number from Section
81T75	Noncommutative geometry methods		01)
81T80	[See also 46L85, 46L87, 58B34] Simulation and numerical modeling	82-04	Explicit machine computation and pro-
	None of the above, but in this section		grams (not the theory of computation or programming)
		82-05	Experimental papers
81Uxx	Scattering theory [See also 34A55, 34L25, 34L40, 35P25, 47A40]	82-06	Proceedings, conferences, collections, etc.
81U05	2-body potential scattering theory [See also 34E20 for WKB methods]	82-08	Computational methods
81U10	<i>n</i> -body potential scattering theory	82Byy	Equilibrium statistical mechanics
81U15	Exactly and quasi-solvable systems		Foundations
81U20	S-matrix theory, etc.	82B05	
81U30	Dispersion theory, dispersion relations	02000	ics (general)
81U35	Inelastic and multichannel scattering	82B10	
81U40	Inverse scattering problems		chanics (general)
81U99	None of the above, but in this section	82B20	_
81Vxx	Applications to specific physical	82B21	Continuum models
-	systems		(systems of particles, etc.)
81V05	Strong interaction, including	82B23	Exactly solvable models; Bethe ansatz
	quantum chromodynamics		Interface problems;
			diffusion-limited aggregation

82B26	Phase transitions (general)	82C40	Kinetic theory of gases
	Critical phenomena		Dynamics of random walks, random
82B28	Renormalization group methods [See also 81T17]		surfaces, lattice animals, etc. [See also 60G50]
82B30	Statistical thermodynamics [See also 80-XX]	82C43	Time-dependent percolation [See also 60K35]
82B31	Stochastic methods	82C44	Dynamics of disordered systems
82B35	Irreversible thermodynamics, including		(random Ising systems, etc.)
	Onsager-Machlup theory	82C70	Transport processes
	[See also 92E20]	82C80	Numerical methods (Monte Carlo, series
	Kinetic theory of gases	0.000	resummation, etc.)
82B41	Random walks, random surfaces, lattice animals, etc. [See also 60G50, 82C41]	82C99	None of the above, but in this section
	Percolation [See also 60K35]	82Dxx	Applications to specific types of physi-
62D44	Disordered systems (random Ising models, random Schrödinger operators, etc.)	82D05	cal systems
82B80	Numerical methods (Monte Carlo, series		Plasmas
02000	resummation, etc.)		Liquids
	[See also 65-XX, 81T80]		Solids
82B99	None of the above, but in this section		Crystals (For crystallographic group the-
			ory, see 20H15)
	Time-dependent statistical mechanics (dynamic and nonequilibrium)	82D30	Random media, disordered materials (including liquid crystals and spin
	Foundations		glasses)
82C05	Classical dynamic and nonequilibrium		Metals
82C10	statistical mechanics (general) Quantum dynamics and nonequilib-		Semiconductors
02C10	rium statistical mechanics (general)		Magnetic materials
82C20	Dynamic lattice systems (kinetic Ising,		Ferroelectrics
	etc.) andsystems on graphs		Superfluids
82C21	Dynamic continuum models		Superconductors
	(systems of particles, etc.)		Polymers
82C22	Interacting particle systems [See also 60K35]		Nuclear reactor theory; neutron transport
82C23	Exactly solvable dynamic models [See also 37K60]	82D77	Quantum wave guides, quantum wires [See also 78A50]
82C24	Interface problems; diffusion-limited ag-		Nanostructures and nanoparticles
	gregation	82D99	None of the above, but in this section
82C26	Dynamic and nonequilibrium phase transitions (general)	83-XX	Relativity and gravitational theory
82C27	Dynamic critical phenomena	83-00	General reference works (handbooks,
82C28	Dynamic renormalization group methods [See also 81T17]		dictionaries, bibliographies, etc.)
82C31	Stochastic methods (Fokker-Planck,	83-01	Instructional exposition (textbooks, tutorial papers, etc.)
	Langevin, etc.) [See also 60H10]	83-02	Research exposition (monographs,
82C32	Neural nets [See also 68T05, 91E40, 92B20]	00 02	survey articles)
82C35	Irreversible thermodynamics, including		

Onsager-Machlup theory

83-03	Historical (must also be assigned at least one classification number from Section	83C75	Space-time singularities, cosmic censor-ship, etc.
	01)	83C80	Analogues in lower dimensions
83-04	Explicit machine computation and programs (not the theory of computation or	83C99	None of the above, but in this section
83-05	programming)	83Dxx	Relativistic gravitational theories other
83-06	Experimental work Proceedings, conferences, collections,		than Einstein's, including asymmetric field theories
83-08	etc. Computational methods	83D05	Relativistic gravitational theories other than Einstein's, including asymmetric field theories
	Special relativity Special relativity	83D99	None of the above, but in this section
	None of the above, but in this section	83Exx	Unified, higher-dimensional and super
02P.m	Observational and americantal	83E05	Geometrodynamics
озвах	Observational and experimental questions		Kaluza-Klein and other higher-dimen-
83B05	Observational and experimental	00-1-0	sional theories
	questions None of the above, but in this section	83E30	String and superstring theories [See also 81T30]
03033	None of the above, but in this section	83E50	Supergravity
83Cxx	General relativity	83E99	None of the above, but in this section
	Einstein's equations (general structure,		
	canonical formalism, Cauchy problems)		Cosmology
83C10	Equations of motion		Cosmology
83C15	Exact solutions	83F99	None of the above, but in this section
83C20	Classes of solutions; algebraically special solutions, metrics with symmetries	85-XX	(Astronomy and astrophysics
83C22			(FOR Celestial mechanics, see
	Einstein-Maxwell equations		(For celestial mechanics, see 70F15)
83C25	Approximation procedures, weak fields	85-00	70F15)
83C25	-		70F15) General reference works (handbooks, dictionaries, bibliographies, etc.)
83C25 83C27	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news	85-01	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.)
83C25 83C27 83C30	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, <i>H</i> -spaces, etc.)	85-01	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs,
83C25 83C27 83C30 83C35	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, <i>H</i> -spaces, etc.) Gravitational waves	85-01 85-02	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles)
83C25 83C27 83C30 83C35	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, <i>H</i> -spaces, etc.)	85-01	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least
83C25 83C27 83C30 83C35 83C40	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, <i>H</i> -spaces, etc.) Gravitational waves Gravitational energy and conservation	85-01 85-02	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least
83C25 83C27 83C30 83C35 83C40	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, H-spaces, etc.) Gravitational waves Gravitational energy and conservation laws; groups of motions	85-01 85-02	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and pro-
83C25 83C27 83C30 83C35 83C40 83C45 83C47	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, H-spaces, etc.) Gravitational waves Gravitational energy and conservation laws; groups of motions Quantization of the gravitational field Methods of quantum field theory	85-01 85-02 85-03	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section
83C25 83C27 83C30 83C35 83C40 83C45 83C47	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, H-spaces, etc.) Gravitational waves Gravitational energy and conservation laws; groups of motions Quantization of the gravitational field Methods of quantum field theory [See also 81T20]	85-01 85-02 85-03	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or
83C25 83C27 83C30 83C35 83C40 83C45 83C47	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, H-spaces, etc.) Gravitational waves Gravitational energy and conservation laws; groups of motions Quantization of the gravitational field Methods of quantum field theory [See also 81T20] Electromagnetic fields	85-01 85-02 85-03 85-04	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming)
83C25 83C27 83C30 83C35 83C40 83C45 83C47 83C50 83C55	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, H-spaces, etc.) Gravitational waves Gravitational energy and conservation laws; groups of motions Quantization of the gravitational field Methods of quantum field theory [See also 81T20] Electromagnetic fields Macroscopic interaction of the gravita- tional field with matter (hydrodynamics,	85-01 85-02 85-03 85-04 85-05	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Experimental work Proceedings, conferences, collections,
83C25 83C27 83C30 83C35 83C40 83C45 83C50 83C55	Approximation procedures, weak fields Lattice gravity, Regge calculus and other discrete methods Asymptotic procedures (radiation, news functions, H-spaces, etc.) Gravitational waves Gravitational energy and conservation laws; groups of motions Quantization of the gravitational field Methods of quantum field theory [See also 81T20] Electromagnetic fields Macroscopic interaction of the gravita- tional field with matter (hydrodynamics, etc.)	85-01 85-02 85-03 85-04 85-05 85-06	General reference works (handbooks, dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Experimental work Proceedings, conferences, collections, etc.

		06 4 00	
85Axx	Astronomy and astrophysics		Geostatistics Glaciology
0E A 0.4	(For celestial mechanics, see 70F15)		Geological problems
	General		Miscellaneous topics
	Galactic and stellar dynamics		•
	Galactic and stellar structure	90-XX	Operations research,
	Planetary atmospheres Radiative transfer		mathematical programming
		90-00	General reference works (handbooks,
03A30	Hydrodynamic and hydromagnetic problems [See also 76Y05]	00.01	dictionaries, bibliographies, etc.)
85A35	Statistical astronomy	90-01	Instructional exposition (toythooks tutorial papers etc.)
	Cosmology	00.02	(textbooks, tutorial papers, etc.)
001110	(For relativistic cosmology, see 83F05)	90-02	Research exposition (monographs, survey articles)
85A99	Miscellaneous topics	90-03	Historical (must also be assigned at least
86-XX	Geophysics		one classification number from Section
	[See also 76U05, 76V05]		01)
86-00	General reference works (handbooks,	90-04	Explicit machine computation and pro-
00 00	dictionaries, bibliographies, etc.)		grams (not the theory of computation or programming)
86-01	Instructional exposition	90-06	Proceedings, conferences, collections,
	(textbooks, tutorial papers, etc.)	<i>7</i> 0-00	etc.
86-02	Research exposition (monographs, survey articles)	90-08	Computational methods
86-03	Historical (must also be assigned at least	90Bxx	Operations research and management
	one classification number from Section		science
06.04	01)	90B05	Inventory, storage, reservoirs
86-04	Explicit machine computation and pro-	90B06	Transportation, logistics
	grams (not the theory of computation or programming)	90B10	Network models, deterministic
86-05	Experimental work	90B15	Network models, stochastic
86-06	Proceedings, conferences, collections,	90B18	Communication networks
	etc.	00000	[See also 68M10, 94A05]
86-08	Computational methods	90B20	Traffic problems
		90B22	Queues and service [See also 60K25, 68M20]
86Axx	Geophysics [See also 76U05, 76V05]	90B25	Reliability, availability, maintenance, in-
86A04	General	70 D2 5	spection [See also 60K10, 62N05]
86A05	Hydrology, hydrography, oceanography	90B30	Production models
	[See also 76Bxx, 76E20, 76Q05, 76Rxx,		Scheduling theory, deterministic
86 4 10	76U05]		[See also 68M20]
00A10	Meteorology and atmospheric physics [See also 76Bxx, 76E20, 76N15, 76Q05,	90B36	Scheduling theory, stochastic
	76Rxx, 76U05]		[See also 68M20]
86A15	Seismology	90B40	Search theory
86A17	Global dynamics, earthquake problems	90B50	Management decision making, includ-
86A20	Potentials, prospecting		ing multiple objectives [See also 90C29, 90C31, 91A35, 91B06]
86A22	Inverse problems [See also 35R30]	90B60	Marketing, advertising [See also 91B60]
86A25	Geo-electricity and geomagnetism [See also 76W05, 78A25]		Theory of organizations, manpower
86A30	Geodesy, mapping problems		planning [See also 91D35]

90B80	Discrete location and assignment [See also 90C10]	90C56	Derivative-free methods and methods using generalized derivatives
90B85	Continuous location		[See also 49J52]
90B90	Case-oriented studies	90C57	Polyhedral combinatorics, branch-and-
90B99	None of the above, but in this section	90C59	bound, branch-and-cut Approximation methods and heuristics
00Cva	Mathamatical programming		Abstract computational complexity for
	Mathematical programming [See also 49Mxx, 65Kxx]		mathematical programming problems [See also 68Q25]
	Linear programming	90C70	Fuzzy programming
	Large-scale problems		Applications of mathematical program-
90C08	Special problems of linear programming (transportation, multi-index, etc.)		ming
90C09	Boolean programming	9009	None of the above, but in this section
	Integer programming	91-XX	Game theory, economics, social
	Mixed integer programming		and behavioral sciences
90C15	Stochastic programming	91-00	General reference works (handbooks,
	Quadratic programming		dictionaries, bibliographies, etc.)
	Semidefinite programming	91-01	Instructional exposition
	Convex programming		(textbooks, tutorial papers, etc.)
	Nonconvex programming, global optimization	91-02	Research exposition (monographs, survey articles)
90C27	Combinatorial optimization	91-03	Historical (must also be assigned at least
	Multi-objective and goal programming		one classification number from section
	Nonlinear programming		01)
	Sensitivity, stability, parametric	91-04	Explicit machine computation and pro-
	optimization		grams (not the theory of computation or programming)
	Fractional programming	91-06	Proceedings, conferences, collections,
90C33	Complementarity and equilibrium prob- lems andvariational inequalities (finite dimensions)	91-08	etc. Computational methods
90C34	Semi-infinite programming	91 A xx	Game theory
90C35	Programming involving graphs or net-		2-person games
	works [See also 90C27]		n-person games, $n > 2$
	Dynamic programming [See also 49L20]		Noncooperative games
90C40	Markov and semi-Markov decision processes		Cooperative games
90C46	Optimality conditions, duality [See also 49N15]		Games with infinitely many players Stochastic games
90C47	Minimax problems [See also 49K35]		Games in extensive form
	Programming in abstract spaces		Multistage and repeated games
	Extreme-point and pivoting methods		Evolutionary games
	Interior-point methods		Differential games [See also 49N70]
	Methods of reduced gradient type		Positional games (pursuit and evasion,
	Methods of quasi-Newton type		etc.) [See also 49N75]
	Methods of successive quadratic pro-	91A25	Dynamic games
	gramming type	91A26	Rationality, learning
			Signaling, communication

91A30	Utility theory for games [See also 91B16]	91B55	Economic dynamics
	Decision theory for games	91B60	Trade models
	[See also 62Cxx, 91B06, 90B50]	91B62	Growth models
91A40	Game-theoretic models	91B64	Macro-economic models
91A43	Games involving graphs		(monetary models, models of taxation)
	[See also 05C57]	91B66	Multisectoral models
	Games involving topology or set theory	91B68	Matching models
	Combinatorial games	91B69	Heterogeneous agent models
	Discrete-time games	91B70	Stochastic models
	Games of timing	91B72	Spatial models
91A60	Probabilistic games; gambling [See also 60G40]		Models of real-world systems
91A65	Hierarchical games	91B76	Environmental economics (natural re-
	Spaces of games		source models, harvesting, pollution, etc.)
	Applications of game theory	91B80	Applications of statistical and quantum
91A90	Experimental studies		mechanics to economics (econophysics)
91A99	None of the above, but in this section	91B82	Statistical methods; economic indices and measures
91Bxx	Mathematical economics	91B84	Economic time series analysis
JIDAA	(For econometrics, see 62P20)		[See also 62M10]
91B02	Fundamental topics (basic mathematics,	91B99	None of the above, but in this section
	methodology; applicable to economics		
	in general)	91Cxx	Social and behavioral sciences: general
91B06	Decision theory	01/205	topics (For statistics, see 62-XX)
01 D 00	[See also 62Cxx, 90B50, 91A35]		Measurement theory
	Individual preferences		One- and multidimensional scaling
	Group preferences		Clustering [See also 62H30]
	Voting theory	91C99	None of the above, but in this section
	Social choice	01D	N. d
	Welfare economics	91DXX	Mathematical sociology
	Utility theory	91D10	(including anthropology) Models of societies, social and urban
	Public goods)1D10	evolution
	Price theory and market structure	91D20	Mathematical geography and
	Asset pricing models		demography
91B26	Market models (auctions, bargaining, bidding, selling, etc.)	91D25	Spatial models [See also 91B72]
91B30	Risk theory, insurance	91D30	Social networks
	Resource and cost allocation	91D35	Manpower systems
	Production theory, theory of the firm	04500	[See also 91B40, 90B70]
91B40	Labor market, contracts	91D99	None of the above, but in this section
	Consumer behavior, demand theory		
/ 1 D 1 <u>-</u>	consumer seriavior, acmana meory	91Exx	Mathematical psychology
91B44	-		
	Informational economics	91E10	Cognitive psychology
91B50	Informational economics General equilibrium theory	91E10	Cognitive psychology Psychophysics and psychophysiology;
91B50	Informational economics General equilibrium theory Dynamic stochastic general equilibrium	91E10 91E30	Cognitive psychology Psychophysics and psychophysiology; perception
91B50	Informational economics General equilibrium theory Dynamic stochastic general equilibrium theory	91E10 91E30 91E40	Cognitive psychology Psychophysics and psychophysiology; perception Memory and learning [See also 68T05]
91B50 91B51 91B52	Informational economics General equilibrium theory Dynamic stochastic general equilibrium	91E10 91E30 91E40 91E45	Cognitive psychology Psychophysics and psychophysiology; perception

91Fxx	Other social and behavioral sciences (mathematical treatment)	92Cxx	Physiological, cellular and medical topics	
91F10	History, political science	92C05	Biophysics	
91F20	Linguistics [See also 03B65, 68T50]	92C10	Biomechanics [See also 74L15]	
91F99	None of the above, but in this section	92C15	Developmental biology, pattern formation	
91Gxx	x Mathematical finance		Cell movement (chemotaxis, etc.)	
91G10	Portfolio theory	92C20	Neural biology	
	Derivative securities	92C30	Physiology (general)	
91G30	Interest rates (stochastic models)	92C35	Physiological flow [See also 76Z05]	
	Credit risk	92C37	Cell biology	
91G50	Corporate finance	92C40	Biochemistry, molecular biology	
	Numerical methods	92C42	Systems biology, networks	
	(including Monte Carlo methods)		Kinetics in biochemical problems (phar	
	Statistical methods, econometrics		macokinetics, enzyme kinetics, etc.) [See also 80A30]	
91G00	Financial applications of other theories (stochastic control, calculus of varia-	92C50	Medical applications (general)	
	tions, PDE, SPDE, dynamical systems)		Biomedical imaging and signal process	
91G99	None of the above, but in this section	02660	ing [See also 44A12, 65R10]	
92-XX	Biology and other natural		Medical epidemiology	
	sciences		Plant biology	
92-00	General reference works (handbooks,	92C99	None of the above, but in this section	
	dictionaries, bibliographies, etc.)	92Dxx	Genetics and population dynamics	
92-01	Instructional exposition		Genetics	
	(textbooks, tutorial papers, etc.)		(For genetic algebras, see 17D92)	
92-02	Research exposition (monographs,	92D15	Problems related to evolution	
02.02	survey articles)	92D20	Protein sequences, DNA sequences	
92-03	Historical (must also be assigned at least one classification number from Section		Population dynamics (general)	
	01)		Epidemiology	
92-04	Explicit machine computation and pro-		Ecology	
) _ 01	grams (not the theory of computation or		Animal behavior	
	programming)		None of the above, but in this section	
92-06	Proceedings, conferences, collections,		,	
	etc.	92Exx	Chemistry	
92-08	Computational methods		(For biochemistry, see 92C40)	
r		92E10	Molecular structure (graph-theoretic	
	Mathematical biology in general		methods, methods of differential topol	
92B05	07		ogy, etc.)	
92B10	Taxonomy, statistics	92E20	,	
	General biostatistics [See also 62P10]	02500	[See also 80A30, 80A32]	
92B20	Neural networks, artificial life and related topics [See also 68T05, 82C32, 94Cxx]	92E99	None of the above, but in this section	
92B25	Biological rhythms and synchronization			
92B99	None of the above, but in this section			

Systems theory; control

92Fxx	Other natural sciences		Geometric methods
	(should also be assigned at least one	93B28	Operator-theoretic methods
	other classification number in this	02020	[See also 47A48, 47A57, 47B35, 47N70]
	section)	93B30	•
92F05	Other natural sciences		Sensitivity (robustness)
	(should also be assigned at least one	93B36	H^{∞} -control
02500	other classification number in section 92)	93B40	Computational methods
92F99	None of the above, but in this section		Synthesis problems
93-XX	Systems theory; control	93B51	Design techniques (robust design, com-
	(For optimal control, see 49-XX)	02052	puter-aided design, etc.)
93-00	General reference works (handbooks,		Feedback control
	dictionaries, bibliographies, etc.)		Pole and zero placement problems
93-01	Instructional exposition		Eigenvalue problems
	(textbooks, tutorial papers, etc.)	93B99	None of the above, but in this section
93-02	Research exposition (monographs,		
	survey articles)		Control systems
93-03	Historical (must also be assigned at least		Linear systems
	one classification number from Section		Nonlinear systems
93-04	01) Explicit machine computation and pro-	93C15	Systems governed by ordinary differential equations [See also 34H05]
	grams (not the theory of computation or programming)	93C20	Systems governed by partial differential equations
93-06	Proceedings, conferences, collections, etc.	93C23	Systems governed by functional-differential equations [See also 34K35]
93Axx	General	93C25	Systems in abstract spaces
93A05	Axiomatic system theory		Systems governed by functional rela-
93A10	General systems		tions other than differential equations
93A13	Hierarchical systems		(such as hybrid and switching systems)
93A14	Decentralized systems	93C35	Multivariable systems
93A15	Large scale systems	93C40	Adaptive control
93A30	Mathematical modeling (models of sys-	93C41	Problems with incomplete information
	tems, model-matching, etc.)	93C42	Fuzzy control systems
93A99	None of the above, but in this section	93C55	Discrete-time systems
		93C57	Sampled-data systems
93Bxx	Controllability, observability, and sys-	93C62	Digital systems
	tem structure	93C65	Discrete event systems
93B03	Attainable sets	93C70	Time-scale analysis and singular pertur-
93B05	Controllability		bations
93B07	Observability		Perturbations
93B10	Canonical structure		Frequency-response methods
93B11	System structure simplification	93C83	Control problems involving computers
93B12	Variable structure systems		(process control, etc.)
93B15	Realizations from input-output data	93C85	Automated systems (robots, etc.)
93B17	Transformations	02607	[See also 68T40, 70B15, 70Q05]
93B18	Linearizations		Applications
93B20	Minimal systems representations	93C99	None of the above, but in this section
93B25	Algebraic methods		

	Stability	94A08	Image processing (compression, reconstruction, etc.) [See also 68U10]		
93D05	Lyapunov and other classical stabilities (Lagrange, Poisson, L^p , l^p , etc.)	94A11	Application of orthogonal and other sp cial functions		
93D09	Robust stability	94A12	Signal theory (characterization, recon-		
93D10	Popov-type stability of		struction, filtering, etc.)		
	feedback systems	94A13	Detection theory		
	Stabilization of systems by feedback	94A14	Modulation and demodulation		
	Asymptotic stability	94A15	Information theory, general		
	Adaptive or robust stabilization		[See also 62B10, 81P94]		
	Input-output approaches		Measures of information, entropy		
	Scalar and vector Lyapunov functions		Sampling theory		
93D99	None of the above, but in this section		Coding theorems (Shannon theory)		
			Source coding [See also 68P30]		
	Stochastic systems and control		Rate-distortion theory		
	Stochastic systems, general		Channel models (including quantum)		
	Estimation and detection [See also 60G35]		Prefix, length-variable, comma-free codes [See also 20M35, 68Q45]		
	Filtering [See also 60G35]		Theory of questionnaires		
	System identification	94A55	Shift register sequences and sequences		
	Data smoothing	0.4.4.60	over finite alphabets		
	Stochastic stability Optimal stochastic control	94A60	Cryptography [See also 11T71, 14G50, 68P25, 81P94]		
93E24	Least squares and related methods	94A62	Authentication and secret sharing		
93E25	Other computational methods		[See also 81P94]		
93E35	Stochastic learning and adaptive control	94A99	None of the above, but in this section		
93E99	None of the above, but in this section	0.470			
94-XX	Information and communica-	94BXX	Theory of error-correcting codes and error-detecting codes		
	tion, circuits	94B05	Linear codes, general		
94-00	General reference works (handbooks,	94B10	Convolutional codes		
	dictionaries, bibliographies, etc.)	94B12	Combined modulation schemes		
94-01	Instructional exposition		(including trellis codes)		
04.00	(textbooks, tutorial papers, etc.)	94B15	Cyclic codes		
94-02	Research exposition (monographs,	94B20	Burst-correcting codes		
04.02	survey articles)	94B25	Combinatorial codes		
94-03	Historical (must also be assigned at least one classification number from Section	94B27	\ 0 11		
	01)		tions of algebraic geometry) [See also 11T71, 14G50]		
94-04	Explicit machine computation and pro-	94B30	Majority codes		
	grams (not the theory of computation or	94B35	Decoding		
	programming)	94B40	Arithmetic codes [See also 11T71, 14G50]		
94-06	Proceedings, conferences, collections,	94B50	Synchronization error-correcting codes		
	etc.	94B60	Other types of codes		
94Axx	Communication, information	94B65	Bounds on codes		
94A05	Communication theory [See also 60G35, 90B18]	94B70	Error probability		

Mathematics education

94B75	Applications of the theory of convex sets and geometry of numbers (covering ra-		Popularization of mathematics
	dius, etc.) [See also 11H31]	97 A99	None of the above, but in this section
94B99	None of the above, but in this section		Educational policy and systems
94Cxx	Circuits, networks		Educational research and planning
	Analytic circuit theory		General education
	Switching theory, application of Boolean		Vocational education
71010	algebra; Boolean functions		Higher education
	[See also 06E30]	97B50	Teacher education
94C12	Fault detection; testing	07040	(For research aspects, see 97C70)
94C15	Applications of graph theory	97B60	Adult and further education
	[See also 05Cxx, 68R10]		Syllabuses, educational standards
94C30	Applications of design theory [See also 05Bxx]	97899	None of the above, but in this section
94C99	None of the above, but in this section	97Cxx	Psychology of mathematics education, research in mathematics education
94Dxx	Fuzzy sets and logic (in connection	97C10	Comprehensive works
, , , , , , ,	with questions of Section 94)	97C20	Affective behavior
	[See also 03B52, 03E72, 28E10]	97C30	Cognitive processes, learning theories
94D05	Fuzzy sets and logic (in connection with	97C40	Intelligence and aptitudes
	questions of Section 94)	97C50	Language and verbal communities
	[See also 03B52, 03E72, 28E10]	97C60	Sociological aspects of learning
94D99	None of the above, but in this section	97C70	Teaching-learning processes
97-XX	Mathematics education	97C99	None of the above, but in this section
07.00			
97-00	General reference works (handbooks,		
	dictionaries, bibliographies, etc.)	97Dxx	Education and instruction
97-00	dictionaries, bibliographies, etc.) Instructional exposition		in mathematics
97-01	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.)		in mathematics Comprehensive works,
	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs,	97D10	in mathematics Comprehensive works, comparative studies
97-01	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least	97D10 97D20	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics)
97-01 97-02	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section	97D10 97D20 97D30	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals
97-01 97-02	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least	97D10 97D20 97D30	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics)
97-01 97-02 97-03	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01)	97D10 97D20 97D30 97D40	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic
97-01 97-02 97-03	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or	97D10 97D20 97D30 97D40	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques
97-01 97-02 97-03 97-04	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming)	97D10 97D20 97D30 97D40 97D50	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx)
97-01 97-02 97-03 97-04 97-06	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc.	97D10 97D20 97D30 97D40 97D50	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx)
97-01 97-02 97-03 97-04 97-06 97-08	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education	97D10 97D20 97D30 97D40 97D50	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement con-
97-01 97-02 97-03 97-04 97-06 97Axx 97A10	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education Comprehensive works, reference books	97D10 97D20 97D30 97D40 97D50 97D60 97D70	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating
97-01 97-02 97-03 97-04 97-06 97Axx 97A10	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education	97D10 97D20 97D30 97D40 97D50 97D60 97D70 97D80	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating Learning difficulties and student errors
97-01 97-02 97-03 97-04 97-06 97Axx 97A10 97A20	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education Comprehensive works, reference books Recreational mathematics, games	97D10 97D20 97D30 97D40 97D50 97D60 97D70 97D80	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating Learning difficulties and student errors Teaching units and draft lessons
97-01 97-02 97-03 97-04 97-06 97Axx 97A10 97A20	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education Comprehensive works, reference books Recreational mathematics, games [See also 00A08]	97D10 97D20 97D30 97D40 97D50 97D60 97D70 97D80 97D99	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating Learning difficulties and student errors Teaching units and draft lessons
97-01 97-02 97-03 97-04 97-06 97Axx 97A10 97A20 97A30	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education Comprehensive works, reference books Recreational mathematics, games [See also 00A08] History of mathematics and mathemat-	97D10 97D20 97D30 97D40 97D50 97D60 97D70 97D80 97D99	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating Learning difficulties and student errors Teaching units and draft lessons None of the above, but in this section
97-01 97-02 97-03 97-04 97-06 97Axx 97A10 97A20 97A30 97A40	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education Comprehensive works, reference books Recreational mathematics, games [See also 00A08] History of mathematics and mathematics education [See also 01-XX]	97D10 97D20 97D30 97D40 97D50 97D60 97D70 97D80 97D99 97Exx 97E10	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating Learning difficulties and student errors Teaching units and draft lessons None of the above, but in this section Foundations of mathematics
97-01 97-02 97-03 97-04 97-06 97Axx 97A10 97A20 97A30 97A40 97A50	dictionaries, bibliographies, etc.) Instructional exposition (textbooks, tutorial papers, etc.) Research exposition (monographs, survey articles) Historical (must also be assigned at least one classification number from Section 01) Explicit machine computation and programs (not the theory of computation or programming) Proceedings, conferences, collections, etc. General, mathematics and education Comprehensive works, reference books Recreational mathematics, games [See also 00A08] History of mathematics and mathematics education [See also 01-XX] Mathematics and society	97D10 97D20 97D30 97D40 97D50 97D60 97D70 97D80 97D99 97Exx 97E10	in mathematics Comprehensive works, comparative studies Philosophical and theoretical contributions (maths didactics) Objectives and goals Teaching methods and classroom techniques Teaching problem solving and heuristic strategies (For research aspects, see 97Cxx) Student assessment, achievement control and rating Learning difficulties and student errors Teaching units and draft lessons None of the above, but in this section Foundations of mathematics Comprehensive works Philosophy and mathematics

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97E40	Language of mathematics	97170	Functional equations
97E50	Reasoning and proving in the mathe-	97180	Complex analysis
	matics classroom	97199	None of the above, but in this section
	Sets, relations, set theory		
97E99 	None of the above, but in this section	97Kxx	Combinatorics, graph theory, probability theory, statistics
97Fxx	Arithmetic, number theory	97K10	Comprehensive works
97F10	Comprehensive works	97K20	Combinatorics
97F20	Pre-numerical stage, concept of numbers	97K30	Graph theory
97F30	Natural numbers	97K40	Descriptive statistics
97F40	Integers, rational numbers	97K50	Probability theory
97F50	Real numbers, complex numbers	97K60	Distributions and stochastic processes
97F60	Number theory	97K70	Foundations and methodology of statis-
97F70	Measures and units		tics
97F80	Ratio and proportion, percentages		Applied statistics
97F90	Real life mathematics, practical arith-	97K99	None of the above, but in this section
07700	metic		
97F99	None of the above, but in this section	97Mxx	Mathematical modeling, applications
		073.610	of mathematics
	Geometry		Modeling and interdisciplinarity
	Comprehensive works	97M20	Mathematics in vocational training and career education
	Informal geometry	97M30	Financial and insurance mathematics
	Areas and volumes		Operations research, economics
	Plane and solid geometry		Physics, astronomy, technology,
	Transformation geometry	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	engineering
	Plane and spherical trigonometry	97M60	Biology, chemistry, medicine
	Analytic geometry. Vector algebra		Behavioral and social sciences
	Descriptive geometry	97M80	Arts, music, language, architecture
97G99	None of the above, but in this section		None of the above, but in this section
	Algebra	07Nixx	Numerical mathematics
	Comprehensive works		Comprehensive works
97H20	Elementary algebra		-
97H30	Equations and inequalities		Rounding, estimation, theory of errors
97H40	Groups, rings, fields		Numerical anglysis
97H50	Ordered algebraic structures		Numerical analysis
97H60	Linear algebra		Interpolation and approximation
97H99	None of the above, but in this section		Mathematical programming Discrete mathematics
97Ixx	Analysis	9/11/00	Mathematical software, computer programs
97I10	Comprehensive works	97N199	None of the above, but in this section
97I20	Mappings and functions	71± N 77	rone of the above, but in this section
97I30	Sequences and series	97Pvv	Computer science
97I40	Differential calculus	97PXX 97P10	-
97I50	Integral calculus	97F 10	Theory of computer science
97160	Functions of several variables	97F 20	-
		271 30	System somware

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97P40	Programming languages	97R20	Applications in mathematics
97P50	Programming techniques	97R30	Applications in sciences
97P60	Hardware	97R40	Artificial intelligence
97P70	Computer science and society	97R50	Data bases, information systems
97P99	None of the above, but in this section	97R60	Computer graphics
		97R70	User programs,
97Qxx	Computer science education		administrative applications
97Q10	Comprehensive works	97R80	Recreational computing
97Q20	Affective aspects in teaching computer	97R99	None of the above, but in this section
	science		
	Cognitive processes	97Uxx	Educational material and media, edu-
97Q40	Sociological aspects		cational technology
97Q50	Objectives	97U10	Comprehensive works
97Q60	Teaching methods and	97U20	Textbooks. Textbook research
	classroom techniques	97U30	Teachers' manuals and planning aids
97Q70	Student assessment	97U40	Problem books. Competitions.
97Q80	Teaching units		Examinations
97Q99	None of the above, but in this section	97U50	Computer assisted instruction; e-learning
07D	0 1 1 1	97U60	Manipulative materials
	Computer science applications		Technological tools, calculators
97K10	Comprehensive works,		Audiovisual media
	collections of programs		
		9/099	None of the above, but in this section

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